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| Author: René König, 268127 | Open | |
| numor. Rene Ronig, 20012/ | | |
| | | |
| | | |
| Supervisor at UiS: Professor Aksel Hiorth | | |
| Supervisor at Clo. 17 of essor Time et 11 tor th | | |
| Co-supervisor: Professor Jasna Bogunovic Jakobsen | | |
| Co Supervisor. 1 rojessor susha Boyanova | Councosen | |
| External supervisor(s): Bernardo Morais o | da Costa, Statens neanesen | |
| External supervisor (s). Bernar as morals | au Costa, Statens begresen | |
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| | René Konis | |
| | here Konig | |
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Abstract

The Lysefjord Bridge is a suspension bridge at the entrance to the Lysefjord in south-western Norway at which full-scale measurements on wind conditions and bridge response are collected using anemometers and accelerometers. In this work Python is used to develop a toolset for analysing the wind and response measurement data from the Lysefjord Bridge. The functionality is provided through different methods compiled in a class. This includes methods for importing and combining data from multiple days, re-arranging and interpreting the data, feature engineering, data cleaning, filtering and various types of visualisations. The code is demonstrated in an analysis of 30 days of data. The analysis focuses on the wind conditions for south-westerly and north-easterly winds in terms of wind speeds, primary directions, turbulence intensity and angle of attack as well as the bridges lateral, vertical and torsional wind response. The analysis shows on average slightly higher wind speeds, lower turbulence intensities and higher angles of attack for south-westerly winds, compared to north-easterly winds. Towards the southern end of the bridge the wind direction has a south tendency for south-westerly winds and north tendency for north-easterly winds. Turbulence intensity is measured slightly higher on the downwind side of the bridge. The angle of attack is straightened towards 0° on the downwind side. Furthermore, the analysis shows that the assumption of a linear correlation between drag coefficient and angle of attack used in the so-called quasi-steady theory of wind loading and the corresponding numerical simulations underestimates most of the larger lateral bridge responses at angles of attack above 0°. The lift and moment coefficients estimated using similar linearity assumptions overestimate some of the larger vertical and torsional bridge responses at angles of attack above +5°.



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List of Abbreviations

The following abbreviations and acronyms are used in the data, code and documentation of this work:

| acc | Accelerometer |
|---------|-------------------------------------------------------|
| anemo | Anemometer |
| CFD | Computational fluid dynamics |
| id | Identification |
| IDE | Integrated development environment |
| ind | Index |
| key | Key of a key-value pair in a dictionary |
| LFB | Lysefjord Bridge |
| MATLAB | Matrix laboratory |
| N/E/S/W | North, East, South or West. Combinations possible. |
| NaN | Not a number |
| NumPy | Numerical Python |
| pandas | Python Data Analysis Library, derived from panel data |
| PEP | Python Enhancement Proposal |
| SSV | Statens vegvesen |
| UiS | Universitetet i Stavanger |
| VSCode | Visual Studio Code |



List of Symbols

The following symbols are used in the data, code and documentation of this work:

| $C_{D/L/M}$ | Wind load coefficient for drag, lift or moment | |
|----------------------------------------------------------------|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|--|
| $F_{D/L/M}$ | Drag, lift or moment | |
| <i>S</i> _t | Strouhal number | |
| U_r | Resonance wind velocity | |
| f_S | Vortex shedding frequency | |
| f_e | Eigenfrequency | |
| AOA | Angle of attack, commonly incidence angle α | |
| AOI | Horizontal angle of incidence, commonly yaw angle β | |
| Aox | Lateral acceleration | |
| Aoy | Longitudinal acceleration | |
| Aoz | Vertical acceleration | |
| Dir | Wind direction, direction from which the wind is blowing, commonly $\boldsymbol{\Theta}$ | |
| h | Height of the bridge girder | |
| H/V/T S/A # | Horizontal, vertical or torsional (a)symmetric eigenmode number # | |
| H | Horizontal wind component, commonly \emph{U} | |
| H ## E/W t/b Hanger number ## East or West top or bottom | | |
| H ## E/VV t/b | Hanger number ## East or West top or bottom | |
| H ## E/VV Vb Hum | | |
| | Humidity | |
| Hum | Humidity | |
| Hum P T | Humidity | |
| Hum P T theta | Humidity Pressure Temperature | |
| Hum P T theta Vx | Humidity Pressure Temperature Torsional acceleration along the longitudinal axis (calculated), com. θ | |
| Hum P T theta Vx Vy | HumidityPressureTemperatureTorsional acceleration along the longitudinal axis (calculated), com. θLateral across-bridge wind component in x-direction | |
| Hum P T theta Vx Vy | HumidityPressureTemperatureTorsional acceleration along the longitudinal axis (calculated), com. θLateral across-bridge wind component in x-directionLongitudinal along-bridge wind component in y-direction | |
| Hum P T theta Vx Vy U | HumidityPressureTemperatureTorsional acceleration along the longitudinal axis (calculated), com. θLateral across-bridge wind component in x-directionLongitudinal along-bridge wind component in y-directionVertical wind component | |
| Hum P T theta Vx Vy U | HumidityPressureTemperatureTorsional acceleration along the longitudinal axis (calculated), com. θLateral across-bridge wind component in x-directionLongitudinal along-bridge wind component in y-directionVertical wind componentWean wind speedWidth of the bridge girder | |



List of Indices

The following indices are used in the data, code and documentation of this work in combination with some of the symbols from List of Symbols:

| _C | Central acceleration (calculated) |
|-------------|----------------------------------------------------------------------------------|
| _E | East side accelerometer |
| _max | Maximum of 10-minute data package |
| _max_by_std | Quotient of _max and _std |
| _mean | Mean of 10-minute data package, commonly overlined, e.g. $\overline{\mathbf{U}}$ |
| _min | Minimum of 10-minute data package |
| _std | Standard deviation of 10-minute data package, commonly $\boldsymbol{\sigma}$ |
| _turb | Turbulence intensity of 10-minute data package, commonly I_i |
| _W | West side accelerometer |



1 Introduction

The collapse of the Tacoma Narrows Bridge in 1940 is a famous example for the response of a mechanical structure to wind leading to its destruction. The still-frame from Barney Elliott's film-recording of the Tacoma Narrows Bridge in Figure 1 shows the suspension bridge twisting in a torsional vibration mode in a dynamic response to wind with speeds of up to 65 km/h.



Figure 1: Tacoma Narrows Bridge as the wind induced destruction is imminent [1]

While the bridge has been designed and built for a static wind force of 160 km/h, this extreme dynamic response was unforeseen, as no dynamic analysis has been carried out. [2, p. 4]

This shows the importance of analysing the wind response of a structure to prevent over-stressing the structure.

"The Norwegian Public Road Administration is considering building long-span floating suspension bridges in Western Norway to cross deep fjords that are up to around 5 km wide. [...] They are therefore extremely wind sensitive structures which require a dedicated investigation of wind-induced effects." [3]



Understanding the wind field characteristics in the complex terrain of the fjords and the wind response of a bridge is essential for those construction projects. Full-scale monitoring of wind and wind response at existing bridges is carried out to help understand these effects.

1.1 The Lysefjord Bridge



Figure 2: Lysefjord Bridge North view at H11. Adapted from [4]



Figure 3: Lysefjord Bridge viewed from the West. Adapted from [5]

The Lysefjord Bridge displayed in Figure 2 and Figure 3 is a suspension bridge located at the entrance of the Lysefjord in South-Western Norway, as shown in Figure 4 and Figure 5.





Figure 4: Map of the Stavanger and Lysefjord area. Adapted from [6]



Figure 5: Aerial footage of the Lysefjord Bridge.

Figure 5 shows an aerial photograph of the Lysefjord Bridge at the entrance to the Lysefjord taken by the author.



The bridge is a critical transportation link in the region. It facilitates the transport of goods and people from Stavanger to the municipality of Forsand and other communities south of the Lysefjord and back. This includes heavy industry such as the Norsk Spennbetong AS concrete plant and NCC Helle sandtak sand pit, as depicted in Figure 6. [7, p. 3], [8]



Figure 6: Heavy industry route to Stavanger via Lysefjord Bridge and Ryfylke Tunnel. Adapted from [8]

Note that the Ryfylke Tunnel connecting Stavanger to Ryfylke first opened at the end of 2019. Before the opening of the tunnel, the traffic across the bridge had to take the Lauvvik-Oanes Ferry, as depicted in Figure 7.





Figure 7: Heavy industry route to Stavanger via Lysefjord Bridge and Lauvvika-Oanes Ferry. Adapted from [9]

While there is also a ferry quay directly in Forsand, enabling traffic to take other ferry routes and by-passing the Lysefjord Bridge, it should be noted that ferry connections have a limited capacity, run at a schedule and are less reliable, compared to a road connection. The Lauvvika-Oanes ferry for example is currently discontinued. [10]



The bridge was built from 1995 to 1997 at a cost of 150 million Norwegian kroner. It has a total length of 639 m with a main span of 446 m. The towers stand at a height of 102.26 m. The main cables have a sag of 45 m, as depicted in Figure 8. [7, p. 3], [3, p. 2]

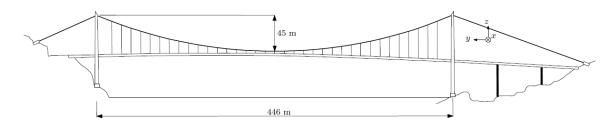


Figure 8: Schematic of the Lysefjord Bridge (sideview from the West) [3, p. 3]

The bridge is asymmetric with the bridge deck support at a height of 52.36 m at the north tower and 44.9 m at the south tower. The bridge girder is suspended from the two main cables by 35 hanger pairs with a longitudinal distance of 12 m between hanger pairs and 19 m between the outmost hangers and the towers. At mid-span, hanger 18 (H18), the deck is suspended 53.37 m above the sea surface with the main cables at their lowest point 3 m above the deck. The girder has a closed steel cross section with a height of 2.76 m and width of 12.3 m, as depicted in Figure 9. [7, pp. 3,5], [3, p. 2]

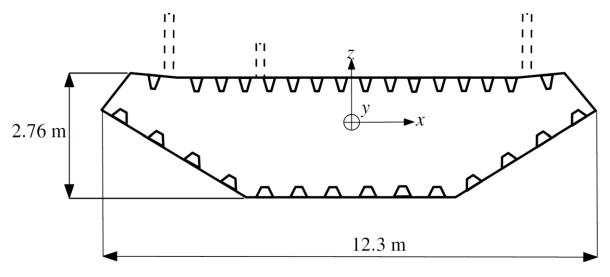


Figure 9: Girder cross section [7, p. 11]



1.1.1 Wind conditions in the surrounding area

The wind in the area around the Lysefjord Bridge is highly influenced by the rough terrain created by the mountains, valleys and fjords. Figure 11 - Figure 15 show the wind directions and monthly strength distributions at different locations around the Stavanger and Lysefjord area. Note that not all weatherstations have been actively reporting data in the same time periods and are therefore not directly compareable. Figure 10 shows a compilation of wind roses overlayed on an overview map of the area. Note that there are currently no weather stations further to the East of the bridge published on windfinder.com.



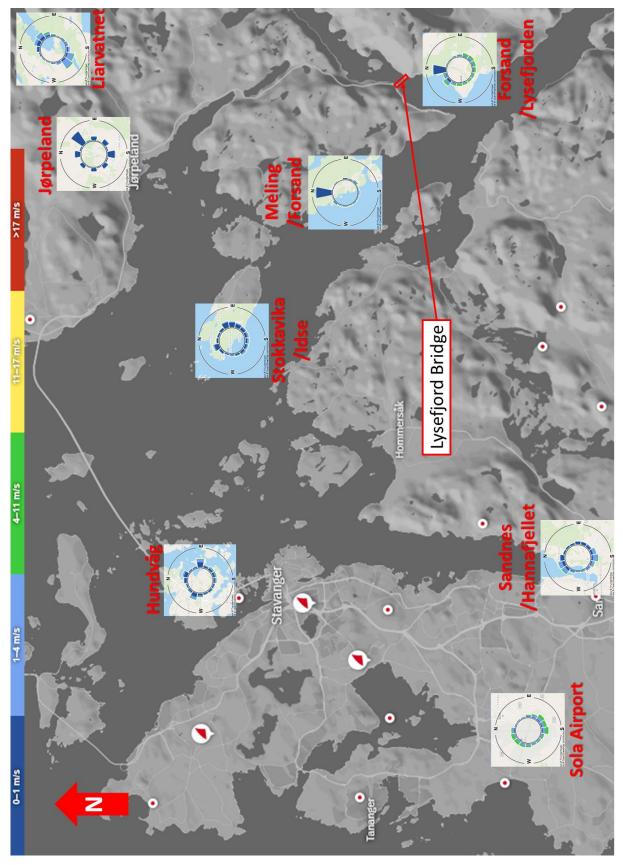


Figure 10: Wind map of the area around the Lysefjord Bridge. Adapted from [11], [12], [13], [14], [15], [16], [17]



The Forsand weather station depicted in Figure 11 has been the closest weather station to the Lysefjord Bridge, about 2 km to the South of the bridge, at the entrance to the Fjord.

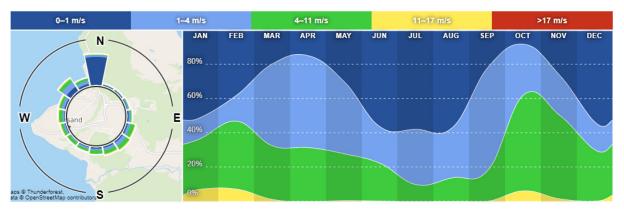


Figure 11: Wind directions and monthly strength distribution at Forsand/Lysefjorden (05/2012 - 02/2017) [11]

Note that the high number of data showing winds of up to 1 m/s from direct North visible in the wind rose might be outliers due to errors in the measurements or averaging method and can be disregarded, as they are for very low windspeeds. The primary wind directions at this weather station are therefore most likely NW and SE, following the orientation of the foot of the mountain to the east. Figure 11 shows relatively high windspeeds at Forsand, especially in the spring and autumn period where more than 40% or even 60% of the wind respectively is recorded at over 4 m/s. This is relatively high, compared to the other weather stations. An exception to this is the weather station at Sola Airport, which is depicted in Figure 12.



The weather station at Sola Airport depicted in Figure 12 is located about 20 km to the West of the Lysefjord Bridge, directly at the Atlantic coast.

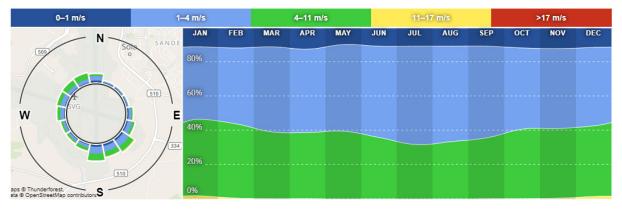


Figure 12: Wind directions and monthly strength distribution at Sola Airport (01/2002 - 04/2023) [14]

The primary wind directions at Sola Airport are NW and SSE. The wind strength distribution is relatively consistent throughout the year with about 40% of the wind recorded at over 4 m/s.

The Meling weather station depicted in Figure 13 has been the second closest weather station to the Lysefjord Bridge, located on the NE-shore of the Høgsfjord, about 5 km NW of the bridge.

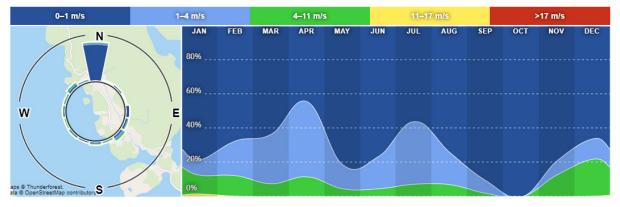


Figure 13: Wind directions and monthly strength distribution at Meling/Forsand (04/2014 - 02/2017) [16]

Note that similarly to the weather station in Forsand there are possibly outliers displaying a lot of wind from the North. This data can again be ignored. The primary wind directions are therefore most likely SE and NW, following the orientation of the shoreline. The wind speeds are below 4 m/s about 90% of the time from February to October. In December about 20% of the wind speeds recorded are above 4 m/s.



The weather station in Stokkavika depicted in Figure 14 is located on the island of Idse in the Høgsfjord, about 12.5 km NW of the Bridge.

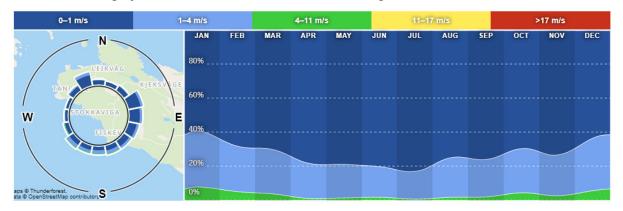


Figure 14: Wind directions and monthly strength distribution at Stokkavika/Idse (04/2014 - 05/2020) [15]

The windspeeds are below 4 m/s about 95% of the time throughout the year and the wind directions are variable with a slight tendency to a broad range of south-westerly winds and a narrow band of NNW winds.

The weather station at Liarvatnet depicted in Figure 15 is about 14 km to the North of the Lysefjord Bridge, in the valley of the Liarvatnet lake.



Figure 15: Wind directions and monthly strength distribution at Liarvatnet (04/2014 - 04/2023) [12]

The primary wind directions at Liarvatnet are SW and NE, which follows the orientation of the valley. About 90% of the wind is below 4 m/s throughout the whole year.



Computational fluid dynamics (CFD) simulations have been used in [18] to better understand the influence of the terrain on the wind flow characteristics at the entrance to the Lysefjord. Results from the CFD simulations with different wind directions are displayed in Figure 16 and Figure 17.

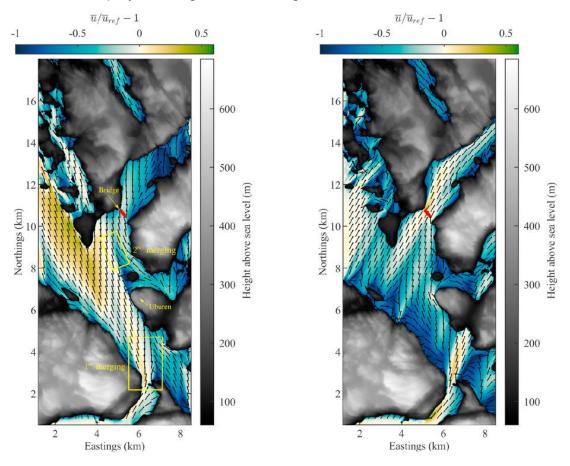


Figure 16: Normalized mean horizontal wind velocity 60m above the surface simulated with a direction of 168° (left) and 210° (right) at the inlet boundary [18, p. 10]

Figure 16 shows how a flow from south-easterly directions through the Høgsfjord can turn to a flow from SSW when entering the Lysefjord. It should be noted that a CFD simulation, such as any simulation or model, is only a model of reality that has its limitations and cannot replicate reality in all its complexity. However, they can still be useful.

"All models are wrong but some are useful" [19]



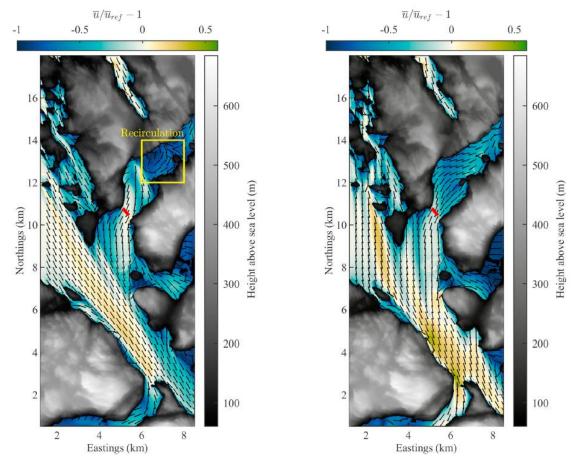


Figure 17: Normalized mean horizontal wind velocity 60m above the surface simulated with a direction of 335° (left) and 355° (right) at the inlet boundary [18, p. 12]

Figure 17 shows how small changes in the wind direction at the inlet boundary can create a recirculation zone in the Lysefjord north-east of the bridge. A detailed description of the simulation and the results can be found in [18].



1.1.2 Wind definitions

Figure 18 illustrates the wind definitions in the horizontal plane used in this work for SSW (left) and NNE wind conditions (right).

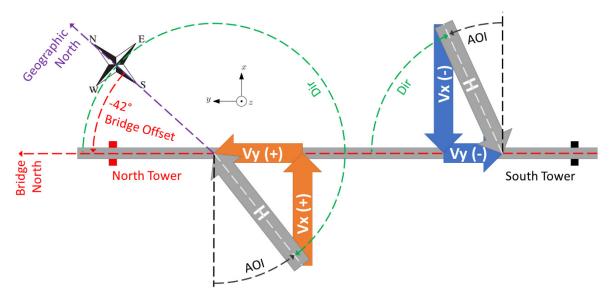


Figure 18: Horizontal wind definitions in this work for a SSW (left) and NNE wind condition (right)

The direction from the *south tower* (right) towards the *north tower* (left) is defined as *bridge north*. *Bridge north* is offset from *geographic north* by about -42°. The direction from which the horizontal wind component *H* is blowing from, measured from *bridge north*, is defined as *Dir* from 0° to 360° in clockwise direction. The lateral component of *H* along the x-axis of the bridge coordinate system is defined as *Vx*. The longitudinal component along the y-axis is defined as *Vy*. *Vx* and *Vy* are defined positive in the direction they are blowing to in reference to the bridge coordinate system. This means that a wind from SSW has positive *Vx* and *Vy* and wind from NNE has negative *Vx* and *Vy*.

Some wind engineering models assume a wind field that is coming in perpendicular to the bridge's primary axis. The deviation of the horizontal wind vector H from this perpendicular direction is defined as the angle of incidence (AOI), in wind engineering commonly referred to as the yaw angle. The AOI has no sign.



The vertical wind definitions used in this work for positive (bottom) and negative (top) angle of attack (AOA) are depicted in Figure 19.

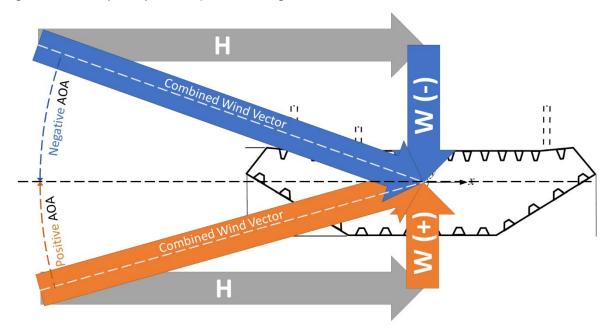


Figure 19: Vertical wind definitions in this work for a positive (bottom) and negative AOA (top). Adapted from [7, p. 11]

The wind vector is a combination of the horizontal component H and vertical component W. W is defined as positive in positive z-direction (bottom) and negative in negative z-direction (top). The angle between the horizontal x-y-plane of the bridge coordinate system and the combined wind vector is the angle of attack (AOA). The AOA is defined as positive for positive W and negative for negative W.



1.2 The data

A field measurement campaign on wind conditions and bridge response at the Lysefjord Bridge by the research group from University of Stavanger started in 2013. [3, p. 2]

The composition of the instrumentation on the bridge has developed over time. It primarily consists of sonic anemometers mounted above the bridge deck and pairs of accelerometers mounted inside the bridge girder.

1.2.1 Anemometers

The sonic anemometers used are 3D WindMaster Pro sonic anemometers from Gill Instrument Ltd. The anemometers can measure wind speeds of up to 65 m/s in all three directions, converted into horizontal and vertical wind components and wind direction. On hanger 10 the anemometer is part of the Vaisala weather transmitter WXT520 and measures horizontal wind speeds of up to 60 m/s and wind direction. [7, pp. 3-6], [20, pp. 35-38], [21, p. 1], [22, pp. 25-27,140]





Figure 20: Anemometer mounting positions on a hanger (left) and on a pole on top of the main cable (right) [7, p. 5]

The anemometers are usually mounted on the hangers, as depicted in Figure 20 (left). Where this method would not position them high enough above the deck, the anemometers are mounted on a pole above the main cable, as depicted in Figure 20 (right). Note that the anemometers are aligned with the bridge axis in a way that the reported wind direction from the North is wind blowing from the north tower parallel along the bridge towards the south tower. This direction is offset by -42° from geographic North due to the bridge's orientation.



1.2.2 Accelerometers

The accelerometers used are triaxial microelectromechanical silicon accelerometers with a range of ±5g by Canterbury Seismic Instruments Ltd. [23]

The accelerometers are mounted inside the bridge girder as depicted in Figure 21.





Figure 21: Accelerometer mounting position inside the bridge girder [7, p. 6]

Figure 22 shows the position of the accelerometers in the girder cross section.

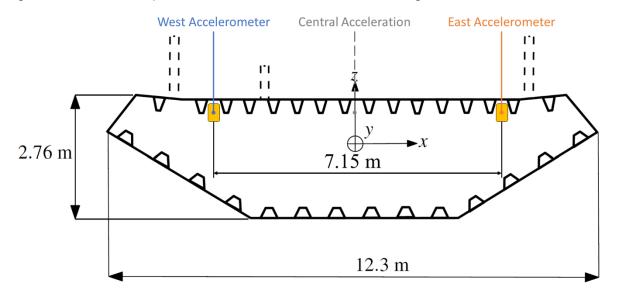


Figure 22: Girder cross section with accelerometers. Adapted from [7, p. 11]

The pairwise installation of the accelerometers allows the monitoring of torsional accelerations (theta) along the bridge's longitudinal axis (y-axis) in addition to the central translational accelerations in lateral, longitudinal and vertical direction (Aox, Aoy and Aoz). The lateral distance of the accelerometers is 7.15 m. [20, pp. 35-38]



1.2.3 Instrumentation Layout

The sensors' positions are denoted as shown in the naming convention depicted in Figure 23. Note that accelerometer pairs are denoted only by the hanger number.

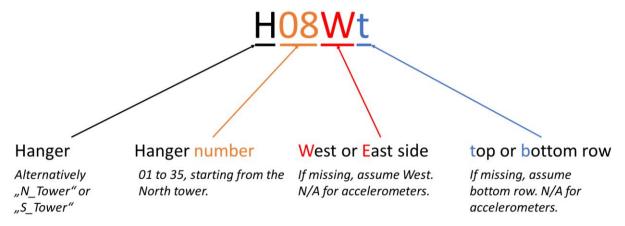


Figure 23: Sensor naming convention.

Bottom row anemometers are mounted 6 m above the bridge deck while top row anemometers are mounted 10 m above the bridge deck.

Figure 24 shows an overview of the instrumentation of the Lysefjord Bridge in July 2017.

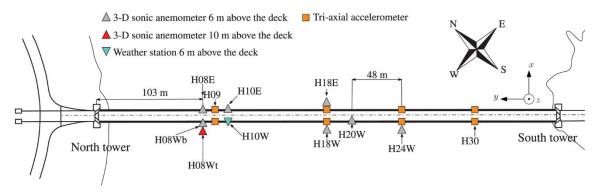


Figure 24: Overview of the instrumentation of the Lysefjord Bridge in July 2017. Adapted from [24, p. 3]

Initially six anemometers have been fitted to the west side of the bridge at hangers 08, 16, 18, 20 and 24, denoted H08Wb, H16W, H18W, H20W and H24W, with the weather station at H10W.

Four pairs of accelerometers have been installed at H09, H18, H24 and H30. Note that in the MATLAB files the position of the accelerometer pair at H24 is mistakenly denoted as H20. This mistake might have carried over in parts of this work during the import of the MATLAB files. Any mentioning of H20 in reference to an accelerometer is therefore to be interpreted as H24.



At hanger 08 an additional anemometer has been installed 10 m above the deck in June 2014, denoted H08Wt. [7, pp. 3-6], [20, pp. 35-38]

In 2014 an additional anemometer has been installed on top of the north tower, denoted N_Tower, which has been rendered un-operational in the same year.

In June 2017 additional anemometers have been installed on the east side of the bridge at H08E, H10E and H18E. [7, pp. 3-6]

Figure 25, Figure 26, Figure 27 and Figure 28 show the anemometers mounted to the bridge as of June 2022.

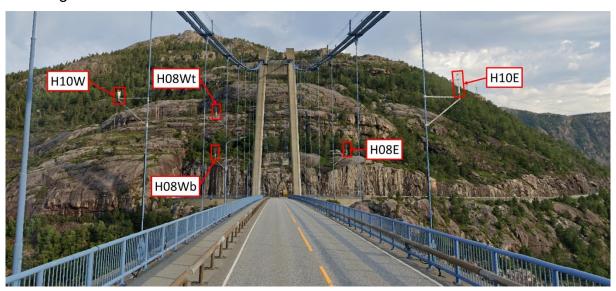


Figure 25: Location of anemometers H08Wb, H08Wt, H08E, H10W and H10E. Adapted from [4]



Figure 26: Location of anemometers H18W and H18W. Adapted from [25]





Figure 27: Location of anemometers H20W and H24W. Adapted from [26]



Figure 28: Location of anemometer H24W. Adapted from [27]

1.2.4 Data compilation

The sensors are connected to data acquisition units, which are connected to GPS receivers, providing an accurate timestamp to the data. The data, which is collected at a sample rate of 4 Hz, 32 Hz and 200 Hz by the weather station, anemometers and accelerometers respectively, is then resampled by a central data acquisition unit to 50 Hz. The central data acquisition unit outputs a single, synchronized, time-aligned dataset for every 10 minutes. This dataset is stored locally and simultaneously transferred to a server at University of Stavanger. [7, p. 7]

The 10-minute data packages of each day are compiled into a single MATLAB file. A MATLAB file for one day has an average file size of about 1.2 GB.



1.2.5 Data structure

Figure 29 illustrates the data structure of the compiled MATLAB files.

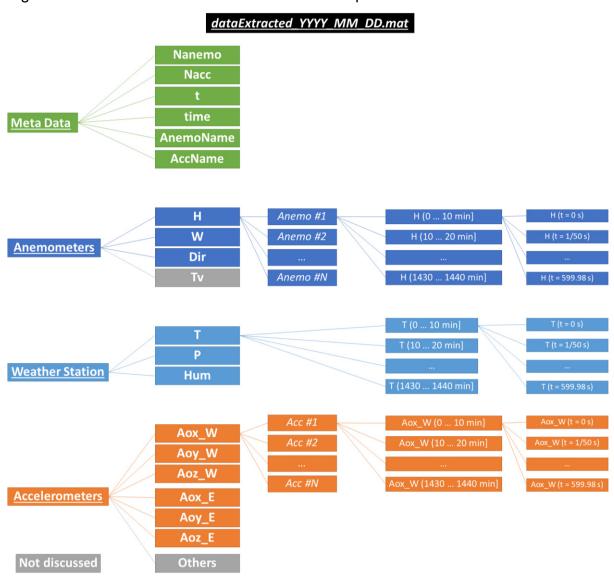


Figure 29: Data structure of MATLAB files.

The first level of the data structure can be grouped into meta data, data from anemometers, data from the weather station, data from accelerometers and data from other sources, which are not discussed in this thesis. The meta data includes information about the collected data such as timestamps as well as names of anemometers and accelerometers according to the naming convention illustrated in Figure 23. Measurements from anemometers include the horizontal wind component (H), the vertical wind component (W) and the direction from which the wind is blowing (Dir), as defined in 1.1.2 Wind definitions. Note that all wind measurements are in



reference to the bridge coordinate system, as the sensors are mounted on the bridge. The bridge coordinate system can move translationally and rotationally relative to the world coordinate system. The measurements from the weather station include the temperature (T), pressure (P) and humidity (Hum). The measurements from each accelerometer pair are split into measurements from the west side accelerometer (W) and east side accelerometer (E) and into acceleration data in x-, y- and z-direction (Aox, Aoy, Aoz) respectively. For measurements from anemometers and accelerometers the measurements are stored in an array, or matrix, in which the first axis, or dimension, splits the data into the measurements from the different anemometers or accelrometers. The name of each anemometer or accelerometer can be obtained from AnemoName or AnemoAcc respectively using the index of this first axis. Note that this is not applicable to the weather station, as there is only one sensor of that type installed on the bridge. The second axis splits the data from that sensor into the 10-minute data packages. The final axis represents a 10-minute-long time-series of measurements from the respective sensor, sampled at 50 Hz.



1.3 Background information

Some background information from the wind engineering theory and previous works on the Lysefjord Bridge is presented below. This background information is referred to in *4 Analysis using this works code*.

1.3.1 Eigenfrequencies and eigenmodes

Eigenfrequencies are also known as the natural frequencies of a structure, at which it resonates with an external loading and, if undamped, starts to vibrate with steadily increasing amplitude until the deformation of the structure surpasses its stress limits leading to material failure. The shape of the deformation along a structure, at each eigenfrequency, is characterised in terms of the associated. A structure can have multiple symmetric and asymmetric eigenmode shapes. The true deformation might be a combination of multiple modes. [28], [29]

The eigenfrequencies and eigenmodes of the Lysefjord Bridge have been identified from the ambient vibration data and compared to those estimated using different computational models by E. Cheynet in [20, pp. 116-127]



The eigenfrequencies identified from the data are depicted in Table 1.

Table 1: Eigenfrequencies identified from the data by E. Cheynet. Adapted from [20, p. 118]

| Mode | HS1 | HA1 | HS2 | HA2 | HS3 | HA3 | VA1 | VS1 | VS2 | VA2 | VS3 | VA3 | TS1 | TA1 |
|------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|
| Hz | 0.136 | 0.444 | 0.577 | 0.626 | 0.742 | 1.011 | 0.223 | 0.294 | 0.408 | 0.587 | 0.853 | 1.163 | 1.237 | 2.184 |

The first two symmetric and asymmetric eigenmode shapes for horizontal and vertical for horizontal and vertical vibrations, as well as the first symmetric and asymmetric eigenmode shape for torsional vibrations are depicted in Figure 30.

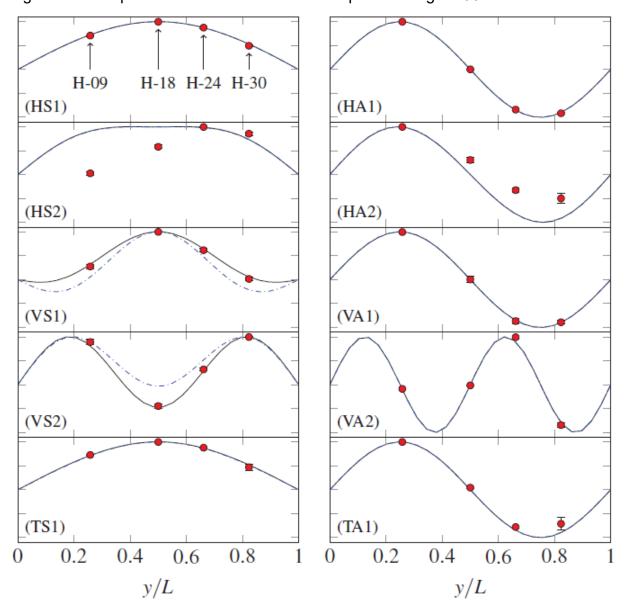


Figure 30: Identified eigenmode shapes from data (red dots) and models (lines). Adapted from [20, p. 126]



1.3.2 Wind load coefficients

The wind load coefficients for the drag (C_D) , lift (C_L) and moment (C_M) of the girder cross section have been determined at different AOAs in wind tunnel testing.

The load coefficients are calculated from the respective measured forces F_D , F_L and F_M on the bridge girder cross section using the equations below:

$$C_D = \frac{F_D}{\frac{1}{2}\rho U^2 h}$$

$$C_L = \frac{F_L}{\frac{1}{2}\rho U^2 b}$$

$$C_M = \frac{F_M}{\frac{1}{2}\rho U^2 b^2}$$

in which ρ is the air density, U is the mean wind speed, h is the height of the bridge girder and b is the width of the bridge girder. [30, pp. 4-10]



Figure 31 displays the results from the wind tunnel testing as the measured datapoints for the drag coefficient (blue circles), lift coefficient (orange stars) and moment coefficient (yellow square).

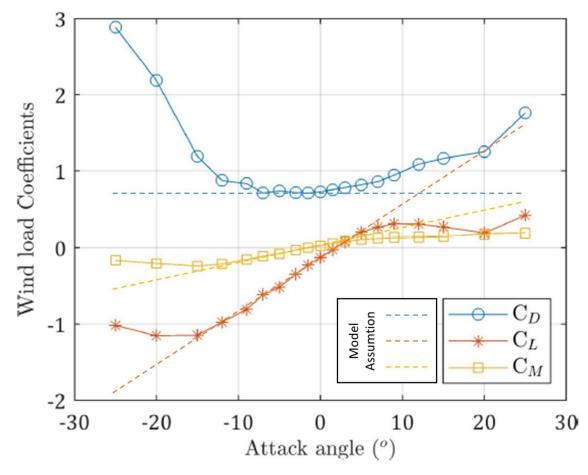


Figure 31: Wind load coefficients of the Lysefjord Bridge girder. Adapted from [30, p. 11]

In the so-called quasi-steady theory of wind loading and the corresponding numerical simulations a linear relation between AOA and the wind load coefficients, as illustrated in Figure 31, is assumed. The model assumption is illustrated by dashed lines, which are superimposed tangents at 0° AOA for the moment coefficient and lift coefficient and a horizontal line for the drag coefficient. Note that these are for illustrative purposes, the actual models might differ. While this linearity assumption is accurate enough at small AOAs, close to 0°, it leads to over- or underestimations in the wind response at higher positive or negative AOAs. From Figure 31 we see that the linearity assumption is accurate enough from about -15° to +5° for the lift coefficient, from about -12° to +5° for the moment coefficient and from about -8° to 0° for the drag coefficient.



1.3.3 Vortex shedding

Vortex shedding is a phenomenon in which the airflow detaches from both sides of a structure, with oppositely rotating vortices alternatingly shed from each side of the body, creating what is known as a Kármán vortex street, as depicted in Figure 32.

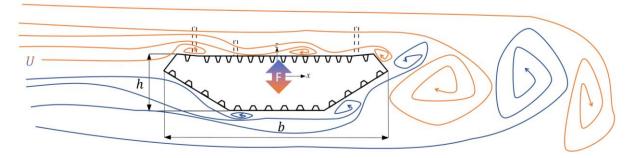


Figure 32: Illustration of vortex shedding at the bridge girder. Adapted from [7, p. 11]

These vortices create a harmonically varying force on the structure, primarily perpendicular to the wind direction with a distinct frequency of the vortex shedding. The shedding frequency f_S is

$$f_S = S_t \frac{U}{h}$$

Where U is the mean wind speed, h is the height of the bridge girder and S_t is the Strouhal number, which depends on the geometry of the structure and the Reynolds number. [2, pp. 59-60], [31, p. 5]

The Reynolds number, which captures the ratio between the inertia and the viscosity forces in the flow, has a smaller effect on the vortex shedding process for bodies with sharp edges, such as the girder of the Lysefjord Bridge. At a girder width to height ratio close to 4.5, which is the case at the Lysefjord Bridge, the Strouhal number can be assumed as 0.11. [2, p. 60], [32]

If the shedding frequency is close to one of the eigenfrequencies of the structure f_e this creates resonance, activating an eigenmode of the structure. The resonance wind velocity U_r is therefore

$$U_r = f_e \frac{h}{S_t}$$

[31, pp. 3, 5]



J. Tveiten has calculated critical wind velocities for vortex induced vibrations at 5.4 m/s, 7.6 m/s and 10.2 m/s, depending on the eigenmode, in [2, p. 61] Using the eigenfrequencies for vertical modes identified by E. Cheynet from Table 1 and the equation from above we can calculate the respective resonance wind velocities depicted in Table 2.

Table 2: Critical resonance wind velocities for vortex shedding. Adapted from [20, p. 118]

| Mode | VA1 | VS1 | VS2 | VA2 | VS3 | VA3 |
|-------------------------------|-------|-------|-------|-------|-------|-------|
| Eigenfrequency [Hz] | 0.223 | 0.294 | 0.408 | 0.587 | 0.853 | 1.163 |
| Resonance wind velocity [m/s] | 5.6 | 7.38 | 10.24 | 14.73 | 21.4 | 29.18 |



1.4 Motivation

The continues measurements since 2013 are now, almost 10 years later, equivalent to multiple terabytes of data. The data from the daily MATLAB files can be analysed directly in MATLAB, which has successfully been demonstrated in previous works in the department of Department of Mechanical and Structural Engineering and Materials Science at UiS in [20], [7] and [3]. However, the open-source programming language Python has become one of the most popular programming languages in recent years, as depicted in Figure 33.

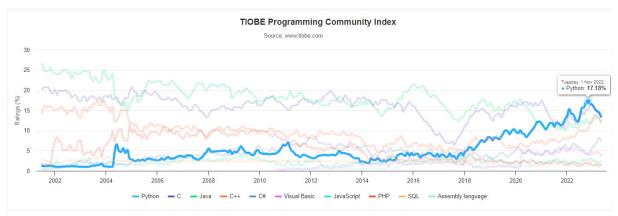


Figure 33: Popularity of different programming languages [33]

The open-source nature of Python and easy syntax provides opportunities to examine the data from a different perspective.

Research questions are related to the complex wind flow in the terrain surrounding the Lysefjord Bridge and the response of the bridge to the wind. Analysing datasets of multiple days in a consistent manner could help to answer these questions.



2 Method and design

The first goal of this work is to create a tool for detailed, consistent data analysis of multiple days of data from the Lysefjord Bridge using Python. The second goal is to demonstrate the code by using it to perform analysis on a dataset of a selected period, focusing on the local wind conditions at the Lysefjord Bridge and the bridge's response to different wind conditions.

2.1 Programming environment

Python has been chosen as the programming language for this work for its great readability and easy syntax allowing fast development of the code as well as open-source nature and extendibility, which are just a few reasons for its recent popularity. [34]

The code is written in a Jupyter Notebook, which allows to split the code into multiple code cells, have the output appear in an output cell right after each code cell and add markdown cells, as depicted in Figure 34.

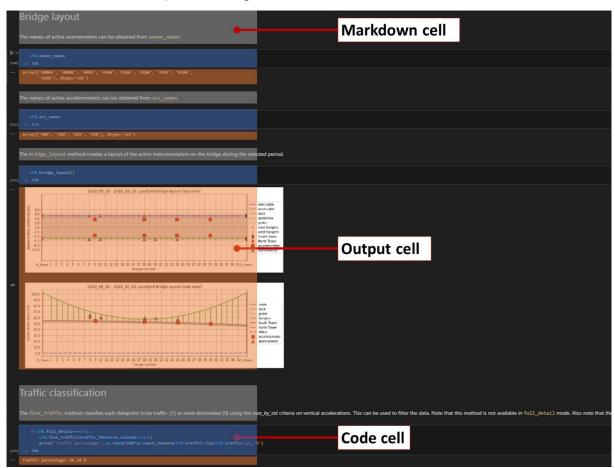


Figure 34: Structure of a Jupyter Notebook in VSCode with markdown-, code- and output-cells



The markdown cells can be used as explanatory text with formatting and as headings with different levels to group code cells together and give the notebook a structure.
[35]

The integrated development environment (IDE) used is Visual Studio Code (VSCode).

2.2 Programming paradigms: Functional and object-oriented programming

A combination of functional and class-based object-oriented programming is used.

"Functional programming decomposes a problem into a set of functions." [36]

Functions are defined to solve a type of problem, taking inputs, processing them and returning outputs. They can later be called to solve a specific problem, by giving them specific inputs so they return specific outputs.

"Object-oriented programs manipulate collections of objects. Objects have internal state and support methods that query or modify this internal state in some way." [36]

An object can be an instance of a class, giving it the internal structure of that class.

"Classes provide a means of bundling data and functionality together. Creating a new class creates a new type of object, allowing new instances of that type to be made. Each class instance can have attributes attached to it for maintaining its state. Class instances can also have methods (defined by its class) for modifying its state." [37]

A function inside a class is called a method of that class. Two different instances of a class have the same internal structure and methods of that class available but can have a different internal state.



In this work a class is defined to handle data from the Lysefjord Bridge of multiple dates. The functionality is contained in the methods of that class. An instance of that class is created with data from a given set of dates. The methods of the class are used to manipulate the internal state of that class instance, processing the data. This ensures that two different instances of the class, handling two different periods of data, have the same internal structure and the data can be processed in a consistent manner.

2.3 Data structures: NumPy array VS pandas dataframe

There is a powerful dedicated data analysis library for Python called pandas, which stores data in dataseries and dataframes. While pandas has a lot of inbuilt functionality for data analysis, it was deliberately decided to not use this library for this project. This is because this added functionality, such as explicit indexing, considerably slows down the data processing, compared to implicitly indexed NumPy arrays. It should be noted that this increased performance for NumPy arrays only holds up to datasets with about 50k columns, after which pandas performs better for some operations. On datasets of more than about 500k columns pandas outperforms Python on most operations. However, the bridge data in this work is by default downsampled to 144 samples per day by taking statistical metrics of each 10-minute data package. Therefore, analysing up to 1 year of data, equating roughly 50k rows, still benefits from the higher performance of NumPy arrays. Additionally, NumPy arrays consume less than half the memory of an equally sized pandas dataframe. [38], [39], [40]

This however means that special care had to be taken to keep the data in the different arrays aligned.

2.4 Coding style and documentation

The coding style and the documentation of the code is based on the Python Enhancement Proposal (PEP) "PEP 8 – Style Guide for Python Code" [41]. The docstrings for the class and its methods are based on "PEP 257 – Docstring Conventions" [42], the NumPy style guide [43] and the pandas docstring guide [44]. Some of the potential invalid inputs are directly handled by raising exceptions, informing the user of the corrective measures necessary.



2.5 Main class structure

In this work a class called *BridgeData*, containing most of the functionality in its methods, is defined. In the initialisation of an instance of that class parameters for the data, the design of the bridge and sensor ranges are defined. While the code is specifically tailored to the Lysefjord Bridge, this design allows it to be adapted to a different bridge where similar data might be collected.

The class is engineered in a modular design to allow for expendability. The methods for processing the data can be split into methods for pre-processing, processing and post-processing, as depicted in Figure 35.

```
BridgeData class definition
The BridgeData class defined below contains most of the functionallity of this work to load, process and analyze data from the Lysefjord Bridge.
              ***A class for processing wind and response data from a suspensionbridge, as in the case of the data collected at the Lysefjord Bridge by Universited def __init__(self,file_names,file_path = '../Data/Bridge/dataExtracted/',char_lim = 255, ...
                def convert_MATIAB(self,data,delete_data_after_import=True,ignore_nans=True,rename_H2B_acc=True,replace_invalid=True,full_detail=False,H=
               def define_units(self,accs_in_SI_units=True):
                       load_data(self,print_data_structure-False,delete_data_after_import=True,ignore_nans=True,rename_H20_acc=True,replace_invalid=True,full_detail=False,H-
                 def find_invalid_sensors(self,data,threshold-0.5,lp_cutoff-np.inf,hp_cutoff-np.inf,zeros-False,nans-True,lowpass-False,highpass-False)
               def find_common_ok_sensors(self,ok_sensor_ids_s1,ok_sensor_ids_s2):
                        idx data(self,data,mans=False,zeros=False,lp cutoff=mp.inf,hp cutoff=-mp.inf,lowpass=False,highpass=False):
                               n_data(self,delete_original_data=False,threshold=0.5,detailed_report=False):
               def get_ok_sensor_ind(self,sensor_names=[],sensor_type='anemo',key='H_mean'):
                       find_traffic(self,traffic_thresh=8,cleaned=True):
                def feature_time(self,cleaned=True):
               def filter_data(self,data,prior_idxs=None,nans=False,zeros=False,lp_cutoff=np.inf,hp_cutoff=-np.inf,lowpass=False,highpass=False,method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method='all',method
               scatterplot(self,data1,data2,data3,label1='data1',label2='data2',label3='data3',units=['[]','[]','[]',title_suffix='',color=True,plot_in_order_of_color
                                  ose(self,Dir,data,bridge_offset--42,label-'data',unit-'[]',title_suffix-'',bridge_morth-False,bins-[],mbins-6,cmap-'viridis',split se
                          ist2d(self,data1,data2,label1-'data1',label2-'data2',units-['[]','[]'],title_suffix-'',bins-(20,20),save-False):
               def boxplot(self,data,labels,ylabel='data',yunit='[]',title suffix='',save=False):-
                                          on matrix(self,data1,data2,labels data1=[],labels data2=[],title1='data1',title2='data2',title suffix='',save=False):
```

Figure 35: BridgeData class overview showing the different methods defined in the class.

The class-methods can be divided into secondary helper-methods and primary methods. Primary methods can either stand on their own or act as a wrapper-method that makes use of one or more helper-methods. Primary methods are designed to be called directly by the user. Secondary methods can technically also be called by the



user but might be less relevant. The methods are designed to be flexible, giving the user options in the analysis, while also providing a suitable default configuration.

In the following some of the methods for pre-processing, processing and post-processing are roughly described to illustrate the class structure and general workflow. Further details and explanations can be found in section 3 *Implementation*, in the code documentation, the docstrings for each method and the code itself, which can be found in the appendix.

2.5.1 Pre-processing

The pre-processing consists of the helper-methods convert_MATLAB and define_units as well as the wrapper-method load_data.

convert_MATLAB converts MATLAB data of a single day into NumPy arrays and dictionaries of NumPy arrays. By default, the data is down-sampled to 144 samples per day by taking the mean (_mean), standard deviation (_std), maximum (_max) and minimum (_min) of each 10-minute data package. Readings that are outside the sensors' ranges are by default replaced by Not a Number (NaN) and ignored in the down-sampling. Additional features such as AOA, AOI, turbulence intensity (_turb) as well as central acceleration (_C_) and torsional acceleration (theta_) are engineered from the measurements.

define_units defines the units of each measurement and by default converts the accelerometric data from μG to $\frac{m}{c^2}.$

load_data loads and combines data from one or multiple days using the previous helper-methods. This is the primary function that gets called by the user to pre-process data from a specific set of dates.

2.5.2 Processing

The processing consists of the helper-methods *find_invalid_sensors*, *remove_invalid_sensors*, *idx_data* and the wrapper-method *clean_data*. These methods are used for data cleaning. The data cleaning process can be divided into two steps. Firstly, sensors that have by default more than 50% invalid data are marked as invalid and removed from the cleaned dataset using *find_invalid_sensors* and *remove_invalid_sensors*. This threshold can be adjusted by the user. Invalid data can be NaNs, zeros or values above or below a certain threshold, depending on



the measurement type. Secondly, invalid data from the remaining sensors is indexed using *idx_data* and removed from the cleaned dataset. Note that if there is invalid data for a single measurement type from a single sensor, all readings from all other sensors are also marked as invalid and removed to keep the data aligned. Additional methods that are useful for the preparation of visualisations are *get_ok_sensor_ind*, *find common ok sensors*, *find traffic*, *feature time* and *filter data*.

get_ok_sensor_ind and find_common_ok_sensors are useful methods to select the right sensors for visualisations. feature_time creates time arrays in days, hours, minutes and seconds, starting at 0, for plotting of time-series data. filter_data allows sophisticated filtering of the data returning indices of the filtered data. It also allows combining the filter with indices of previously filtered data to apply multiple filters to the data at once.

For some analysis it is important to be able to separate wind induced vibrations of the bridge from traffic induced vibrations. Sophisticated methods for the identification of traffic induced vibrations are discussed in [24].

For this work a simple approach has been chosen, where the maximum vertical acceleration of each 10-minute data package is divided by the standard deviation of the vertical acceleration, resulting in the new measurement statistic <code>_max_by_std</code>. The vertical acceleration and wind speed data have been studied with <code>full_detail</code> set to <code>True</code>, as depicted in Figure 36 - Figure 43.



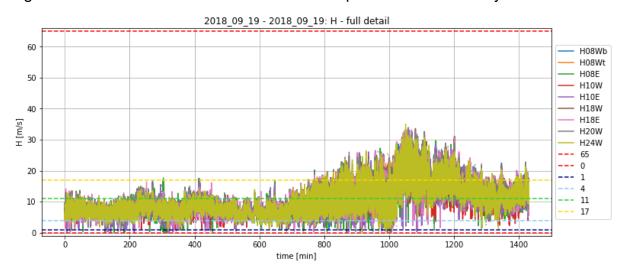


Figure 36: One day of full detail horizontal wind speed data



The data shows a horizontal wind speed mostly below 11 m/s in the first half of the day and reaching wind speeds above 17 m/s after about 13 hours or 780 minutes and mostly subsiding below 17 m/s at about 22 hours or 1320 minutes.

Figure 37 shows the central vertical acceleration data between minutes 600 and 610. Note that the naming error for accelerometer pair H24 mentioned in *1.2.3 Instrumentation Layout* might be carried over in some of the illustrations below. Any mentioning of H20 in reference to an accelerometer is to be interpreted as H24.

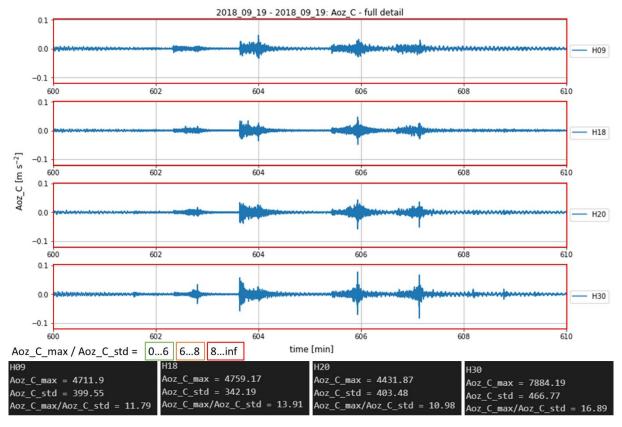


Figure 37: Full detail max_by_std criteria study (600min - 610min)

The respective calculation of maximum, standard deviation and the *max_by_std* criteria for each sensor in the given time period are below the plots and marked on each sensors plot according to the color code. The acceleration data shows four sharp patterns of clearly traffic induced vibrations at about 602.5 minutes, 603.5 minutes, 605.5 minutes and 607 minutes across all sensors. The *max_by_std* criteria is well above 8 across all sensors.



Figure 38 showcases that windspeeds were relatively low in the relevant period.

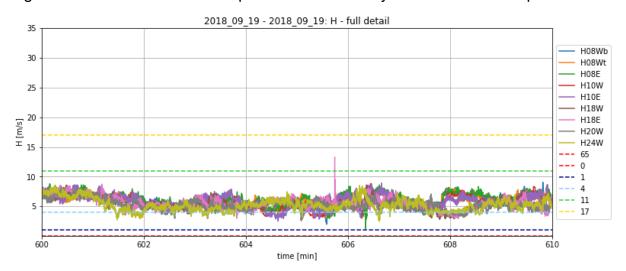


Figure 38: Full detail horizontal wind speed (600min - 610min)



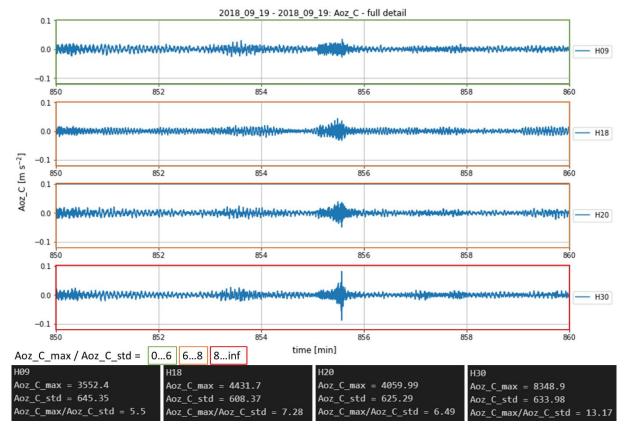


Figure 39 shows the acceleration data between minutes 850 and 860.

Figure 39: Full detail max_by_std criteria study (850min - 860min)

The acceleration data shows vibrations with higher amplitudes throughout the period, compared to the previous period, and a potential traffic induced vibration at about 855.5 minutes. The *max_by_std* criteria is below 6 at H09, between 6 and 8 at H18 and H24 and well above 8 at H30.

Figure 40 showcases that windspeeds are between 11 m/s and 17 m/s throughout most of the period and even peaking above 17 m/s around the time of the potential traffic induced vibration.



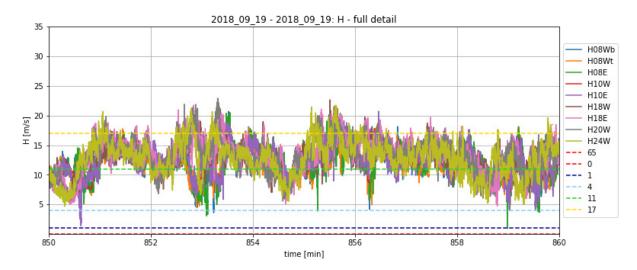


Figure 40: Full detail horizontal wind speed (850min - 860min)

This represents an edge case, where it is unclear if the vibrations in the period are traffic dominated or wind dominated.



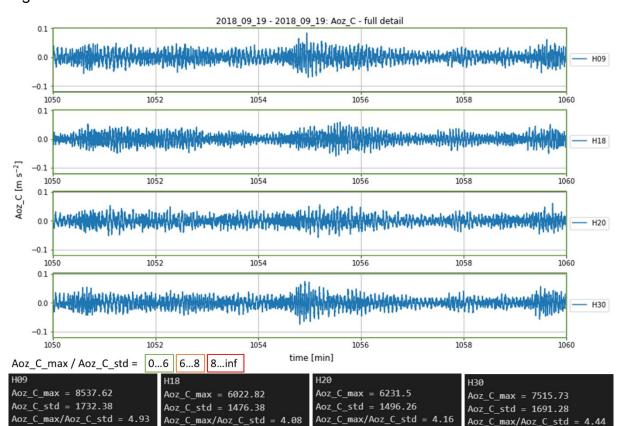


Figure 41 shows the acceleration data between minutes 1050 and 1060.

Figure 41: Full detail max_by_std criteria study (1050min - 1060min)

The acceleration data shows vibrations with even higher amplitudes throughout this period, compared to the previous periods. There is no clear sign of traffic induced vibrations. The max by std criteria is well below 6 across all sensors.



Figure 42 showcases that the wind speed is well above 17 m/s throughout most of the period.

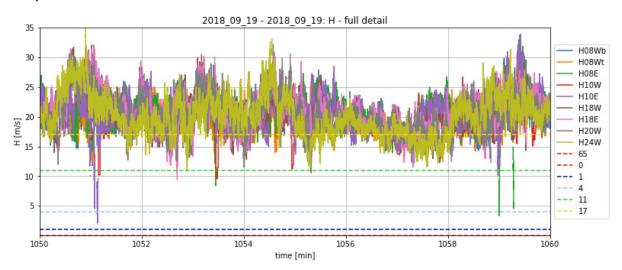


Figure 42: Full detail horizontal wind speed (1050min - 1060min)

This period is clearly a case of wind dominated vibrations.

Random 10-minute periods have been examined throughout the day in a similar way. A compilation of the results is showcased in Figure 43.

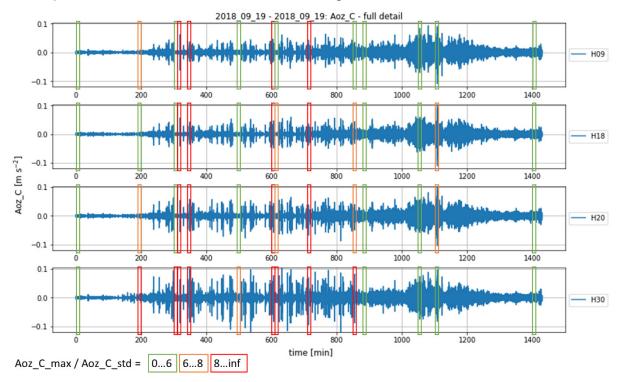


Figure 43: Full detail studies of central vertical acceleration with random samples of the max_by_std criteria

The sampled 10-minute periods are color-coded according to the respective result for the *max_by_std* criteria. These studies lead to the conclusion, that wind dominated



bridge responses have a vertical <code>max_by_std</code> value below 6 and traffic dominated bridge responses have a vertical <code>max_by_std</code> value above 8. <code>max_by_std</code> values between 6 and 8 are inconclusive edge cases, where the period can not be clearly classified as traffic dominated or wind dominated. The method <code>find_traffic</code> therefore uses a default lower threshold of 8 for the <code>max_by_std</code> criteria to find traffic dominated periods in the data, using the <code>idx_data</code> method. This threshold can be adjusted by the user.

2.5.3 Post-processing

bridge_layout creates an overview of the bridge illustrating the instrumentation layout for the chosen dates, as depicted in Figure 44 and Figure 45.

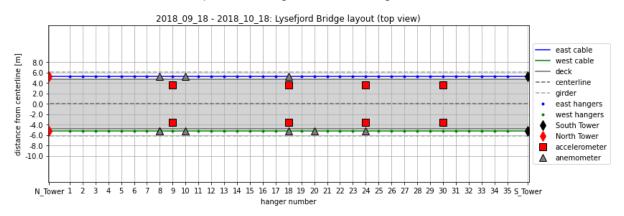


Figure 44: Lysefjord Bridge instrumentation layout from bridge_layout (top view)

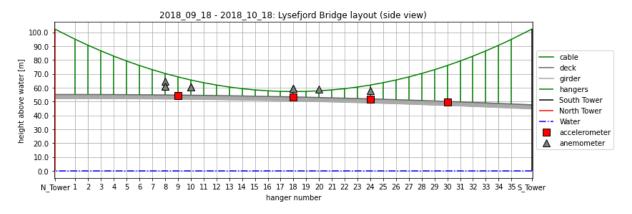


Figure 45: Lysefjord Bridge instrumentation layout from bridge_layout (side view)

Note that these layouts are for illustrative purposes only and not to be used as an engineering model.

The methods plot_data, hist, scatterplot, polar_scatterplot, windrose, hist2d, boxplot and correlation_matrix are designed similarly for a consistent visualisation of data from the Lysefjord Bridge. They take raw or processed data and create time-series



plots, histograms, scatterplots, polar scatterplots, wind roses, 2-dimensional histograms, boxplots or a heatmap of a correlation matrix respectively. In most of the methods it is possible to either display data for a measurement type combined from all sensors, or split it up, creating a visualisation per sensor. This allows comparisons of behaviours along the bridge span and on the upwind versus the downwind side of the bridge.



3 Implementation

The following Python libraries are used to implement the functionality of the class methods: *numpy* for mathematical operations and handling, transforming and shaping the data arrays, *scipy* to read MATLAB files and perform curve-fitting, *matplotlib* for most visualisations, *seaborn* for heatmaps of correlation matrices, *windrose* for wind roses and *gc* for garbage collection to free up memory.

3.1 Class methods

In this section the implementation of some of the class methods is explored and explained. To examine the full implementation of all methods, refer to the full documented code in the appendix.

3.1.1 convert MATLAB

Data outside the sensor range for anemometers and accelerometers, specified by anemo_range and acc_range, is by default considered invalid and replaced with NaN in the method convert_MATLAB, as depicted in Figure 46.

```
if replace_invalid:
    # Replace data out of technical range of sensors with nan.
    data['H'][(data['H']>self.anemo_range)|(data['H']<0)] = np.nan
    data['W'][(data['W']>self.anemo_range)|(data['W']<-self.anemo_range)] = np.nan
    data['Dir'] = np.where((data['Dir']>360)|(data['Dir']<0),np.nan,data['Dir'])

data['Aox_W'][(data['Aox_W']>self.acc_range*1e6)|(data['Aox_W']<-self.acc_range*1e6)] = np.nan
    data['Aoy_W'][(data['Aoy_W']>self.acc_range*1e6)|(data['Aoy_W']<-self.acc_range*1e6)] = np.nan
    data['Aox_E'][(data['Aox_E']>self.acc_range*1e6)|(data['Aox_E']<-self.acc_range*1e6)] = np.nan
    data['Aoy_E'][(data['Aoy_E']>self.acc_range*1e6)|(data['Aoy_E']<-self.acc_range*1e6)] = np.nan
    data['Aoz_E'][(data['Aoz_E']>self.acc_range*1e6)|(data['Aoz_E']<-(self.acc_range*1e6)] = np.nan
    data['Aoz_E'][(data['Aoz_E']>(self.acc_range+1)*1e6)|(data['Aoz_E']<-(self.acc_range-1)*1e6)] = np.nan</pre>
```

Figure 46: Code snippet of method convert_MATLAB, replace_invalid

Note that the *acc_range* is given in G and therefore needs to be converted to µG by multiplying with 1e6.

The data is by default then down sampled to 144 samples per day, unless *full_detail* is set to *True*. This is achieved by calculating the statistics mean, std, min and max for each 10-minute data package of each measurement. There are two methods implemented to calculate the statistics. By default *np.nanmean* is used to calculate the mean of a 10-minute data package, as depicted in Figure 47, which ignores NaNs.



```
if ignore_nans:
    # Use np.nanmean etc. instead of np.mean to ignore nans.
if H:
    anemo['H_mean'] = np.nanmean(data['H'],axis=2)
    anemo['H_std'] = np.nanstd(data['H'],axis=2)
    anemo['H_min'] = np.nanmin(data['H'],axis=2)
    anemo['H_max'] = np.nanmax(data['H'],axis=2)

if W:
    anemo['W_mean'] = np.nanmean(data['W'],axis=2)
    anemo['W_std'] = np.nanmin(data['W'],axis=2)
    anemo['W_min'] = np.nanmin(data['W'],axis=2)
    anemo['W_max'] = np.nanmax(data['W'],axis=2)
```

Figure 47: Code snippet of method convert_MATLAB, ignore_nans

Note that the calculations are performed along *axis* 2, meaning that they are performed for all sensors and all 10-minute data packages simultaneously, showcasing the strength of array operations using NumPy, compared to running a double for-loop over all sensors and all data packages for example.

Also note how the calculations for a given measurement, H or W for example, are only performed if the respective variable is set to True. While this is the default for all measurements, it allows the user to de-select measurements that are not relevant for their analysis to save memory and speed up the processing.

If *ignore_nans* is set to *False*, *np.mean* is used instead to calculate the mean of a 10-minute data package, which sets the value for that mean to NaN if there is at least one NaN value in the 10-minute data package. *np.nanstd*, *np.nanmin* and *np.nanmax* or *np.std*, *np.min* and *np.max* are used similarly.

The statistics for the direction cannot be calculated directly in the same manner, as for example taking the mean of 30° and 350° in that way would give a result of 190°, although the correct mean is 10°. This is due to the 360° - 0° discontinuity. To avoid this issue, the horizontal wind vector, defined by the horizontal wind component and direction, is de-composed into wind in x-direction and y-direction according to bridge coordinates, denoted vx and vy, using $v_x = -\sin(\mathrm{Dir}\cdot H)$ and $v_y = -\cos(\mathrm{Dir}\cdot H)$, as depicted in Figure 48.

```
# Decompose horizontal wind vector into vx and vy component
# according to the bridge coordinate system.
vx = -np.sin(np.deg2rad(data['Dir']))*data['H']
vy = -np.cos(np.deg2rad(data['Dir']))*data['H']
```

Figure 48: Code snippet of method convert_MATLAB, vector-decomposition



Note the minus sign at the front of the equation. This is to keep the orientation of vx and vy consistent with the definition in Figure 18. Also note that the direction in degrees has to be converted to radians for the trigonometric functions in NumPy using np.deg2rad.

The mean of *Vx* and *Vy* is calculated separately, as depicted in Figure 49.

```
if Vx or Dir or Upwind:
    anemo['Vx_mean'] = np.nanmean(vx,axis=2)
    anemo['Vx_std'] = np.nanstd(vx,axis=2)
    anemo['Vx_min'] = np.nanmin(vx,axis=2)
    anemo['Vx_max'] = np.nanmax(vx,axis=2)

if Vy or Dir or Upwind:
    anemo['Vy_mean'] = np.nanmean(vy,axis=2)
    anemo['Vy_std'] = np.nanstd(vy,axis=2)
    anemo['Vy_min'] = np.nanmin(vy,axis=2)
    anemo['Vy_max'] = np.nanmax(vy,axis=2)
```

Figure 49: Code snippet of method convert_MATLAB, Vx and Vy statistics

Note that these calculations are also performed if *Dir* or *Upwind* are selected, even if *Vx* or *Vy* are de-selected, as these measurements are dependent on the statistics of *Vx* and *Vy*.

From these mean wind vectors in x- and y- direction the actual mean-direction is calculated using the *np.arctan2* function and modulo operator (%), as depicted in Figure 50.

```
if Dir or Upwind:
    # Calculate mean of direction from Vx_mean and Vy_mean
    # instead of original data to deal with 360-0 discontinuity.
    anemo['Dir_mean'] = (np.rad2deg(np.arctan2(anemo['Vx_mean'],anemo['Vy_mean']))+180+360)%360
```

Figure 50: Code snippet of method convert_MATLAB, Dir_mean

Note that *np.arctan2* returns the arctangent, " [...] choosing the quadrant correctly [...] so that arctan2(x1, x2) is the signed angle in radians between the ray ending at the origin and passing through the point (1,0), and the ray ending at the origin and passing through the point (x2, x1)." [45] Note that this requires the first argument to be the y-coordinate and the second argument to be the x-coordinate. [45] By reversing the arguments, giving the x-coordinate to the first argument (x1) and the y-coordinate to the second argument (x2), we get the angle between the ray passing through the origin and the point (0,1) and the ray passing through the origin and the



point (y,x). Therefore 0° will be at the top of the wind rose, instead of at the East position.

np.rad2deg converts the radians back to degrees, giving a result of -180° to +180°. Adding 360° and applying the modulo operator, which returns the remainder of the division by 360°, converts the result to a range of 0° to 360°. Adding another 180° reverses the minus sign applied in the vector-decomposition and ensures the correct direction, from which the wind is blowing, is preserved.

The AOA is calculated using $AOA = tan^{-1}(\frac{W}{H})$, as depicted in Figure 51.

```
if AOA:
    anemo['AOA_mean'] = np.nanmean(np.rad2deg(np.arctan(data['W']/data['H'])),axis=2)
    anemo['AOA_std'] = np.nanstd(np.rad2deg(np.arctan(data['W']/data['H'])),axis=2)
    anemo['AOA_min'] = np.nanmin(np.rad2deg(np.arctan(data['W']/data['H'])),axis=2)
    anemo['AOA_max'] = np.nanmax(np.rad2deg(np.arctan(data['W']/data['H'])),axis=2)
```

Figure 51: Code snippet of method convert_MATLAB, AOA

The turbulence intensity (_turb) describing the relative wind variability for each wind component is calculated in this work by dividing the standard deviation of each component by the combined mean wind vector magnitude, as depicted in Figure 52.

Figure 52: Code snippet of method convert_MATLAB, turbulence intensity

The code for *H_turb* for example can be translated into the equation

$$H_{turb} = \frac{H_{std}}{\sqrt{H_{mean}^2 + W_{mean}^2}}$$

Note that the commonly used definition of turbulence intensity slightly differs from the way it is implemented in this work, considering the standard deviation along and across a mean wind vector, as described in [20, pp. 12-14].



The central accelerations Aox_C , Aoy_C and Aoz_C are calculated from the east- and west- accelerometer of each accelerometer pair using $C = \frac{W+E}{2}$, as depicted in Figure 53.

```
if centr:
    acc['Aox_C_mean'] = np.nanmean((data['Aox_W']+data['Aoy_E'])/2,axis=2)
    acc['Aox_C_std'] = np.nanstd((data['Aox_W']+data['Aox_E'])/2,axis=2)
    acc['Aox_C_min'] = np.nanmin((data['Aox_W']+data['Aox_E'])/2,axis=2)
    acc['Aox_C_max'] = np.nanmax((data['Aox_W']+data['Aox_E'])/2,axis=2)
    acc['Aox_C_max_by_std'] = acc['Aox_C_max']/acc['Aox_C_std']

acc['Aoy_C_mean'] = np.nanmean((data['Aoy_W']+data['Aoy_E'])/2,axis=2)
    acc['Aoy_C_std'] = np.nanmin((data['Aoy_W']+data['Aoy_E'])/2,axis=2)
    acc['Aoy_C_min'] = np.nanmin((data['Aoy_W']+data['Aoy_E'])/2,axis=2)
    acc['Aoy_C_max'] = np.nanmax((data['Aoy_W']+data['Aoy_E'])/2,axis=2)
    acc['Aoy_C_max_by_std'] = acc['Aoy_C_max']/acc['Aoy_C_std']
```

Figure 53: Code snippet of method convert_MATLAB, central acceleration

Note that for accelerometer data an additional statistic *_max_by_std* is calculated.

This quotient of _max and _std is later used to find bridge responses to traffic-dominated periods in the accelerometer data and separate it from responses to wind-dominated periods, as described in 2.5.2 Processing.

The torsional accelerations are calculated using $theta = tan^{-1}(\frac{W-E}{x_dist_from_centerline})$, as depicted in Figure 54.

```
if theta:
    acc['theta_mean'] = np.nanmean(np.rad2deg(np.arctan(((data['Aoz_W'] - data['Aoz_E'])*self.g*le-6/self.acc_x_dist_from_centerline))),axis=2)
    acc['theta_std'] = np.nanstd(np.rad2deg(np.arctan(((data['Aoz_W'] - data['Aoz_E'])*self.g*le-6/self.acc_x_dist_from_centerline))),axis=2)
    acc['theta_min'] = np.nanmin(np.rad2deg(np.arctan(((data['Aoz_W'] - data['Aoz_E'])*self.g*le-6/self.acc_x_dist_from_centerline))),axis=2)
    acc['theta_max'] = np.nanmax(np.rad2deg(np.arctan(((data['Aoz_W'] - data['Aoz_E'])*self.g*le-6/self.acc_x_dist_from_centerline))),axis=2)
    acc['theta_max_by_std'] = acc['theta_max']/acc['theta_std']
```

Figure 54: Code snippet of method convert_MATLAB, theta

Note that the original data is in μG and needs to be converted to $\frac{m}{s^2}$ by multiplying with self.g and 1e-6 to obtain $\frac{rad}{s^2}$, which is then converted to $\frac{\circ}{s^2}$ using np.rad2deg.



The names of the anemometers, saved in the *anemo_names* meta data, is used to determine if a sensor is up- or downwind for a given measurement, depending on the wind direction, as depicted in Figure 55.

Figure 55: Code snippet of method convert_MATLAB, Upwind

Similarly, the hanger number, y-position and information if an anemometer is on the West or East side of the bridge and if it is on the top or bottom row is determined from the anemometer name and encoded for each datapoint.

3.1.2 load data

Data for one or multiple days is loaded using the *load_data* method. This method first uses the *scipy.io.loadmat* function to load the MATLAB file for one day and then the convert_matlab method to pre-process it. This is repeated for further days in a for-loop as a form of batch-processing, as depicted in Figure 56.

```
# Batch-processing of further days of data, if any,
# with temporary variables being created for each day
# and deleted afterwards to free up memory for processing of the next day.
for day in range(1,len(self.file_names)):
    print('Day',day+1,':',self.file_names[day][:-4][14:])
    temp_data = scipy.io.loadmat(self.file_path+self.file_names[day])
    temp_anemo_names, temp_acc_names, temp_time_array, temp_tarray, temp_anemo, temp_acc, temp_weather = self.convert_MATLAB(
```

Figure 56: Code snippet of method load_data, for-loop

This is necessary because the MATLAB files loaded via *scipy.io.loadmat* take up a lot of memory.



Through the use of batch-processing, temporary data can be cleaned up using *del* and the garbage collector function *gc.collect()*, as depicted in Figure 57.

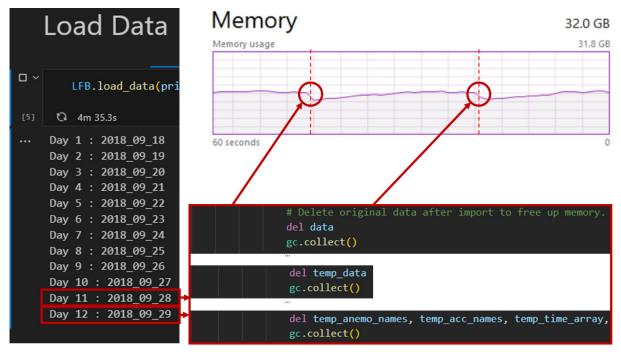


Figure 57: Memory usage during batch import

Figure 57 shows how the memory usage is reduced by using *batch-processing* to import the data. Each day of MATLAB data is processed sequentially in a *for-loop*. Temporary data variables are created for each day. These are deleted before moving on to the next step in the import pipeline, to free up memory for processing of the next day. This keeps the memory usage at a relatively constant level.

The temporary data arrays are stacked to the existing data arrays horizontally, as depicted in Figure 58.

```
for key in temp_anemo.keys():
    if key in self.anemo.keys():
        self.anemo[key] = np.hstack((self.anemo[key],temp_anemo[key]))
    else:
        self.anemo[key] = np.hstack((np.zeros_like(self.time_array),temp_anemo[key]))
```

Figure 58: Code snippet of method load data, horizontal stacking

If a measurement type was not available in previous days, the data from those days is engineered as zeros to keep all data synchronized.

After the batch-processing the method *define_units* is called to define the units of the loaded measurements and by default convert accelerations to $\frac{m}{c^2}$.



3.2 Quick start guide

In the following a quick start guide is provided on how to use the *BridgeData* class and its methods to import MATLAB bridge data, process it and visualize it. This only covers the basics and aims to encourage the user to explore how to perform more detailed analysis. It is encouraged to refer to the documentation for the class methods by using the *help(class.method)* function and explore the documented example code in the appendix as well as the example analysis performed in *4 Analysis using this works code*.

3.2.1 Data import

Firstly, an instance of the *BridgeData* class needs to be initialized. In the example below an instance called *LFB* is created:

```
file_path = '../Data/Bridge/dataExtracted/'
file_names = ['dataExtracted_2018_09_18.mat','dataExtracted_2018_09_19.mat']
LFB = BridgeData(file_names=file_names,file_path=file_path)
```

The *BridgeData* class requires a file path relative to the location of the notebook to where the MATLAB data is stored and a list of names for the files to import. Once the class instance is initialized as *LFB*, the MATLAB data can simply be loaded into the class instance with the code below:

LFB.load data()

Use the following line of code to access the documentation of *load_data* and find out more about the import options:

help(BridgeData.load_data)

Once the data is loaded, it can be processed and analysed.

3.2.2 Data processing

Use the line of code below to clean the data:

LFB.clean_data()

Note that the cleaned data is stored in class variables with the suffix *_cleaned*, such as *anemo_cleaned* and *acc_cleaned*.

The following line of code can be used to create time arrays for time series analysis:

LFB.feature_time(cleaned=False)

This creates the class variables *LFB.days*, *LFB.hours*, *LFB.minutes*, and *LFB.seconds*. Note that the keyword *cleaned* needs to be set to *True* or *False* accordingly, depending on which type of data is to be analysed with it.



The following line of code can be used to classify the data into data that is traffic- or wind-dominated:

LFB.find_traffic(traffic_thresh=8)

The *find_traffic* method uses a threshold *traffic_thresh* for the *max_by_std* criteria discussed in *2.5.2 Processing*. The classification is stored in the class variable *LFB.traffic*.

The *filter_data* method can be used to filter the data, as in the code below:

filter_idxs = LFB.filter_data(LFB.anemo['H_mean'], hp_cutoff=8, highpass=True)
Note that this only creates the indices *filter_idxs* of data applying to that filter, in this case mean horizontal wind speed measurements above 8 m/s. These filter indices need to be applied to the data in the visualisation to see the filter in effect. This can be done as showcased in the code below:

filtered data = LFB.anemo['H mean'].T[filter idxs].T

Note how the array of anemometer data needs to be transposed using the .T operation before applying the filter indices and transposed back to its original shape afterwards using another .T operation. This is also the case for accelerometer data, but not for weather data or time arrays created by LFB.feature_time, as they are of lower dimension.

3.2.3 Saving and loading the state of a class instance

A class instance with the name *LFB* can be saved in its current state, including imported and processed data, using the *dump* function of the *dill* module, as in the example below:

dill.dump(LFB,file=open('Your/File/Path/YourFileName','wb'))

Reversely, a previously saved class instance state can be loaded using *load* function as in the code below:

LFB = dill.load(open('Your/File/Path/YourFileName','rb'))

This is especially useful when you want to come back to the analysis of a larger dataset, where re-importing the data would take up considerable amounts of time.

3.2.4 Data analysis

As described in 2.5.3 Post-processing, there are multiple methods implemented for the analysis of the data. The code below shows a simple example to plot the time-series data on H_mean with days on the x-axis:



The visualisation methods are designed with a similar structure, sharing some of their functionality and the respective *keywords* to interact with them. To examine some more complex implementations of visualisations study the documented example code in the appendix. The visualisation methods of the *BridgeData* class are based on the default visualisation methods from the *matplotlib* library. However, they are optimized for a consistent visualisation of the bridge data. Nonetheless any of the standard methods from the *matplotlib* library or any other library can be used to visualise and analyse the data. This includes statistical analysis using the *numpy* and *scipy* libraries.

Tip: Should your Jupyter Notebook display graphical bugs upon opening, click *Clear All Outputs*, save it, close it and re-open it. Then run the code again from the top.



4 Analysis using this works code

In the following section 30 days of data are analysed using the developed code. The data is from 18th September 2018 until 18th October 2018. Further visualisations can be found in the code in the appendix.

4.1 Local wind conditions

This specific period has been chosen for its high maximum wind speeds at Sola observation station from data published for 2018 on Yr.no, as depoited in Figure 59.

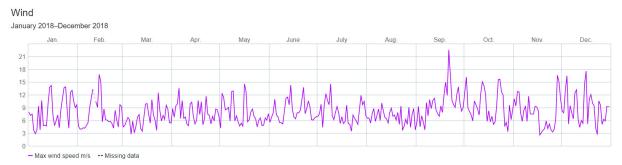


Figure 59: Maximum wind speeds at Sola observation station in 2018 [46]

The strongest gust of that year has been recorded at about 29.4 m/s on 21st September. [46]

4.1.1 Wind speeds and primary direction

Maximum wind speeds H_max have been gusting up to 35 m/s at the Lysefjord Bridge in this period, as depicted in Figure 60.

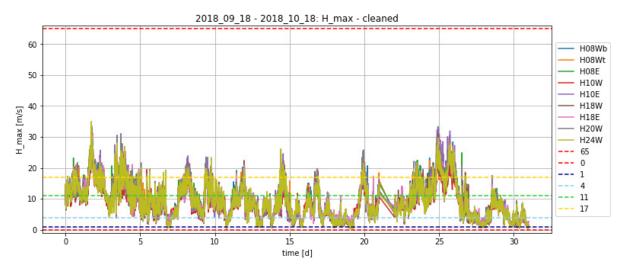


Figure 60: Maximum wind speeds per anemometer at Lysefjord Bridge during 30 days in autumn 2018

In the chosen period maximum wind speeds above 11 m/s have been recorded for multiple days at a time. Note that there is missing data on the 21st day of this period.



The primary wind directions at the Lysefjord Bridge during this period are NNE and SSW, as can be seen in the wind roses in Figure 61 and Figure 62.

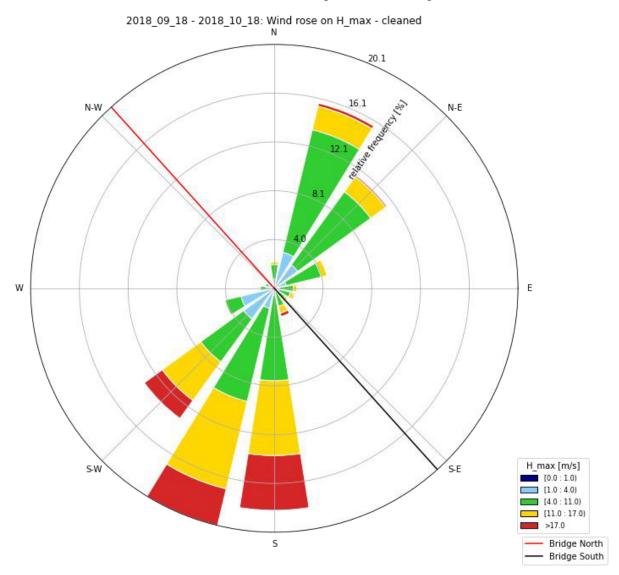


Figure 61: Combined wind rose on maximum wind speeds from all anemometers at Lysefjord Bridge during 30 days in autumn 2018

The two primary wind directions are from here on referred to as north-easterly (NE) wind for winds coming from anywhere NE of the bridge, meaning from -42° to 138° in geographic coordinates or 0° to 180° in bridge coordinates, and south-westerly (SW) wind for winds coming from anywhere SW of the bridge, the remaining half of the wind rose.



Note that the wind rose in Figure 62 displays the mean wind speeds *H_mean* of each 10-minute data package instead of the maximum wind speeds *H_max* displayed in Figure 60 and Figure 61. The mean wind speeds described the average wind condition while the maximum wind speeds describe the gusts.

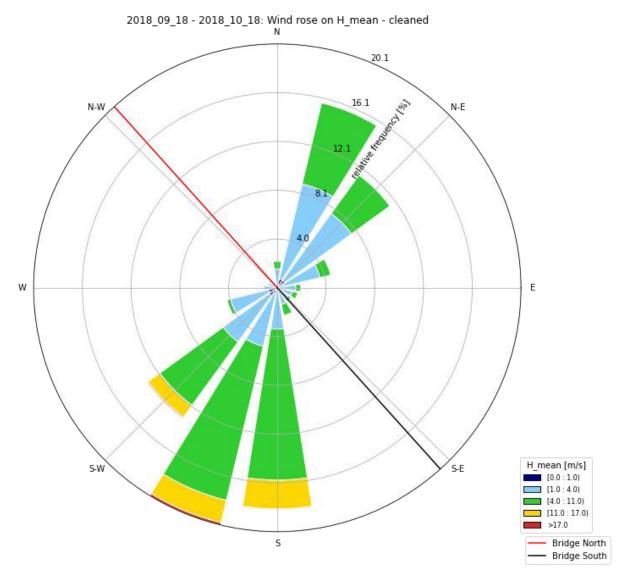


Figure 62: Combined wind rose on mean wind speeds from all anemometers at the Lysefjord Bridge during 30 days in autumn 2018

The wind roses in Figure 61 and Figure 62 show, that there are slightly stronger average winds and gusts from SSW compared to average winds and gusts from NNE. We see that there is a significant angle of incidence, or yaw angle, of up to about 48° for most winds from south-westerly direction and up to about 25° for most winds from north-easterly direction.



The histogram in Figure 63 is displaying the wind direction referring to bridge North, which is offset by -42° from geographic North.

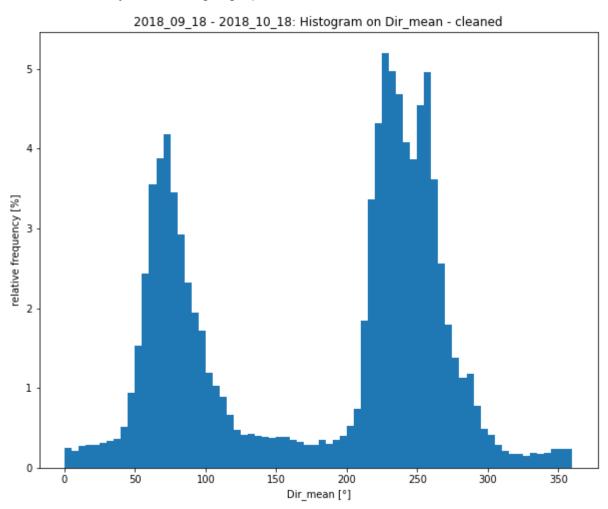


Figure 63: Histogram on mean wind direction

As expected, the histogram displays a bi-polar distribution. There is slightly more data with wind from SSW than wind from NNE in the 30 days period. The bins in Figure 63 have a width of 5°. When accounting for bins that make up more than 0.6% of the data, the wind from SSW is in the range of about 205° to 295° while the wind from NNE is in the range of about 45° to 120°. This gives the winds from SSW a broader bandwidth of about 90°, compared to the bandwidth of winds from NNE, which have a slightly narrower bandwidth of about 75°. This makes sense, as the wind is more confined by the walls of the fjord when coming from NNE, compared to the more open terrain when coming from the entrance to the fjord from SSW. Note that the distribution of wind from SSW is prominently bi-polar itself with one peak at about 225° to 230° and another at about 255° to 260°. There is also another small



peak at about 285° to 295°. This can be explained by the wind direction slightly changing along the span of the bridge, as depicted in Figure 64, which shows the wind rose for each anemometer, arranged by the anemometers position on the bridge. Note that the illustration is rotated 90 degrees counterclockwise with geographic North at the left of the page to increase readability. The bottom (right) row of wind roses is from anemometers on the west side of the bridge, ordered by hanger number with the windrose from H08Wt above (left to) the windrose from H08Wb and the top (left) row of wind roses is from anemometers on the east side of the bridge.



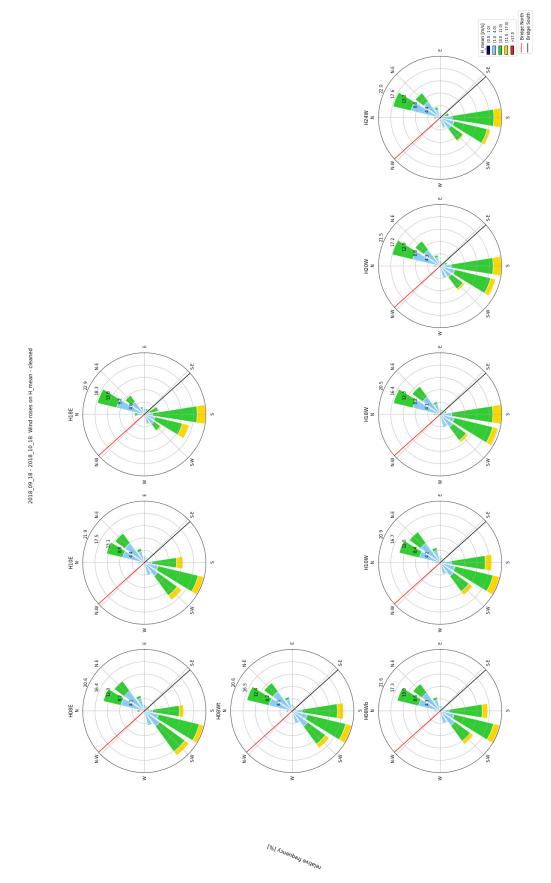


Figure 64: Wind roses on average wind speeds per anemometer, arranged by position on the bridge



For winds from SSW the wind tends to come more from the South for anemometers that are further down south on the bridge. Similarly, for winds from NNW the wind tends to come more from the North for anemometers that are further down south on the bridge.

The data can easily be split into south-westerly and north-easterly winds by applying a filter on the wind direction, as discribed in 3.2.4 Data analysis. This allows the comparison of wind conditions with south-westerly wind and north-easterly wind.

Figure 65 and Figure 66 show the respective histograms on average windspeeds for south-westerly and north-easterly wind.

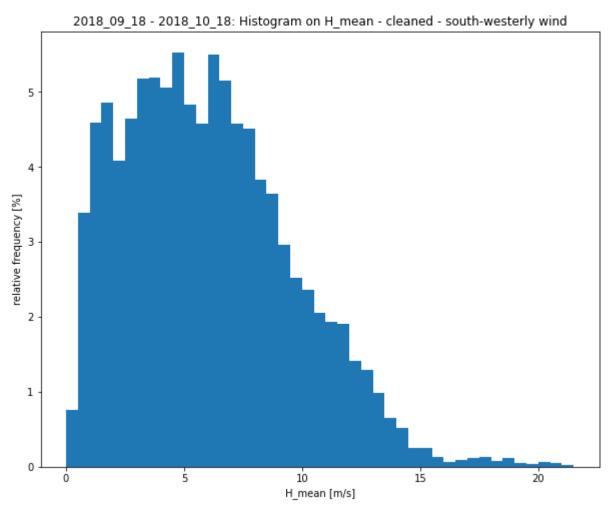


Figure 65: Histogram on average wind speeds for south-westerly wind



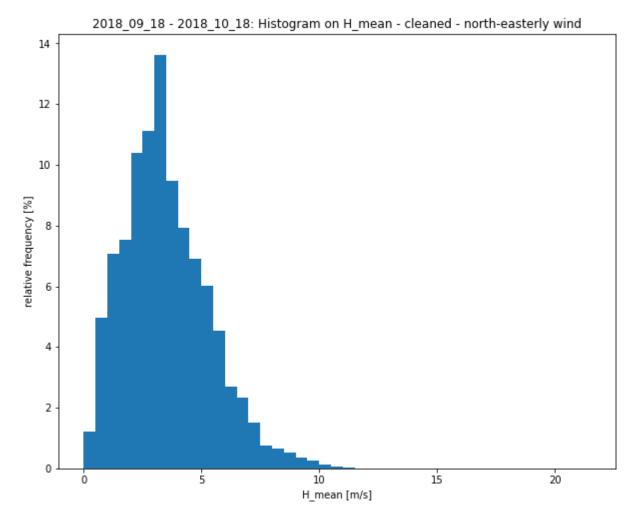


Figure 66: Histogram on average wind speeds for north-easterly wind

The histograms illustrate the different distributions of average wind speeds for south-westerly and north-easterly winds, with generally lower windspeeds from north-easterly directions. The distributions can be further examined using statistics on the filtered data.



Table 3 Compares the statistics on H_mean for the primary wind directions.

Table 3: Comparison of statistics on mean wind speeds for south-westerly wind and north-easterly wind

| Statistic on H_mean [m/s] | south-westerly wind | north-easterly wind |
|-----------------------------|------------------------|----------------------|
| Mean | 6.06 | 3.51 |
| Median | 5.72 | 3.28 |
| Percentile [10, 25, 75, 90] | [1.62 3.25 8.33 11.04] | [1.26 2.22 4.61 5.9] |
| Minimum | 0.18 | 0.22 |
| Maximum | 21.48 | 11.65 |
| Variance | 12.68 | 3.29 |
| Standard deviation | 3.56 | 1.81 |
| Skewness | 0.64 | 0.71 |
| Kurtosis | 0.21 | 0.54 |

The mean and median of mean wind speeds for south-westerly winds are about 2.5 m/s higher than for north-easterly winds. The highest mean windspeed for south-westerly winds are almost double those for north-easterly winds. The distribution for north-easterly mean wind is slightly more skewed towards lower wind speeds. While it has a lower standard deviation, it has slightly heavier tails.

Note that the applied kurtosis uses Fisher's definition, in which the normal distribution has a kurtosis of 0, a distribution with lower kurtosis has thinner tails and a distribution with higher kurtosis has heavier tails. [47]



4.1.2 Turbulence intensity

Similarly, the distribution of turbulence intensities can be examined and compared from the histograms in Figure 67 and Figure 68 as well as Table 4.

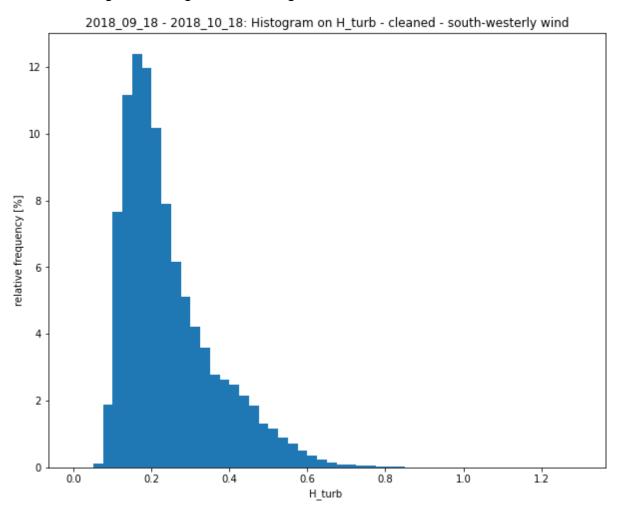


Figure 67: Histogram on horizontal turbulence intensity for south-westerly wind



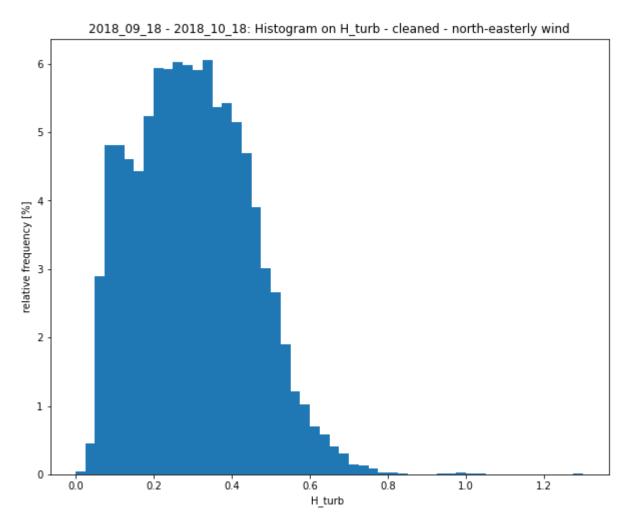


Figure 68: Histogram on horizontal turbulence intensity for north-westerly wind

Table 4: Comparison of statistics on horizontal turbulence intensity for south-westerly wind and north-easterly wind

| Statistic on H_turb | south-westerly wind | north-easterly wind |
|-----------------------------|----------------------|-----------------------|
| Mean | 0.25 | 0.3 |
| Median | 0.21 | 0.29 |
| Percentile [10, 25, 75, 90] | [0.13 0.16 0.3 0.42] | [0.11 0.19 0.41 0.49] |
| Minimum | 0.06 | 0.0 |
| Maximum | 0.98 | 1.29 |
| Variance | 0.01 | 0.02 |
| Standard deviation | 0.12 | 0.15 |
| Skewness | 1.29 | 0.42 |
| Kurtosis | 1.68 | 0.07 |



From the histograms in Figure 67 and Figure 68 as well as Table 4 we see that winds from north-easterly direction are slightly more turbulent. The distribution is less skewed towards lower turbulence intensities. While it has a higher standard deviation it has noticeably thinner tails.

When comparing the turbulence intensity measured by anemometers on the downwind side of the bridge to those on the upwind side, as in Table 5, we see that the turbulence intensity on the upwind side is on average slightly lower.

Table 5: Statistical comparison of turbulence intensity between upwind and downwind anemometers for south-westerly and north-easterly winds

| Statistic | south-westerly wind | | | north-easterly wind | | | | |
|-----------------|---------------------|-------|-------|---------------------|-------|-------|-------|-------|
| on H_turb | | | | | | | | |
| Anemometer | H08Wb | H08E | H18W | H18E | H08Wb | H08E | H18W | H18E |
| Up-/Downwind | U | D | U | D | D | U | D | U |
| Mean | 0.24 | 0.25 | 0.25 | 0.25 | 0.31 | 0.3 | 0.31 | 0.3 |
| Median | 0.2 | 0.22 | 0.21 | 0.22 | 0.31 | 0.29 | 0.3 | 0.29 |
| Percentile [10, | [0.12 | [0.13 | [0.12 | [0.13 | [0.11 | [0.11 | [0.11 | [0.12 |
| 25, | 0.15 | 0.16 | 0.16 | 0.16 | 0.2 | 0.18 | 0.2 | 0.19 |
| 75, | 0.3 | 0.31 | 0.31 | 0.3 | 0.42 | 0.4 | 0.41 | 0.4 |
| 90] | 0.42] | 0.43] | 0.42] | 0.41] | 0.51] | 0.48] | 0.5] | 0.49] |
| Minimum | 0.06 | 0.07 | 0.07 | 0.06 | 0.04 | 0.04 | 0.03 | 0.0 |
| Maximum | 0.89 | 0.95 | 0.84 | 0.98 | 1.03 | 0.98 | 1.0 | 1.02 |
| Variance | 0.01 | 0.01 | 0.01 | 0.01 | 0.02 | 0.02 | 0.02 | 0.02 |
| Standard | 0.12 | 0.12 | 0.12 | 0.11 | 0.15 | 0.14 | 0.15 | 0.15 |
| deviation | | | | | | | | |

For south-westerly winds all statistics on the turbulence intensity at the upwind anemometer H08Wb, except variance and standard deviation, are slightly lower than at the downwind anemometer H08E. At H18 the median, 10th percentile and maximum are slightly lower on the upwind anemometer H18W. The minimum and percentiles 75 and 90 are slightly higher.

For north-easterly winds all statistics on the turbulence intensity at the upwind anemometer H08E, except minimum, 10th percentile and variance, are slightly lower than at the downwind anemometer H08W. At H18 the mean, median, minimum, 25th, 75th and 90th percentiles are slightly lower on the upwind anemometer H18E. The 10th percentile and maximum are slightly higher.



It is also possible to plot the horizontal turbulence intensity on a wind rose, as depicted in Figure 69.

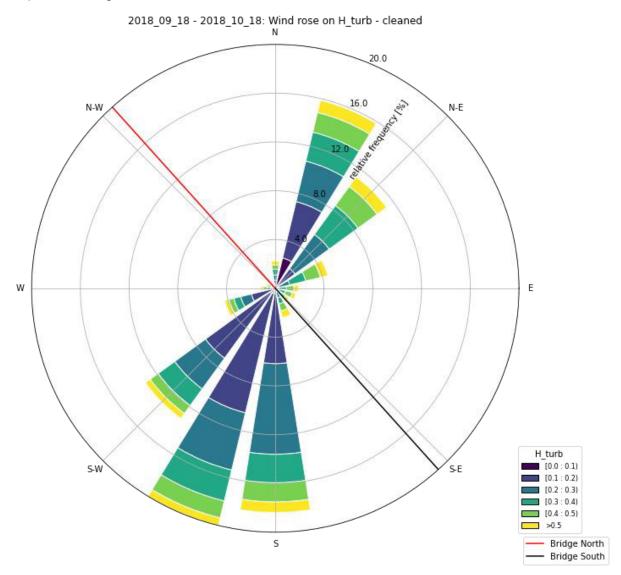


Figure 69: Wind rose on horizontal turbulence intensity, combined data from all anemometers

It is again also possible to split the wind rose into the different anemometers, as depicted in Figure 70, which allows a more detailed analysis of the turbulence distribution across the bridge.



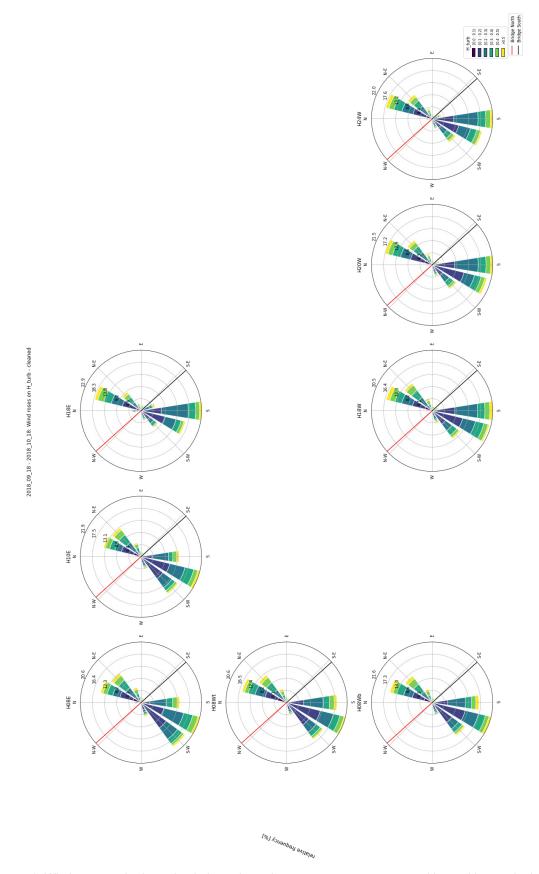


Figure 70: Wind roses on horizontal turbulence intensity per anemometer, arranged by position on the bridge



Figure 70 illustrates, how the turbulence intensity measured on the downwind anemometers is slightly higher for both winds from north-easterly and south-westerly direction. From their perspective the wind flow is disrupted by the upwind structures of the bridge, such as the cables, railings and bridge deck, as well as any traffic that might be on the bridge. We can also see that the top anemometer on H08W experiences slightly less turbulent winds compared to the bottom anemometer, as there is less influence on the wind flow by the bridge deck.

Figure 71 illustrates the horizontal and vertical turbulence intensity on the y-axis and color-axis respectively at different mean horizontal wind speeds on the x-axis.

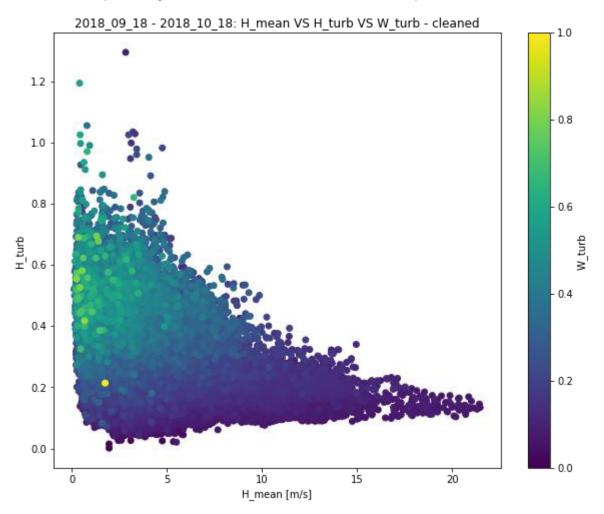


Figure 71: Horizontal and vertical turbulence intensity at different horizontal wind speeds

As expected, turbulence intensity decreases with higher wind speeds and is below 0.3 for wind speeds above 15 m/s. Vertical turbulence intensity increases with horizontal turbulence intensity up to about 0.5 after which the vertical component decreases as the horizontal component increases.



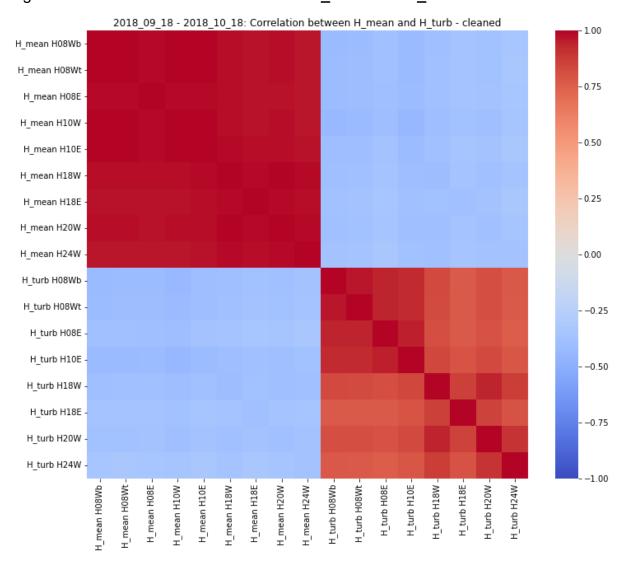


Figure 72 shows the correlations between *H_mean* and *H_turb* across all sensors.

Figure 72: Correlation matrix between horizontal mean wind speed and turbulence intensity per anemometer

From Figure 72 we see that the measurements of mean horizontal wind speed are very well correlated between the anemometers, displayed as a homogeneous dark red coloring in the upper-left quadrant of the correlation matrix heatmap, corresponding to a high positive correlation coefficient close to 1. In the lower right quadrant, we see that the turbulence intensity is slightly less correlated across the anemometers. However, note that there is a higher correlation between the anemometers at hangers H08 to H10. There is also a slightly lower correlation between the anemometers at hangers H18 to H24, however it is still slightly higher compared to their correlation to the previous group of anemometers. The correlation coefficient between H_mean and H_turb is negative across all anemometers at



about -0.4, colored in light blue in the top right and bottom left quadrants. This means that with higher wind speeds turbulence intensity decreases, as expected.

4.1.3 Angle of attack

Figure 73 shows a wind rose on the mean angle of attack, created from the combined data of all anemometers during the 30-day period. Warmer colors represent positive angles of attack while colder colors represent negative angles of attack, as previously illustrated in Figure 19.

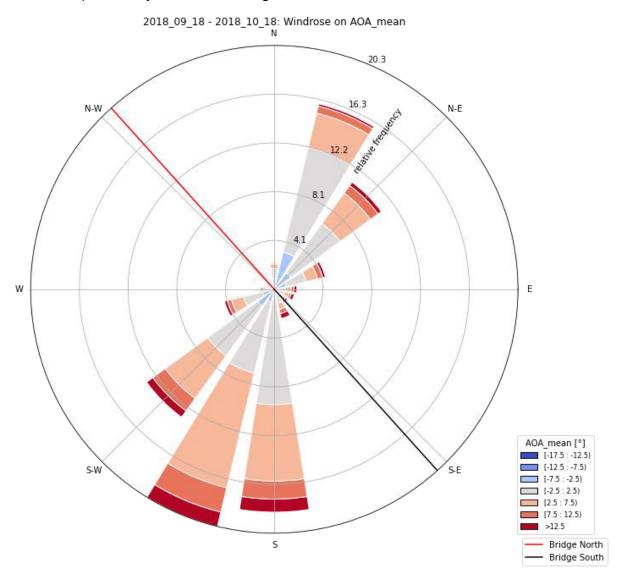


Figure 73: Mean angle of attack wind rose combined from all anemometers

Note how while a good portion of the data displays relatively neutral AOAs there is a tendency to more positive AOAs for winds from SSW and more negative AOAs from NNE. This can also be seen when comparing the histograms on AOA from



north-easterly and south-westerly winds in Figure 74 and Figure 75 as well as Table 6.

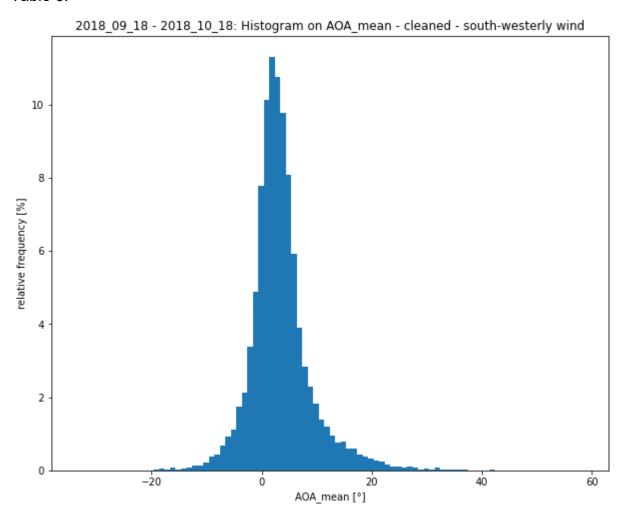


Figure 74: Histogram on mean angle of attack for south-westerly wind

Figure 74 clearly shows the tendency to positive AOAs in the distribution for south-westerly winds.



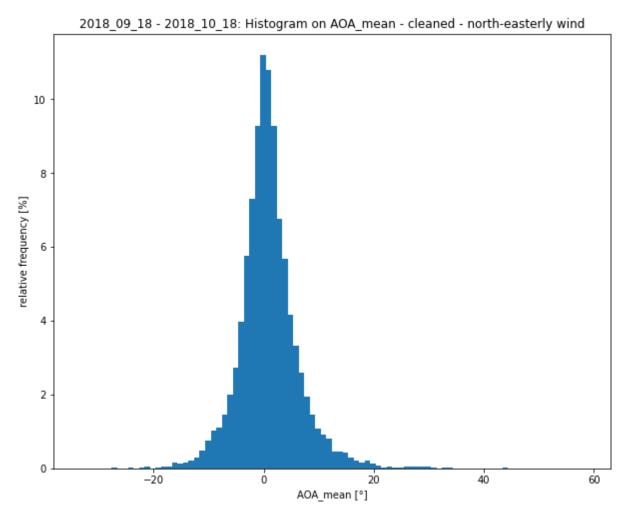


Figure 75: Histogram on mean angle of attack for north-easterly wind

Figure 75 shows a distribution centred around 0° for north-easterly winds.

Table 6: Comparison of statistics on mean angle of attack for south-westerly wind and north-easterly wind

| Statistic on AOA_mean [°] | south-westerly wind | north-easterly wind |
|-----------------------------|------------------------|-------------------------|
| Mean | 3.41 | 0.86 |
| Median | 2.76 | 0.53 |
| Percentile [10, 25, 75, 90] | [-2.05 0.44 5.46 9.73] | [-4.85 -1.99 3.34 7.03] |
| Minimum | -21.9 | -33.11 |
| Maximum | 53.22 | 45.93 |
| Variance | 31.51 | 29.7 |
| Standard deviation | 5.61 | 5.45 |
| Skewness | 1.23 | 0.73 |
| Kurtosis | 5.24 | 4.86 |



As can be seen in Figure 74 and Figure 75 as well as Table 6, both distributions have a similar standard deviation of about 5.5°. South-westerly winds have a slightly positive mean and median angle of attack at about 3.4° and 2.8°, while AOAs of north-easterly winds have a mean and median at about 0.9° and 0.5°. The 10th percentile is about -2° and -5° respectively. The 90th percentile is about 10° and 7° respectively. Therefore 80% of the data is inside a 12° bandwidth for both south-westerly and north-easterly winds. We see that more than 80% of the data is inside the range of -15° to +15°, the critical AOAs at which an aerofoil, such as the wing of an aircraft, would typically experience stall conditions. [48]

However, the wind flow around a bridge girder, as illustrated in Figure 32, is not as laminar and attached as the wind flow around a wing and subjected to vortex shedding, as discussed in 1.3.3 Vortex shedding.

As we have seen in Figure 31, the lift coefficient has a local maximum at about +10° AOA and minimum at about -18°. From Figure 31 we also see that the linearity assumption is accurate enough from about -15° to +5° for the lift coefficient, from about -12° to +5° for the moment coefficient and from about -8° to 0° for the drag coefficient, as discussed in 1.3.2 Wind load coefficients.

From the histograms in Figure 74 and Figure 75 and statistics in Table 6 we see that a considerable amount of data is outside these ranges, especially for positive AOAs and wind from south-westerly direction, where about 25% of the data showcases AOAs over +5° and about 75% of the data showcase AOAs over 0°. This suggests that while the linearity assumption is accurate enough for negative AOAs most of the time, it creates an overestimation of lift and moment coefficients 25% of the time and underestimation of drag coefficients 75% of the time for winds from south-westerly direction.



Figure 76 shows that the mean AOA gets closer to 0° at higher wind speeds, with most of the data between 0° and $+8^{\circ}$ for wind speeds above 15 m/s.

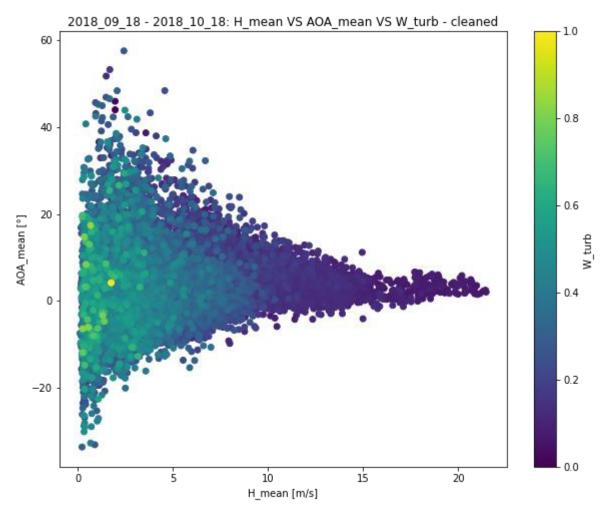


Figure 76: Mean angle of attack and vertical turbulence intensity at different wind speeds

The vertical turbulence intensity, which also decreases with higher wind speeds, is below 0.5 for wind speeds above 10 m/s.



When comparing the mean angle of attack measured by anemometers on the downwind side of the bridge to those on the upwind side, as in Table 5, we see that the mean AOA gets straightened towards 0° as the wind flow passes over the bridge.

Table 7: Statistical comparison of mean angle of attack between upwind and downwind anemometers for southwesterly and north-easterly winds

| Statistic on | south-westerly wind | | | north-easterly wind | | | | |
|-----------------|---------------------|--------|--------|---------------------|--------|--------|--------|--------|
| AOA_mean | | | | | | | | |
| Anemometer | H08Wb | H08E | H18W | H18E | H08Wb | H08E | H18W | H18E |
| Up-/Downwind | U | D | U | D | D | U | D | U |
| Mean | 4.2 | 2.18 | 5.47 | 3.3 | -0.42 | 2.41 | 0.39 | 2.41 |
| Median | 4.13 | 1.75 | 4.5 | 1.18 | -0.09 | 2.36 | 0.22 | 2.3 |
| Percentile [10, | [-1.29 | [-3.35 | [0.51 | [-3.54 | [-4.95 | [-5.48 | [-4.11 | [-5.12 |
| 25, | 2.15 | -0.39 | 2.27 | -0.73 | -2.32 | -2.15 | -1.63 | -0.84 |
| 75, | 6.08 | 4.02 | 7.21 | 5.37 | 1.73 | 6.54 | 2.04 | 5.62 |
| 90] | 8.93] | 8.75] | 12.02] | 15.46] | 3.62] | 10.84] | 4.6] | 9.67] |
| Minimum | -17.55 | -21.04 | -17.74 | -21.9 | -17.86 | -27.67 | -25.3 | -33.11 |
| Maximum | 35.22 | 30.51 | 39.49 | 53.22 | 26.1 | 40.72 | 36.82 | 45.93 |
| Variance | 23.56 | 26.74 | 30.28 | 64.0 | 13.94 | 47.37 | 22.95 | 45.89 |
| Standard | 4.85 | 5.17 | 5.5 | 8.0 | 3.73 | 6.88 | 4.79 | 6.77 |
| deviation | | | | | | | | |

For south-westerly winds all statistics on the mean AOA at the downwind anemometer H08E, except 10th percentile, variance and standard deviation, are lower than at the upwind anemometer H08Wb. At H18 all statistics except 90th percentile, maximum, variance and standard deviation are lower on the downwind anemometer H18E.

For north-easterly winds all statistics on the mean AOA at the downwind anemometer H08Wb, except minimum and 25th percentile, are lower than at the upwind anemometer H08E. At H18 all statistics are lower on the downwind anemometer H18W. Note how the variance increases on the downwind side for south-westerly winds but decreases for north-easterly winds.

Comparing the AOA wind roses for H08E and H08Wb in Figure 77 illustrates how more extreme positive AOAs (orange-red) on the upwind side become more neutral (grey-orange) on the downwind side, as the wind follows the shape of the bridge girder. At H18E an anomaly to this occurs, showing a large population of high positive AOAs (red) from direct south to east.



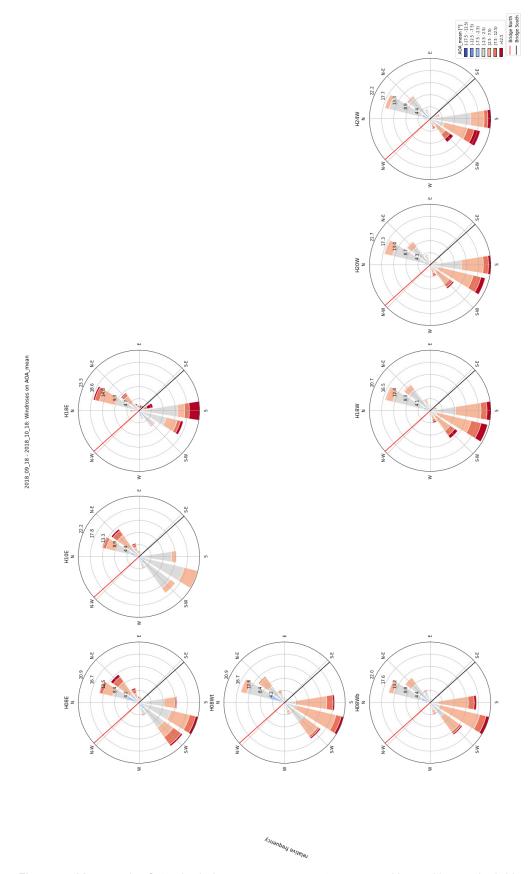


Figure 77: Mean angle of attack wind roses per anemometer, arranged by position on the bridge



This anomaly can be further examined using the polar scatterplots depicted in Figure 78. Note that the datapoints with the highest values on the color-axis, AOA_mean, are plotted on top of datapoints with lower mean angles of attack. Therefore, datapoints with negative AOAs are not very visible in this kind of plot, as they are hidden below datapoints with high AOAs. However, for a closer examination of the before mentioned anomaly at H18E the datapoints with extreme high mean AOAs of +15° or higher (dark red) are of interest. There is a large population of these datapoints in the sector between 0° and 225° with wind speeds mostly below 5 m/s in the sector between 0° and 90° and reaching 10 m/s in the sector between 90° and 225°. It should be noted that we can also observe a population of high AOA datapoints in the sector between 180° and 225° with wind speeds reaching 10 m/s at H08E, but not at H10E. There is also a smaller population of high AOA datapoints in the sector between 0° and 90° with wind speeds below 5 m/s at both H08E and H10E. However, there is no population of high AOA datapoints in the sector between 135° and 180° at both H08E and H10E.



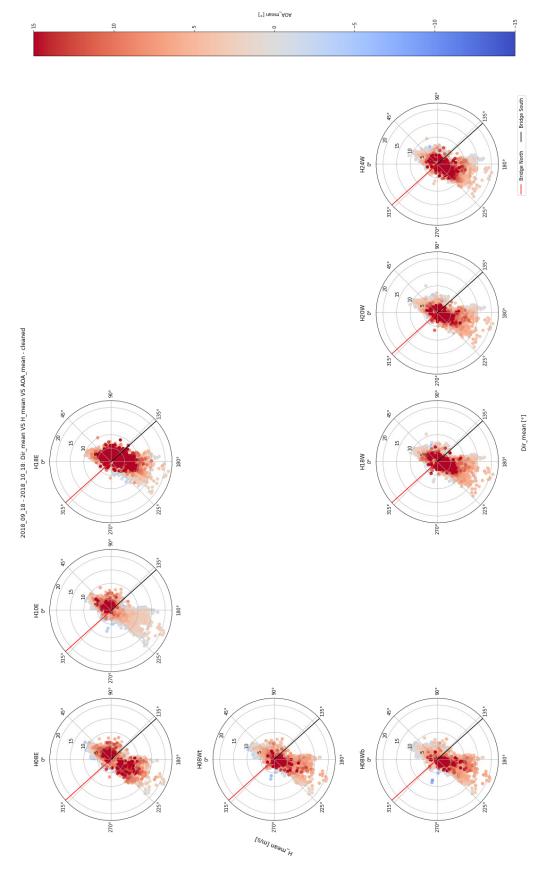


Figure 78: Polar scatterplots on mean angle of attack and horizontal wind speed per anemometer, arranged by position on the bridge



The reasons for this anomaly cannot be explained from this analysis. A miss-alignment of the sensor has been ruled out by a recent examination of the sensor. The scatterplot in Figure 79 does not suggest that the high AOAs in these sectors are caused by un-organized turbulent flow, as the vertical turbulence intensity is mostly below 0.4 in the region of interest at H18E.



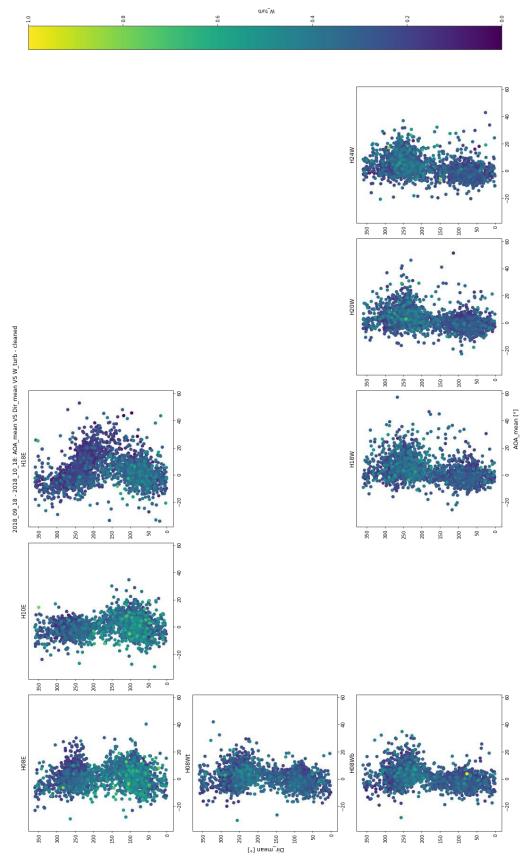


Figure 79: Scatterplots on mean angle of attack and vertical turbulence intensity from different directions per anemometer, arranged by position on the bridge



The author therefore hypothesizes, that the narrow cross-section of the fjord at the point where the bridge crosses the fjord acts as a bottleneck for the wind flow into and out of the fjord, which creates an updraft and re-circulation region just east of the bridge, which gets captured by the anemometer at H18E, but not the other anemometers. Figure 80 and Figure 81 illustrate how such a flow could look like for north-easterly wind.

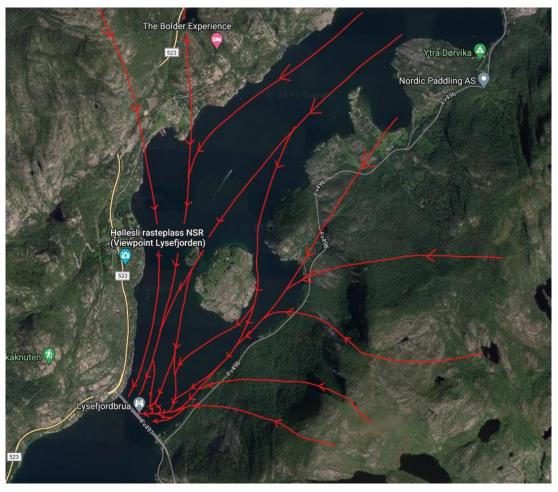


Figure 80: Hypothesis on wind flow causing high angles of attack at H18E from east direction, top view. Adapted from [49]



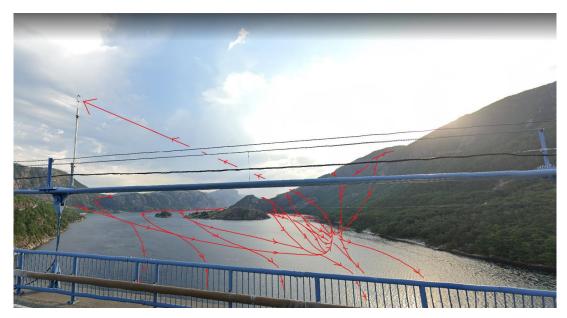


Figure 81: Hypothesis on windflow causing high angles of attack at H18E from east direction, view from the West.

Adapted from [50]

Note that the high AOAs from the sector between 135° to 180° are not well explained by this hypothesis, as the wind flow must cross the bridge or come from the direction of the south tower. Another hypothesis is that a downdraft from the hills southeast of the bridge hits the bridge deck and is reflected upwards through the anemometer at H18E. Additional anemometers at H20E and H24E could help in examining this anomaly. Another approach could be a CFD simulation similar to [18], to examine the origin of this anomaly.



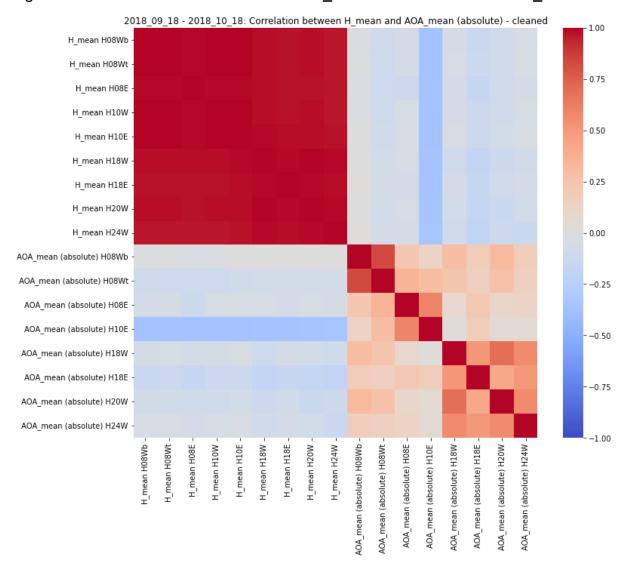


Figure 82 shows the correlations between *H mean* and the absolute *AOA mean*.

Figure 82: Correlation matrix between mean horizontal wind speed and absolute mean angle of attack per anemometer

From Figure 82 we see that the absolute mean AOA is not correlated very much across the anemometers. The absolute mean AOA at H08Wb and H08t are correlated relatively well with a correlation coefficient of about 0.8. However, their correlation to H08E across the bridge deck is relatively low at about 0.25, which is not significantly higher than the correlation to the other anemometers along the span of the bridge. Similar observations can be made for the other anemometers. The correlation to anemometers on the same side of the bridge is slightly higher, compared to the correlation to anemometers across the bridge deck. For anemometers on the same side of the bridge deck the further away another



anemometer is, the lower their correlation. The correlation to *H_mean* is slightly negative, mostly between -0.25 and 0, except for H10E, where it is about -0.5. Figure 83 shows the correlation between absolute *AOA_mean* and *H_turb*.

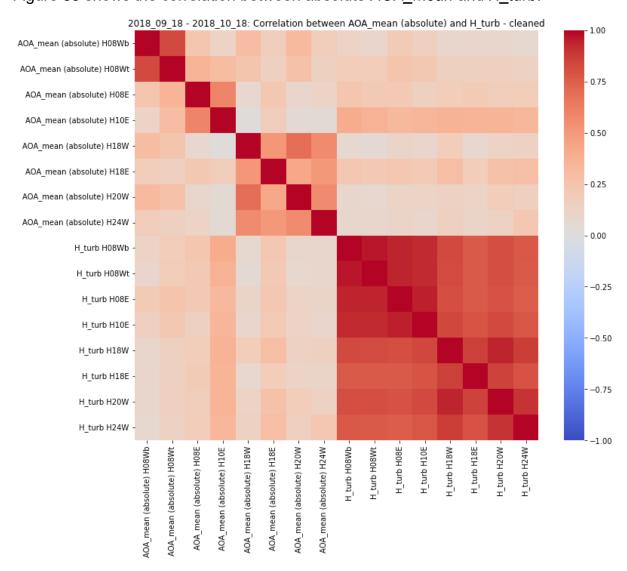


Figure 83: Correlation matrix between absolute mean angle of attack and horizontal turbulence intensity per anemometer

From Figure 83 we see that the correlation between absolute mean AOA and horizontal turbulence intensity is relatively low, but slightly positive between 0 and 0.25 for most anemometers, except for H10E again, where the correlation is slightly higher at about 0.35. Note that correlation does not imply causation and therefore it is not possible to explain this anomaly from these correlation matrices.



4.2 Bridge response

In the following the code of this work is used to examine the response of the bridge to traffic and wind.

4.2.1 Traffic response

Note that the naming error for accelerometer pair H24 mentioned in *1.2.3 Instrumentation Layout* might be carried over in some of the illustrations below. Any mentioning of H20 in reference to an accelerometer is to be interpreted as H24.

Figure 84 shows the maximum vertical acceleration for each 10-minute data package at the centreline of the bridge over the month-long period of recorded data.

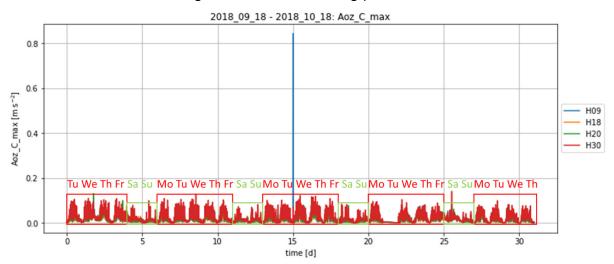


Figure 84: Maximum central vertical accelerations measured at the Lysefjord bridge during 30-day period showing periodic response to traffic

A clear periodic behaviour is visible with a period of one day. This is because more traffic is crossing the bridge during the day than at night. Another clear observation is that after five days of higher maximum accelerations two days of lower maximum accelerations follow. This can respectively be linked to workdays, during which heavy trucks from the Norsk Spennbetong AS concrete plant or NCC Helle sandtak sand pit cross the bridge, and weekend days, during which the traffic primarily consists of lighter cars. As expected by this hypothesis, the first day of data, 18th September 2018, is a Tuesday while the last day, 18th October 2018, is a Thursday. Note that there is an outlier at exactly 15 days at H09, caused by the east accelerometer, which has not been recognised as invalid as it is still inside the operational limits of the accelerometer of ±5g. [23]



4.2.2 Lateral wind response

In Figure 85 to Figure 92 the lateral wind response of the bridge, measured by the standard deviation of acceleration in x-direction Aox_C_std is visualised and analysed.

Figure 85 shows a scatterplot of *Aox_C_std* over the mean horizontal wind component perpendicular to the primary bridge axis *Vx_mean* with the respective turbulence intensity *Vx_turb* on the color-axis.

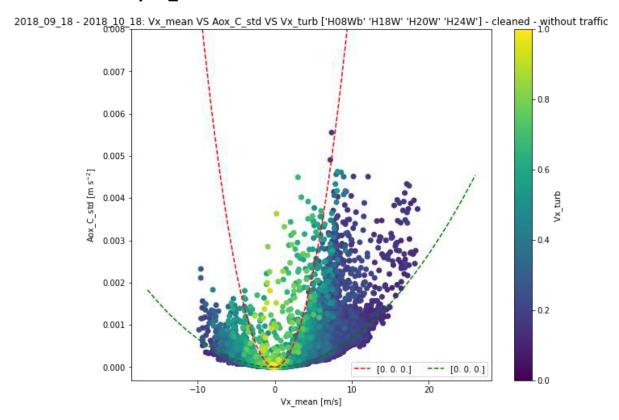


Figure 85: Lateral bridge response and turbulence intensity at different mean wind speeds

Note that positive Vx corresponds to wind from south-westerly direction and a negative Vx to wind from north-easterly direction, matching the bridge coordinate system in Figure 24. A red parabola through the origin is matched to datapoints with $Vx_turb > 0.6$ and a green parabola through the origin is matched to datapoints with $Vx_turb < 0.1$. These parabolas create an envelope into which most of the datapoints fall. Note how higher standard deviations in the accelerations up to about 0.005 m/s^2 can occur even at mean wind speeds below 10 m/s, especially under higher turbulence intensity above 0.5.



By normalizing the standard deviation of acceleration by the turbulence intensity we try to reduce the factor of turbulence intensity, expecting to fold the data in on itself. Figure 86 and Figure 87 showcase this for south-westerly and north-easterly wind conditions respectively, split across the accelerometer pairs at H09, H18, H24 and H30. The wind measurements in these plots are taken from the respective downwind anemometer at midspan H18.

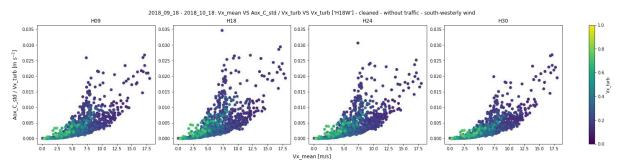


Figure 86: Lateral bridge response normalized by turbulence intensity and turbulence intensity at different mean wind speeds for south-westerly winds per accelerometer pair

As expected, the data is folded in on itself and bound by an upper and lower parabola shape. However, there is still a spread occurring with higher wind speeds.

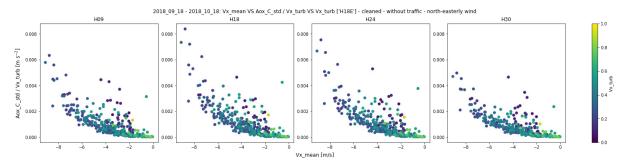


Figure 87: Lateral bridge response normalized by turbulence intensity and turbulence intensity at different mean wind speeds for north-easterly winds per accelerometer pair

Similar observations are to be made for the north-easterly winds, although the distribution of datapoints is more chaotic, especially at wind speeds between -2 m/s and -5 m/s. We can assume that this is due to other effects the terrain has on the wind flow from that direction, especially on the vertical wind component, like the anomaly at H18E discussed in *4.1.3 Angle of attack*.



Figure 88 shows the lateral bridge response at different mean AOAs with the mean horizontal wind speed decoded on the color-axis.

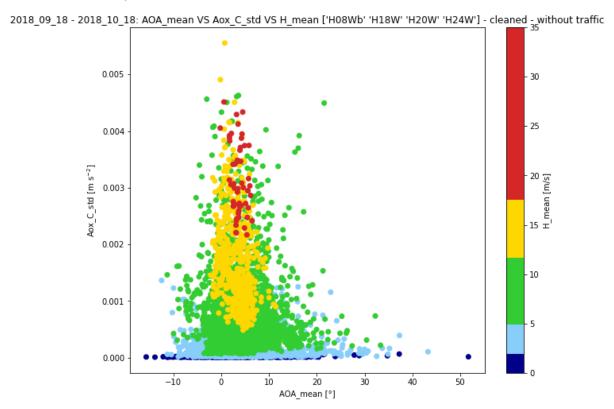


Figure 88: Lateral bridge response and mean wind speed at different angles of attack

From Figure 88 we again see that larger lateral responses above 0.002 m/s² can be observed even at wind speeds below 11 m/s at AOAs between -5° to +20°. Wind speeds above 11 m/s occur only in a relatively narrow AOA band between -1° and +10°. As discussed in 1.3.2 Wind load coefficients and showcased in Figure 31, the linearity assumption for the drag coefficient is accurate at about -8° to 0°. We see that most of the datapoints at wind speeds above 4 m/s causing large lateral responses are above 0°. This suggests that the linearity assumption for the drag coefficient is not suitable to predict large lateral responses, as they mostly occur at higher AOAs, even at lower wind speeds, where the linearity assumption underestimates the lateral wind response.



Normalizing the lateral bridge response by turbulence intensity again results in Figure 89.

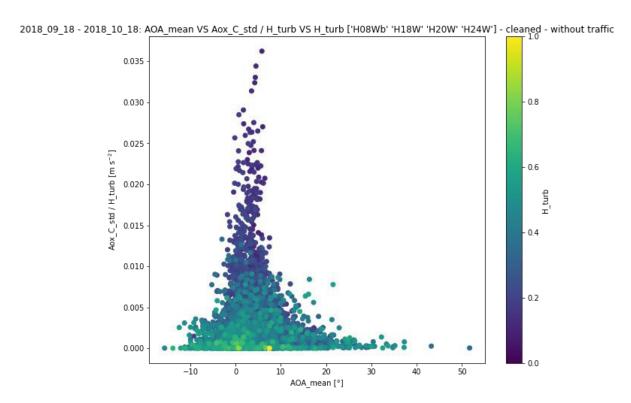


Figure 89: Lateral bridge response normalized by turbulence intensity and turbulence intensity at different angles of attack

We see that some of the higher bridge responses at lower mean wind speeds and at angles of attack further out from 0° are brought down in the normalized scatterplot, as they were more correlated with higher turbulence intensity.



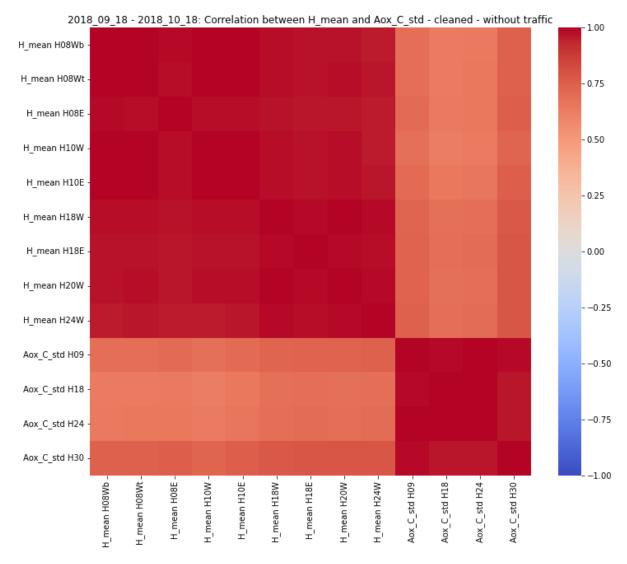


Figure 90 shows the correlation between *H_mean* and *Aox_C_std*.

Figure 90: Correlation between mean wind speed and lateral bridge response per anemometer and accelerometer

From Figure 90 we see that the correlation coefficient between the accelerometers on the lateral response is close to 1, displayed as homogeneous dark red color in the lower right quadrant. The correlation between accelerometers H18 and H24 is slightly higher compared to the correlations with and between the other accelerometers, as they are located closer together. The correlation to the mean horizontal wind velocity is also relatively high at about 0.5 to 0.75. Counterintuitively the correlation of lateral response at midspan H18 and H24 to mean horizontal wind velocity is slightly lower compared to the lateral response measured by accelerometers at H09 and H30 closer to the towers. This suggests that the lateral response at the midspan of the bridge, where the main cables are at the lowest point and the hanger length is the



shortest, is less sensitive to higher wind speeds, compared to further out towards the towers. However, this does not account for other factors on the lateral response, explaining how an eigenmode shape like the first and second symmetric horizontal eigenmode shapes *HS1* and *HS2* identified by E. Cheynet in [20, p. 126] which are depicted in Figure 30, can occur. Also note that the data might be a combination of symmetric and asymmetric eigenmode shapes. In the later the acceleration at midspan is close to zero and higher at H09 and H30.

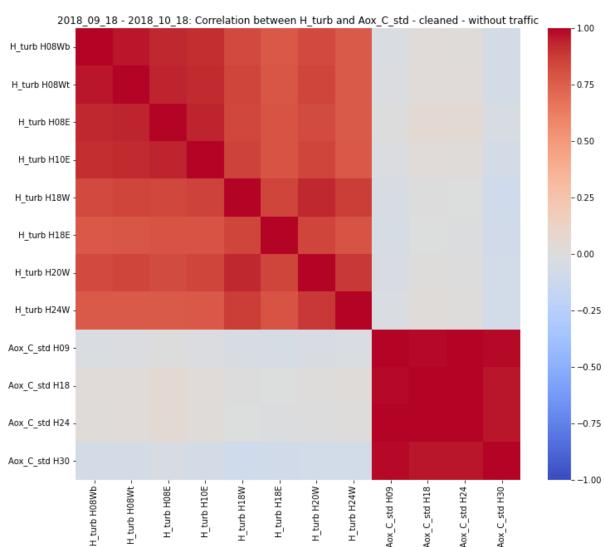


Figure 91 shows the correlation between *H_turb* and *Aox_C_std*.

Figure 91: Correlation turbulence intensity and lateral bridge response per anemometer and accelerometer

From Figure 91 we see that the correlation between the lateral response and horizontal turbulence intensity is close to 0, slightly negative at H09 and H30. No significant assumption can be drawn from these correlations.



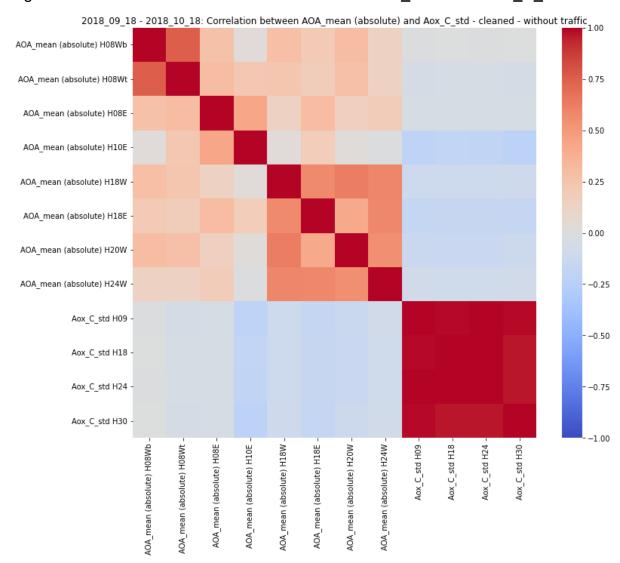


Figure 92 shows the correlation between absolute AOA_mean and Aox_C_std.

Figure 92: Correlation between absolute mean angle of attack and lateral bridge response per anemometer and accelerometer

From Figure 92 we see that the correlation between the lateral response and absolute mean AOA is close to 0, or slightly negative for anemometers at H10E, H18E and H20W, but below 0.25. This coincides with the anomaly detected in Figure 82 and discussed in *4.1.3 Angle of attack*. No further significant assumptions can be drawn from these correlations.



4.2.3 Vertical wind response

In Figure 93 to Figure 101 the vertical wind response of the bridge, measured by the standard deviation of acceleration in z-direction Aoz_C_std is visualised, analysed and compared to the lateral wind response discussed in 4.2.2 Lateral wind response. Figure 85 shows a scatterplot of Aoz_C_std over the mean horizontal wind component perpendicular to the primary bridge axis Vx_mean with the respective turbulence intensity Vx_turb on the color-axis, similar to Figure 85.

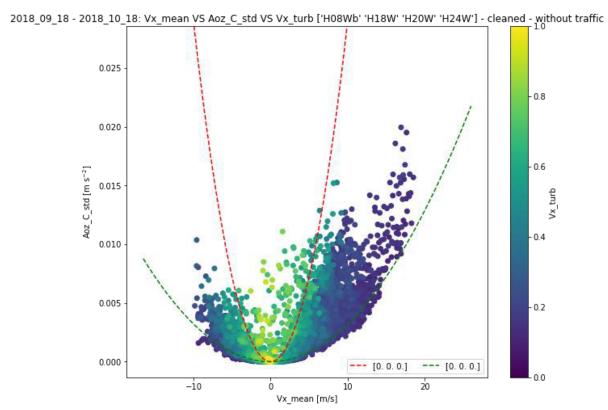


Figure 93: Vertical bridge response and turbulence intensity at different mean wind speeds

The highest standard deviation of vertical acceleration is measured at about 0.02 m/s² at a perpendicular wind speed of about 18 m/s and low turbulence intensity. This is about 3.5 to 4 times higher than the highest measured standard deviation of lateral acceleration. At about 8 m/s Aoz_C_std is measured at about 0.015 m/s² at a turbulence intensity of about 0.6. At about 2 m/s Aoz_C_std is measured at about 0.011 m/s² at a turbulence intensity of about 0.8.



Figure 94 and Figure 95 showcase *Aoz_C_std / Vx_turb* for south-westerly and north-easterly wind conditions respectively, split across the accelerometer pairs at H09, H18, H24 and H30, similar to Figure 86 and Figure 87.

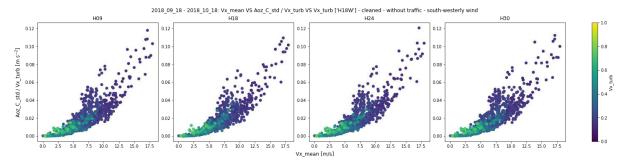


Figure 94: Vertical bridge response normalized by turbulence intensity and turbulence intensity at different mean wind speeds for south-westerly winds per accelerometer pair

As expected, the data is folded in on itself and bound by an upper and lower parabola shape. The remaining spread occurring with higher wind speeds is less than for the lateral response in Figure 86. The higher vertical response we are seeing between about 7 m/s and 12 m/s could be explained by vortex shedding, as described in 1.3.3 Vortex shedding.

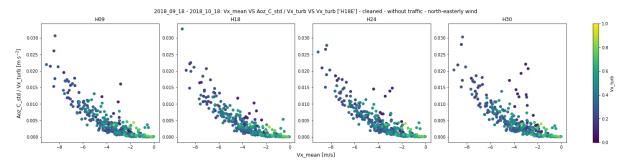


Figure 95: Vertical bridge response normalized by turbulence intensity and turbulence intensity at different mean wind speeds for north-easterly winds per accelerometer pair

As in the case for lateral response in Figure 87, similar observations are again to be made for the north-easterly winds for the vertical response. The distribution of datapoints is again more chaotic, at wind speeds between -2 m/s and -5 m/s, especially towards the south of the bridge at H30.



Figure 96 shows the vertical bridge response at different mean AOAs with the mean horizontal wind speed decoded on the color-axis, similar to Figure 88.

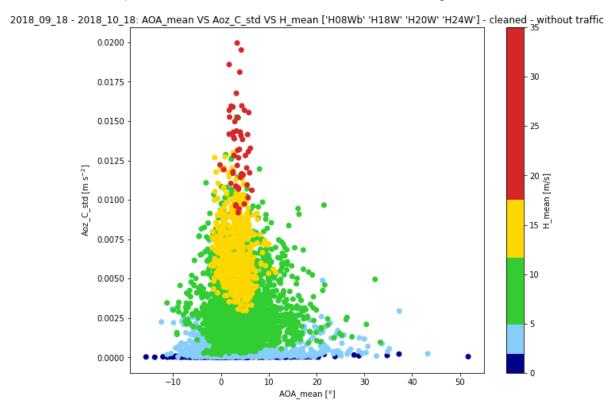


Figure 96: Vertical bridge response and mean wind speed at different angles of attack

From Figure 96 we see that larger vertical responses above 0.0125 m/s² and up to about 0.02 m/s² can be observed primarily at wind speeds above 17 m/s at AOAs between +1° to +8°. Wind speeds between 11 m/s and 17 m/s only result in a response from 0.0025 m/s² up to 0.0125 m/s² at a wider AOA band between -2° and +10°. This contrasts with the lateral wind response, where the wind speed had a lesser impact on the observable wind response. As discussed in 1.3.2 Wind load coefficients and showcased in Figure 31, the linearity assumption for the lift coefficient is accurate at about -15° to +5°. We see that the datapoints at wind speeds above 11 m/s causing large vertical responses are partially below +5° and partially above +5°. This suggests that the linearity assumption for the lift coefficient is suitable to predict some of the large vertical responses at lower AOAs correctly, but overestimates some of the large vertical responses for AOAs above +5°.



Normalizing the lateral bridge response by turbulence intensity again results in Figure 97, similar to Figure 89.

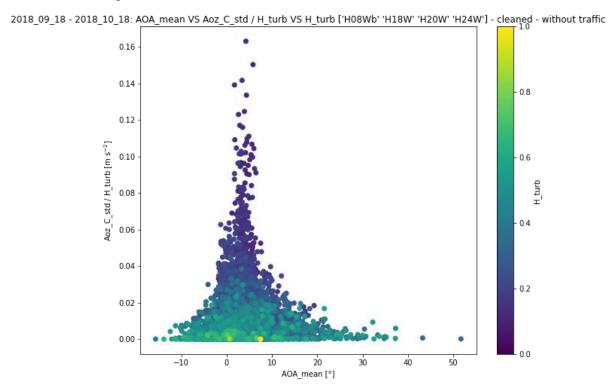


Figure 97: Vertical bridge response normalized by turbulence intensity and turbulence intensity at different angles of attack

Again we see that some of the higher bridge responses at lower mean wind speeds and at angles of attack further out from 0° are brought down in the normalized scatterplot, as they are more correlated with higher turbulence intensity.



Figure 98 shows the correlation between *H_mean* and *Aoz_C_std*, similar to Figure 90.

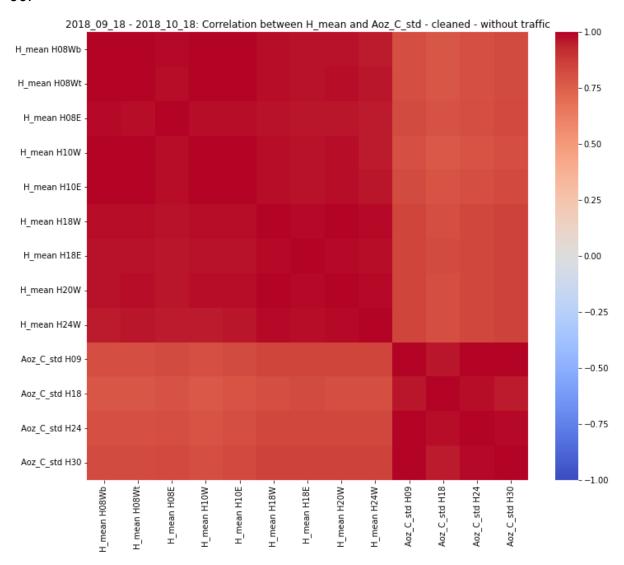


Figure 98: Correlation between mean wind speed and vertical bridge response per anemometer and accelerometer

From Figure 98 we see that the correlation coefficients between all the accelerometer pairs on the vertical response is close to 1, displayed as dark red color in the lower right quadrant. The correlation between accelerometers H09, H24 and H30 is slightly higher compared to the correlations with H18. This is most likely due to the vertical eigenmode shapes depicted in Figure 30, in which the bridge oscillates less at midspan H18, compared to further out towards the north or south, H09 or H24 and H30 respectively. The correlation between H18 and H24 is still higher than the correlation between H18 and H09 or H30, as the former are closer together. The



correlation to the mean horizontal wind velocity is also relatively high at about 0.75 to 0.85. This is higher than the correlation of the lateral response depicted in Figure 90. It is also more homogenous, with a slightly higher correlation to *H_mean* towards the south of the bridge.

Figure 99 shows the correlation between *H_turb* and *Aoz_C_std*, similar to Figure 91.

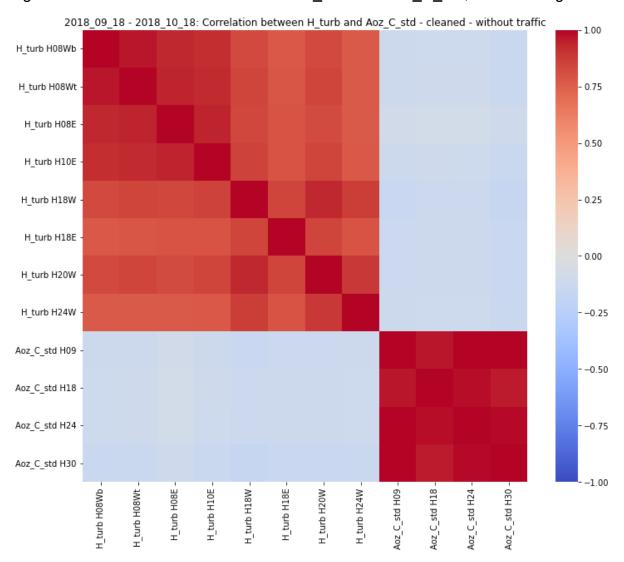


Figure 99: Correlation between turbulence intensity and vertical bridge response per anemometer and accelerometer

From Figure 99 we see that the correlation between the vertical response and horizontal turbulence intensity is homogenously slightly negative at about -0.2, which is in contrast to the lateral response which was less correlated as depicted in Figure 91.



Figure 100 shows the correlation between absolute *AOA_mean* and *Aoz_C_std*, similar to Figure 92.

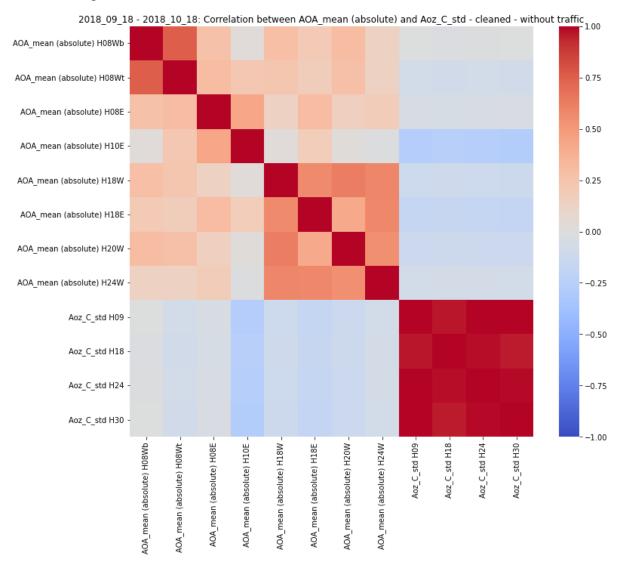


Figure 100: Correlation between absolute mean angle of attack and vertical bridge response per anemometer and accelerometer

From Figure 100 we see that the correlation between the vertical response and absolute mean AOA is close to 0, or slightly negative for anemometers at H10E at about -0.3 as well as H08Wt, H18E and H20W between 0 and -0.25. This, similar to the observation on the lateral response from Figure 92, coincides with the anomaly detected in Figure 82 and discussed in *4.1.3 Angle of attack*. No further significant assumptions can be drawn from these correlations.



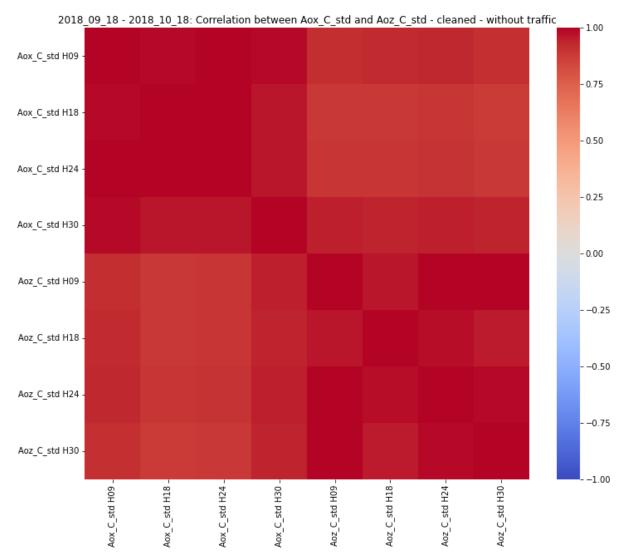


Figure 100 shows the correlation between *Aox_C_std* and *Aoz_C_std*.

Figure 101: Correlation between lateral and vertical wind response per accelerometer

From Figure 101 we see that the lateral and vertical wind response are well correlated with correlation coefficients above 0.8. The lateral response measured at the outer accelerometers at H09 and H30 is slightly more correlated with the vertical response measured at all accelerometers than the lateral response measured at the inner accelerometers H18 and H24 is.



4.2.4 Torsional wind response

In Figure 102 to Figure 111 the torsional wind response of the bridge, measured by the standard deviation of torsional acceleration *theta_std* is visualised, analysed and compared to the vertical wind response discussed in *4.2.3 Vertical wind response*.

Figure 102 shows a scatterplot of *theta_std* over the mean horizontal wind component perpendicular to the primary bridge axis *Vx_mean* with the respective turbulence intensity *Vx_turb* on the color-axis, similar to Figure 93.

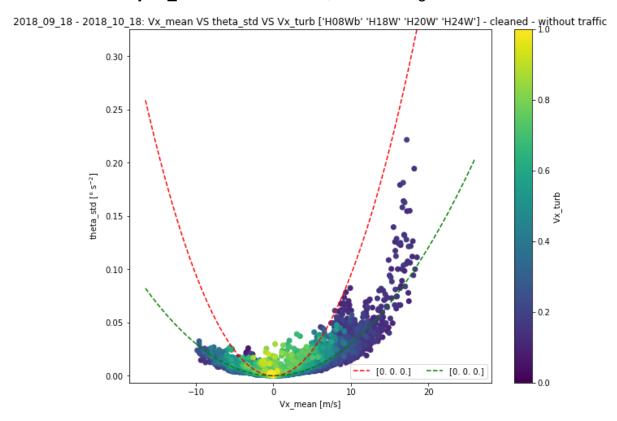


Figure 102: Torsional bridge response and turbulence intensity at different mean wind speeds

The highest standard deviation of torsional acceleration is measured at about 0.22 °/s² at a perpendicular wind speed of about 18 m/s and low turbulence intensity. This is under the same conditions as the highest measured standard deviation of vertical acceleration. At about 10 m/s *theta_std* is measured at about 0.08 °/s² at low turbulence intensity. At about 7 m/s *theta_std* is measured at about 0.05 °/s² at a turbulence intensity of up to about 0.6. We see that theta_std can increase by up to 3 times at about 18 m/s without a significant change in turbulence intensity.



Figure 103 and Figure 104 showcase *theta_std / Vx_turb* for south-westerly and north-easterly wind conditions respectively, split across the accelerometer pairs at H09, H18, H24 and H30, similar to Figure 94 and Figure 95.

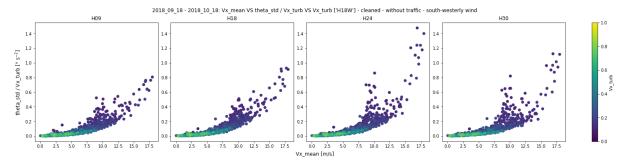


Figure 103: Torsional bridge response normalized by turbulence intensity and turbulence intensity at different mean wind speeds for south-westerly winds per accelerometer pair

As expected, the data is folded in on itself and bound by an upper and lower parabola shape. The remaining spread occurring with higher wind speeds is low, up to 7.5 m/s. Above 7.5 m/s the spread increases.

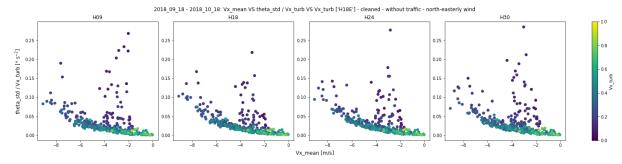


Figure 104: Torsional bridge response normalized by turbulence intensity and turbulence intensity at different mean wind speeds for north-easterly winds per accelerometer pair

As in the case for vertical response in Figure 95, similar observations are again to be made for the north-easterly winds for the torsional response. At wind speeds between -2 m/s and -4 m/s there is a high spread. Between -4 m/s and -6 m/s the spread is low again before increasing again.



Figure 105 shows the vertical bridge response at different mean AOAs with the mean horizontal wind speed decoded on the color-axis, similar to Figure 96.

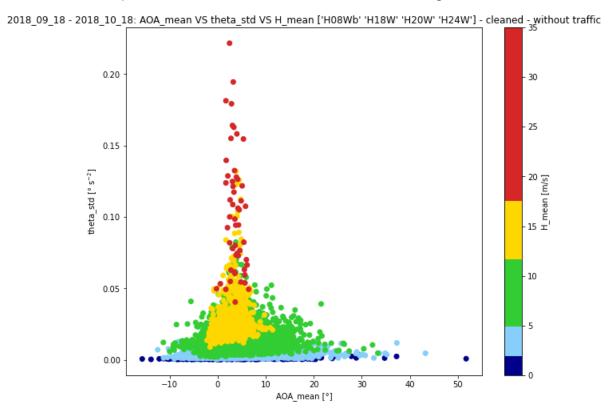


Figure 105: Torsional bridge response and mean wind speed at different angles of attack

From Figure 105 we see that larger torsional responses above 0.08 °/s² and up to about 0.22 °/s² can be observed primarily at wind speeds above 11 m/s at AOAs between +2° to +7°. This is similar to the vertical wind response, where the wind speed has a significant impact on the observable wind response. As discussed in 1.3.2 Wind load coefficients and showcased in Figure 31, the linearity assumption for the moment coefficient is accurate at about -12° to +5°. We see that the datapoints at wind speeds above 11 m/s causing large torsional responses are mostly just below +5° and only partially above +5°. This suggests that the linearity assumption for the lift coefficient is suitable to predict most of the large torsional responses at lower AOAs correctly, but overestimates some of the large torsional responses for AOAs above 5°.



Normalizing the lateral bridge response by turbulence intensity again results in Figure 106, similar to Figure 97.

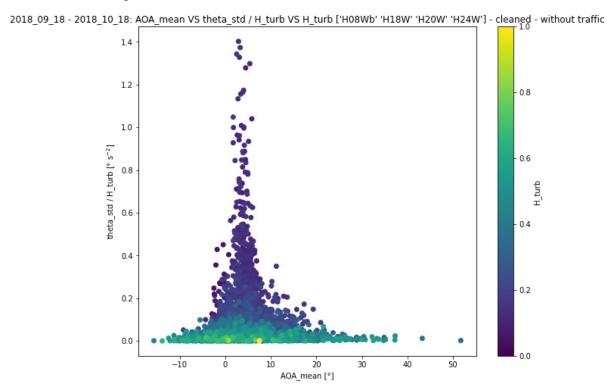


Figure 106: Torsional bridge response normalized by turbulence intensity and turbulence intensity at different angles of attack

In contrast to the lateral and vertical response we do not see as much of an effect from the normalisation, suggesting that high turbulence intensity has a lesser correlation with the torsional wind response.



Figure 107 shows the correlation between *H_mean* and *theta_std*, similar to Figure 98.

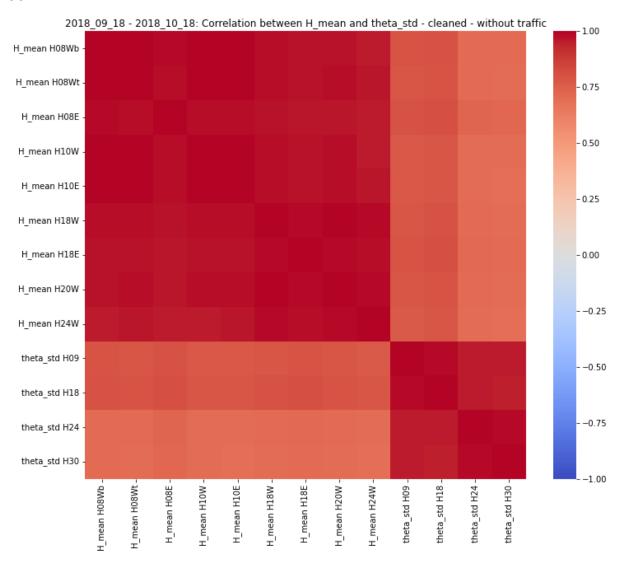


Figure 107: Correlation between mean wind speed and torsional bridge response per anemometer and accelerometer

From Figure 107 we see that the correlation coefficients between all the accelerometer pairs on the tortional response is close to 1, displayed as dark red color in the lower right quadrant. The respective correlation between accelerometers H09 and H18 as well as H24 and H30 is slightly higher compared to the correlations across both groups. This is most likely due to the asymmetric torsional eigenmode shape depicted in Figure 30, in which the north half of the bridge, H09 and H18, oscillates in the opposite direction to the south half, H24 and H30.

There is a positive correlation to the mean horizontal wind velocity, which is slightly higher at about 0.75 for H09 and H18, compared to H24 and H30, where it is about



0.55. The former is comparable to the correlation of the vertical response depicted in Figure 98, while the later is slightly lower, more compareable to the lateral response depicted in Figure 90. However, it is more homogenous across the anemometers. Figure 108 shows the correlation between *H_turb* and *theta_std*, similar to Figure 99.

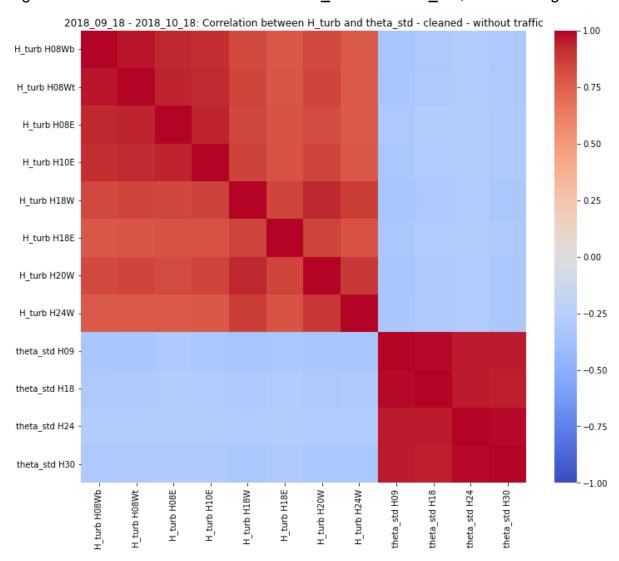


Figure 108: Correlation between turbulence intensity and torsional bridge response per anemometer and accelerometer

From Figure 108 we see that the correlation between the tortional response and horizontal turbulence intensity is homogenously slightly negative at about -0.25, which is similar to the vertical response depicted in Figure 99.



Figure 109 shows the correlation between absolute *AOA_mean* and *theta_std*, similar to Figure 100.

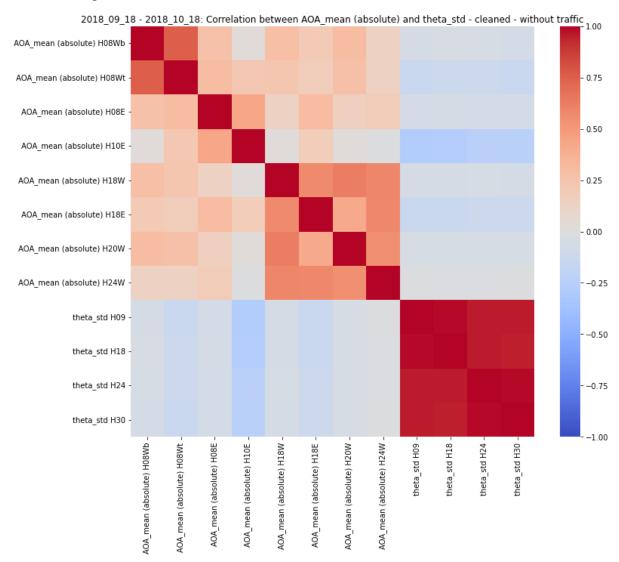


Figure 109: Correlation between absolute mean angle of attack and torsional bridge response per anemometer and accelerometer

From Figure 109 we see that the correlation between the tortional response and absolute mean AOA is close to 0, or slightly negative for anemometers at H10E at about -0.3 as well as H08Wt and H18E between 0 and -0.2. This, similar to the observation on the vertical response from Figure 100, coincides with the anomaly detected in Figure 82 and discussed in *4.1.3 Angle of attack*. No further significant assumptions can be drawn from these correlations.



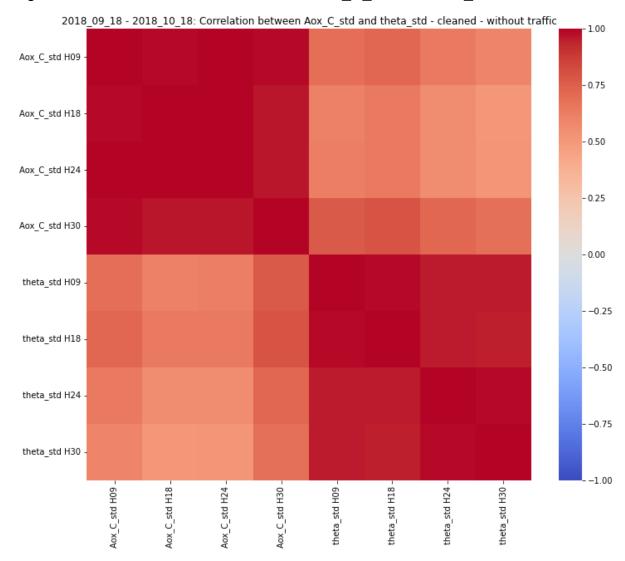


Figure 110 shows the correlation between *Aox_C_std* and *theta_std*.

Figure 110: Correlation between lateral and torsional wind response

From Figure 110 we see that the lateral and tortional wind response are somewhat positively correlated with correlation coefficients from about 0.45 to about 0.65, which is lower than the correlation between lateral and vertical wind response. The lateral response measured at the outer accelerometers at H09 and H30 is slightly more correlated with the tortional response measured at all accelerometers than the lateral response measured at the inner accelerometers H18 and H24 is. This is similar to the correlation between lateral and vertical response.



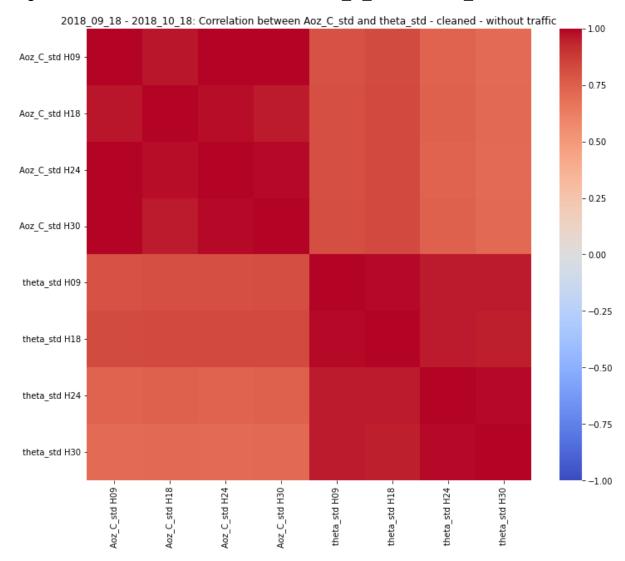


Figure 111 shows the correlation between *Aoz_C_std* and *theta_std*.

Figure 111: Correlation between vertical and torsional wind response

From Figure 111 we see that the vertical and tortional wind response are more positively correlated with correlation coefficients between about 0.65 and 0.85. The tortional response measured at the northern accelerometers at H09 and H18 is slightly more correlated with the vertical response measured at all accelerometers than the tortional response measured at the southern accelerometers H24 and H30 is.



5. Discussion

The results from this work are summarized and discussed in the sections below.

5.1 Conclusion

The results from analysis confirm the primary wind directions of NNE and SSW. Mean wind speeds reached up to 21.5 m/s and gusts up to 35 m/s in the 30-day period. The directional bandwidth for south-westerly winds is about 15° wider than the one for north-easterly winds. Towards the south of the bridge there is a south tendency for south-westerly winds and north tendency for north-easterly winds. The wind from south-westerly direction is on average about 2.5 m/s higher than the wind from north-easterly direction. The highest wind speeds from south-westerly direction are almost double the highest wind speeds from north-easterly direction.

North-easterly winds are slightly more turbulent than south-westerly winds. Anemometers on the downwind side of the bridge record slightly more turbulent wind compared to their upwind counterparts. Turbulence intensity decrease with higher wind speeds. They are negatively correlated across all anemometers.

Mean AOAs reach from -33° to +53°, but 80% of the data is in a 12° range with a mean of about 3.4° and 0.9° for south-westerly and north-easterly winds respectively. The mean AOA is straightened towards 0° on the downwind side. The linearity assumption discussed in 1.3.2 Wind load coefficients is accurate enough for negative AOAs most of the time. For positive AOAs it overestimates lift coefficient and moment coefficient 25% of the time and underestimates drag coefficients 75% of the time for winds from south-westerly direction. Downwind anemometers experience less extreme AOAs compared to their upwind counterparts. An anomaly of high mean AOAs occurs at H18E with winds from easterly directions. Absolute mean AOA is not significantly correlated with mean horizontal wind speed or turbulence intensity, across the anemometers, except for H10E where there is a negative correlation with H mean and positive correlation with H turb.

The bridge displays a periodic response to the daily traffic with higher maximum vertical accelerations on weekdays due to heavy industrial traffic.

The highest vertical wind response is about 3.5 to 4 times higher than the highest lateral wind response. Most of the larger lateral wind responses are at AOAs above



the suitable range of the linearity assumption, where it underestimates the drag coefficient. Note that some of these larger responses might be correlated with higher turbulence intensity. The linearity assumption is partially suitable for the prediction of vertical and torsional responses, but overestimates some of the larger responses above +5° AOA.

Vertical wind response has the highest positive correlation to mean horizontal wind speed. Torsional wind response has a slightly lower positive correlation to mean horizontal wind speed, with slightly higher correlation at the northern accelerometers. Lateral wind response has the lowest positive correlation to mean horizontal wind speed with slightly higher correlation at the outer accelerometers.

Torsional wind response has the highest negative correlation to horizontal turbulence intensity. Vertical wind response has a low negative correlation to horizontal turbulence intensity. Lateral wind response has an insignificant negative correlation to horizontal turbulence intensity at the outer accelerometers. Lateral, vertical and torsional wind response have an insignificant negative correlation to absolute mean AOA with an anomaly occurring at H10E, where the correlation is slightly more negative.

Lateral and vertical wind response have a high positive correlation. Vertical and tortional wind response have a slightly lower positive correlation, with slightly lower correlations in the southern accelerometers. Lateral and torsional wind response have the lowest positive correlation, with slightly lower correlations in the inner accelerometers.

Note that correlation does not imply causation.

Creating a large amount of diverse but consistent visualisations for various measurement type combinations is fast and relatively easy with the methods provided by the *BridgeData* class created in this work. This allows to quickly get an overview of the data and phenomena happening at the bridge. It allows to find interesting phenomena and anomalies that might be overlooked in a more directed approach. The flexible and modular design allows to focus observations on desired phenomena, for example by using filters. Interpreting the visualisations to explain some of the phenomena requires extensive background knowledge in the field of wind engineering.



The ability to save the state of a class object is particularly useful, as it allows to quickly come back to a previous analysis without having to re-import the data.

5.2 Comparison to relevant works

Some of the relevant works on data of the Lysefjord Bridge include [2], [3], [7], [20], [24], and [18]. These works were regularly referenced in the creation of this work.

Figure 112 shows a direct comparison on the turbulence intensity for different windspeeds to E. Chynet's analysis in 2016 [20, p. 18]. The same period and same sensors have been used for this visualisation. E. Cheynet's scatterplot has been layered on top of this works scatterplot, matching the scaling of the axis.

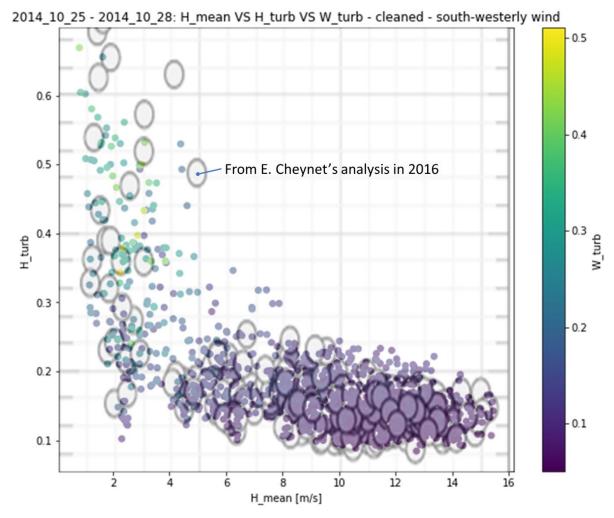


Figure 112: Comparison of turbulence intensity at different wind speeds to E. Cheynet's work in 2016. Adapted from [20, p. 18]

Figure 112 illustrates that a very similar visualisation of the data can be achieved from the same data base. Note that some datapoints might be missing in either scatterplot or have slight variations in their position due to different methods used in



importing and processing of the data, such as the slightly different calculation of the turbulence intensity, as described in 3.1.1 convert_MATLAB. However, the general structure of the scatterplot is very much comparable, showing the same decrease in turbulence intensity with higher wind speeds.

Similarly, a polar scatterplot from E. Cheynet's work in 2016 [20, p. 136] has been replicated using data from 07/10/2014, as depicted in Figure 113.

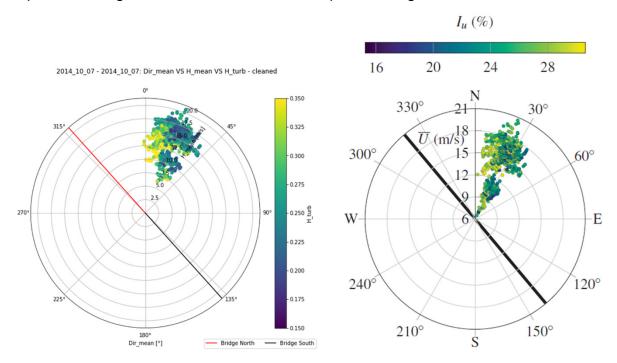


Figure 113: Turbulence visualisation from this work (left) and E. Cheynet's work in 2016 (right) [20, p. 136]

Note that the radial axis starts at 0 m/s in this work, while it starts at 6 m/s in E. Cheynet's work. Apart from slightly different scaling on the radial axis and color axis the polar scatter plots match up very well.

Furthermore E. Cheynet calculates "a mean wind direction of 22° and a standard deviation of almost 9°" [20, p. 135], referring to geographic north. In this work a mean wind direction of about 21° and standard deviation of about 8° is calculated.

Some slight variations might again occur due to different methods in the importing and processing of the data. Also note that differently colored dots on a scatterplot might be plotted on top of each other in a different order. This can be misleading when trying to interpret the color axis. Therefore, lowest color axis values are usually plotted first and higher values afterwards in the colored scatter plots of this work.



However, this can be disabled by setting *plot_in_order_of_color* to *False*. This was done in this comparison to better match E. Cheynet's work.

In contrast to the previously mentioned relevant works, this work did not focus on interpreting results of a particular analysis. However, the author created a toolset to easily and quickly create large amounts of diverse but consistent visualisations for various measurement type combinations, which can help to gain a different perspective on the data. It is possible to perform extensive and detailed analysis on the data using this works code, as demonstrated in 4 Analysis using this works code. The results from this analysis are in line with the results expected from previous relevant works. Useful insights into wind conditions and wind responses are obtained. This includes statistical descriptions and comparisons of north-easterly and south-westerly wind conditions, correlations of wind responses to wind conditions, evaluation of the linearity assumption described in 1.3.2 Wind load coefficients and the discovery of previously unknown anomalies at H10E and H18E.

5.3 Limitations of this work

The technical limitations of this work lie in memory-constraints and the disk-space required to process a larger amount of the relatively large MATLAB files. The computational load during the import stage and the creation of some of the plots, especially scatter plots, is therefore quite high with larger datasets and suffer from a lack of parallel processing. Some of the plots lack flexibility as not all the original matplotlib functionality on which they are based on is passed along. The data filtering is somewhat limited compared to some of the available tools used for database manipulations. Some more in-depth tools for specific types of analysis, such as spectral analysis and modal analysis are currently not implemented. The interpretation of the analysis is not very in-depth and might be incomplete or incorrect as the author has no background in wind engineering. This also shows as there is currently no implementation for transforming the coordinate system to mean wind coordinates, which would commonly be used for turbulence-intensity calculations for example. However, the modular design of this works code should allow to easily implement the missing functionality or use third-party libraries in the data processing and analysis.



5.4 Future work

While the author took care to utilise the parallel computation of numpy functionality, attempts on further parallelisation should be made where possible, using *multiprocessing* for example. To further decrease the computational load, a high-performance Python compiler such as *numba* could be utilized. Other methods to increase performance could be *gpu utilisation* or *outsourcing* parts of the process to a server, or high-performance cluster.

Another approach to improve this work lies in implementing additional functionality such as spectral analysis, modal analysis or the transformation to mean wind coordinates. Additionally, machine learning could be used to, for example, perform regression on the wind response and clustering on the wind conditions. B. da Costa gives a great overview of possibilities in [51].

Finally, the anomalies discovered at H18E and H10E could be further examined for example by performing CFD-simulations or LIDAR studies. The suitability of the linearity assumption could be further examined, especially regarding the potential underestimation of the drag coefficient at positive AOAs.

5.5 Authors experience

For the author it was of high importance to create a modular, flexible tool that could be used to perform further analysis than what has been done in this work. The Python and Jupyter Notebook environment have perfectly supported this goal. Style guides and documentations of Python and its libraries such as [35], [36], [37], [41], [42], [43], [44], [45] and [47] were very helpful in building the *BridgeData* class and documenting it properly. Examining the data and creating large amounts of diverse but consistent visualisations for various measurement type combinations has been a very enjoyable process for the author. The previous relevant works on the bridge data have been very helpful to understand the complex wind engineering related phenomena around the Lysefjord Bridge.

The author assumed a role in between the perspective of a wind engineer and a data scientist. This has required a cross-disciplinary mindset, which allowed the author to acquire, utilise and reproduce knowledge from both domains without the need for an in-depth background in either. While this experience has been challenging, the knowledge and skillsets gained from both domains are worth it.



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Appendix

A1: Complete Code

- → The code itself is provided as an .ipynb file. The data is to be obtained from UiS.
- → Below you will find a .pdf conversion of the Jupyter Notebook. Note that this does not reflect the complete code as some of the longer lines are truncated.

Analysis of wind and response measurement data from a suspension bridge

This Jupyter Notebook is accompanying documentation to the **MASTER'S THESIS** Analysis of wind and response measurement data from a suspension bridge by René König.

Universitetet i Stavanger (UiS)

FACULTY OF SCIENCE AND TECHNOLOGY

MASTER'S THESIS

Study programme / specialisation: Computational Engineering

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Author: René König, 268127

Supervisor at UiS: Professor Aksel Hiorth

Co-supervisor: Professor Jasna Bogunovic Jakobsen

External supervisor(s): Bernardo Morais da Costa, Statens vegvesen

Thesis title: Analysis of wind and response measurement data from a suspension bridge

Credits (ECTS): 30

Keywords: Python, Data Science, Software Development, Suspension Bridge, Wind Engineering, Wind Response, Full-Scale Monitoring, Anemometers, Accelerometers

Stavanger, 14.06.2023

Abstract

The Lysefjord Bridge is a suspension bridge at the entrance to the Lysefjord in south western Norway at which full-scale measurements on wind conditions and bridge response are collected using anemometers and accelerometers. In this work Python is used to develop a toolset for analysing the wind and response measurement data from the Lysefjord Bridge. The functionality is provided through different methods compiled in a class. This includes methods for importing and combining data from multiple days, re-arranging and interpreting the data, feature engineering, data cleaning, filtering and various types of visualisations. The code is demonstrated in an analysis of 30 days of data. The analysis focuses on the wind conditions for south-westerly and north-easterly winds in terms of wind speeds, primary directions, turbulence intensity and angle of attack as well as the bridges lateral, vertical and torsional wind response. The analysis shows on average slightly higher wind speeds, lower turbulence intensities and higher angles of attack for south-westerly winds, compared to north-easterly winds. Towards the

southern end of the bridge the wind direction has a south tendency for south-westerly winds and north tendency for north-easterly winds. Turbulence intensity is measured slightly higher on the downwind side of the bridge. The angle of attack is straightened towards 0° on the downwind side. Furthermore, the analysis shows that the assumption of a linear correlation between drag coefficient and angle of attack used in the so-called quasi-steady theory of wind loading and the corresponding numerical simulations underestimates most of the larger lateral bridge responses at angles of attack above 0°. The lift and moment coefficients estimated using similar linearity assumptions overestimate some of the larger vertical and torsional bridge responses at angles of attack above +5°.

Libraries used

The libraries below are used in this code.

```
import numpy as np # Math, handling data arrays
import matplotlib.pyplot as plt # Plots
import matplotlib as mpl # Handle colormaps
from matplotlib.colors import ListedColormap # Create colormaps
import scipy.io # Read matlab files
import scipy.optimize # Curve-fitting
import scipy.stats # Statistics
import seaborn as sn # Heatmaps
from windrose import WindroseAxes # Wind roses
import gc # Garbage collection to free up memory
import dill # Saving and Loading data
import warnings
warnings.filterwarnings('ignore') # Clean up the notebook by ignoring the expected w
```

The code was developed under Python version 3.9.6

BridgeData class definition

The BridgeData class defined below contains most of the functionallity of this work to load, process and analyze data from the Lysefjord Bridge.

```
In [ ]:
         class BridgeData:
             """A class for processing wind and response data from a suspensionbridge, as in
             Attributes
             -----
             file_names : list of strs
                 List of Lysefjord Bridge dataExtracted.mat MATLAB file names at `file_path`
             file path : str
                 Defining the filepath to the location of the bridge data relative to this no
             char lim : int, default 255
                 Character limit for filepath when saving figures. A too long fliepath can le
             tower_dist : float, default 446
                 Distance between the two towers of the bridge in meters.
             sag : float, default 45
                 Sag of the main cables in meters, measured from the top of the towers.
             n_hangers : int, default 35
                 Number of hanger pairs (hangers per main cable) between the towers.
             hanger dist : float, default 12
```

```
Distance between hanger pairs in y-direction in meters.
first_hanger_y_tower_dist : float, default 19
    Distance of the first hanger pair from the north tower in meters.
last_hanger_y_tower_dist : float, default 19
    Distance of the last hanger pair from the south tower in meters.
mid_span_cable_height_above_deck : float, default = 3
   Height of the main cables above the deck at mid-span in meters.
mid_span_deck_height : float, default 53.37
   Height of the deck above the waterline at mid-span in meters.
acc_x_dist_from_centerline : float, default 7.15/2
    Distance from the East and West accelerometers from the centerline of the br
g : float, default 9.818287
    Local gravity constant. Default value for stavanger measured according to 'G
anemo_range : float, default 65
    Anemometer range in +- m/s.
acc_range : float, default 5
   Accelerometer range in +- G.
def __init__(self,file_names,file_path = '../Data/Bridge/dataExtracted/',char_li
             tower_dist = 446, # m
             h_{towers} = 102.26, \# m
             sag = 45, # m
             n_{\text{hangers}} = 35,
             hanger_dist = 12, # m
             first_hanger_y_tower_dist = 19, # m
             last_hanger_y_tower_dist = 19, # m
             mid_span_cable_height_above_deck = 3, # m
             mid_span_deck_height = 53.37, # m
             tower 1 deck support height = 44.9, # m
             tower_2_deck_support_height = 52.36, # m
             girder_height = 2.76, # m
             cable_section_weight = 816, # kg/m
             hanger_section_weight = 95, # kg/m
             girder_section_weight = 5350, # kg/m
             cable_x_dist = 10.5, # m assumption
             deck_width = 9.5, # m assumption
             girder_width = 12.3, # m
             acc_x_dist_from_centerline = 7.15/2, # m
             g = 9.818287,
             anemo\_range = 65,
             acc_range = 5
             ):
    """Initializes the class.
    Parameters
    _____
    file names : list of strs
        List of Lysefjord Bridge dataExtracted.mat MATLAB file names at `file_pa
    file path : str
       Defining the filepath to the location of the bridge data relative to thi
    char_lim : int, default 255
       Character limit for filepath when saving figures. A too long fliepath ca
    tower_dist : float, default 446
       Distance between the two towers of the bridge in meters.
    sag : float, default 45
       Sag of the main cables in meters, measured from the top of the towers.
    n hangers : int, default 35
       Number of hanger pairs (hangers per main cable) between the towers.
    hanger_dist : float, default 12
       Distance between hanger pairs in y-direction in meters.
    first_hanger_y_tower_dist : float, default 19
       Distance of the first hanger pair from the north tower in meters.
```

```
last_hanger_y_tower_dist : float, default 19
       Distance of the last hanger pair from the south tower in meters.
   mid_span_cable_height_above_deck : float, default = 3
       Height of the main cables above the deck at mid-span in meters.
    mid span deck height : float, default 53.37
       Height of the deck above the waterline at mid-span in meters.
    acc x dist from centerline : float, default 7.15/2
       Distance from the East and West accelerometers from the centerline of th
    g : float, default 9.818287
       Local gravity constant. Default value for stavanger measured according t
    anemo_range : float, default 65
       Anemometer range in +- m/s.
    acc_range : float, default 5
       Accelerometer range in +- G.
    self.file_names = file_names
    self.file_path = file_path
    self.char_lim = char_lim
    self.tower_dist = tower_dist
    self.h_towers = h_towers
    self.sag = sag
    self.n_hangers = n_hangers
    self.hanger_dist = hanger_dist
    self.first_hanger_y_tower_dist = first_hanger_y_tower_dist
    self.last_hanger_y_tower_dist = last_hanger_y_tower_dist
    self.mid_span_cable_height_above_deck = mid_span_cable_height_above_deck
    self.mid_span_deck_height = mid_span_deck_height
    self.tower_1_deck_support_height = tower_1_deck_support_height
    self.tower 2 deck support height = tower 2 deck support height
    self.girder_height = girder_height
    self.cable_section_weight = cable_section_weight
    self.hanger_section_weight = hanger_section_weight
   self.girder_section_weight = girder_section_weight
    self.deck_width = deck_width
    self.girder_width = girder_width
    self.cable_x_dist = cable_x_dist
    self.acc_x_dist_from_centerline = acc_x_dist_from_centerline
    self.g = g
    self.anemo_range = anemo_range
    self.acc_range = acc_range
    self.acc\_unit = '\mu G'
# Pre-processing
def convert_MATLAB(self,data,delete_data_after_import=True,ignore_nans=True,rena
    """Convert Lysefjord Bridge dataExtracted.mat files imported via `scipy.io.l
    Parameters
    _____
    data : dict of {str : ndarray}
       Dictionary with variable names as keys, and loaded matrices as values fr
    delete_data_after_import : bool, default True
       Delete original `data` from memory after import to free up memory.
    ignore_nans : bool, default True
        Ignores nans when calculating mean, std, min and max, using the remaining
    rename H20 acc : bool, default True
        Rename accelerometers H20 to H24, as there seems to be a systematic erro
    replace invalid : bool, default True
        Replace invalid sensor readings (outside of technical sensor range) with
    full_detail : bool, default False
        Keep full detail of `data`, sampled at 50Hz instead of resampling to eve
   H ... TopBottom : bool, default True
       Select which part of the `data` should be imported or generated during i
```

```
Returns
anemo names : list of str
    List of anemometer names.
acc_names : list of str
    List of accelerometer names.
time_array : array_like
t_array : array_like
anemo : dict of {str : array_like}
    Data from anemometers, 2d arrays sensor_id x measurement_id, grouped by
acc : dict of {str : array_like}
    Data from accelerometers, 2d arrays sensor id x measurement id, grouped
weather : dict of {str : array_like}
    Data from weatherstation, 1d arrays measurement_id, grouped by measureme
# Convert time data.
time = data['time'].T[0]
t = data['t'][0]
time_array = time
t_array = np.repeat(t,time_array.shape[0])
# Get names of anemometers and accelerometers.
anemo_names = []
acc_names = []
for ind, anemo in enumerate(data['AnemoName'][0]):
    anemo_names.append(anemo[0])
for ind,acc in enumerate(data['AccelName'][0]):
    if rename H20 acc:
        if acc[0] == 'H20':
            acc_names.append('H24')
        else:
            acc_names.append(acc[0])
    else:
        acc_names.append(acc[0])
anemo_names = np.array(anemo_names)
acc_names = np.array(acc_names)
anemo_shape = (len(anemo_names),len(time))
acc_shape = (len(acc_names),len(time))
# Initialize dicts for data from anemometers, weather and accelerometers.
anemo = \{\}
weather = {}
acc = \{\}
if replace invalid:
    # Replace data out of technical range of sensors with nan.
    data['H'][(data['H']>self.anemo range)|(data['H']<0)] = np.nan</pre>
    data['W'][(data['W']>self.anemo\_range)|(data['W']<-self.anemo\_range)] =
    data['Dir'] = np.where((data['Dir']>360)|(data['Dir']<0),np.nan,data['Di</pre>
    data['Aox_W'][(data['Aox_W']>self.acc_range*1e6)|(data['Aox_W']<-self.ac</pre>
    data['Aoy W'][(data['Aoy W']>self.acc range*1e6)|(data['Aoy W']<-self.ac</pre>
    data['Aoz_W'][(data['Aoz_W']>(self.acc_range+1)*1e6)|(data['Aoz_W']<-(self.acc_range+1)*1e6)|</pre>
    data['Aox_E'][(data['Aox_E']>self.acc_range*1e6)|(data['Aox_E']<-self.ac</pre>
    data['Aoy E'][(data['Aoy E']>self.acc range*1e6)|(data['Aoy E']<-self.ac</pre>
    data['Aoz_E'][(data['Aoz_E']>(self.acc_range+1)*1e6)|(data['Aoz_E']<-(se</pre>
# Decompose horizontal wind vector into vx and vy component
# according to the bridge coordinate system.
```

```
vx = -np.sin(np.deg2rad(data['Dir']))*data['H']
vy = -np.cos(np.deg2rad(data['Dir']))*data['H']
if full detail:
    # Retain full detail of the data, sampled at 50Hz instead of every 10min
   # Note that the data is described as _mean, although no mean is calculat
   # This enables use of functions orig. designed for the downsampled data.
   self.full_detail = True
   anemo_shape = (len(anemo_names),len(t)*len(time))
   acc_shape = (len(acc_names),len(t)*len(time))
    # Transform time arrays.
   time_array = np.linspace(time[0],time[-1],len(t)*len(time))
   t_array = np.tile(t,len(time))
   # Convert/create numpy arrays from original data
   # organized in dictionaries by type of measurement.
   if H:
        anemo['H_mean'] = data['H'].reshape(anemo_shape)
   if W:
        anemo['W_mean'] = data['W'].reshape(anemo_shape)
   if Vx or Dir or Upwind:
        anemo['Vx_mean'] = vx.reshape(anemo_shape)
    if Vy or Dir or Upwind:
        anemo['Vy_mean'] = vy.reshape(anemo_shape)
   if Dir or Upwind:
        anemo['Dir_mean'] = data['Dir'].reshape(anemo_shape)
   if Tv:
        anemo['Tv_mean'] = data['Tv'].reshape(anemo_shape)
   if AOA:
        anemo['AOA_mean'] = np.rad2deg(np.arctan(data['W']/data['H'])).resha
        anemo['AOI_mean'] = np.where((0<data['Dir'])&(data['Dir']<=90),90-da</pre>
    if Aox W:
        acc['Aox_W_mean'] = data['Aox_W'].reshape(acc_shape)
   if Aoy_W:
        acc['Aoy_W_mean'] = data['Aoy_W'].reshape(acc_shape)
    if Aoz W:
        acc['Aoz_W_mean'] = data['Aoz_W'].reshape(acc_shape)
        acc['Aox_E_mean'] = data['Aox_E'].reshape(acc_shape)
    if Aoy_E:
        acc['Aoy_E_mean'] = data['Aoy_E'].reshape(acc_shape)
    if Aoz E:
        acc['Aoz_E_mean'] = data['Aoz_E'].reshape(acc_shape)
    if centr:
        acc['Aox_C_mean'] = ((data['Aox_W']+data['Aox_E'])/2).reshape(acc_sh
        acc['Aoy_C_mean'] = ((data['Aoy_W']+data['Aoy_E'])/2).reshape(acc_sh
        acc['Aoz_C_mean'] = ((data['Aoz_W']+data['Aoz_E'])/2).reshape(acc_sh
```

```
if theta:
        acc['theta mean'] = np.rad2deg(np.arctan(((data['Aoz W'] - data['Aoz
   if T:
       weather['T mean'] = data['T'].flatten()
   if P:
       weather['P mean'] = data['P'].flatten()
   if Hum:
        weather['Hum_mean'] = data['Hum'].flatten()
else:
   self.full detail = False
   # Convert/create numpy arrays from original data
   # organized in dictionaries by type of measurement.
   if ignore_nans:
        # Use np.nanmean etc. instead of np.mean to ignore nans.
            anemo['H_mean'] = np.nanmean(data['H'],axis=2)
            anemo['H_std'] = np.nanstd(data['H'],axis=2)
            anemo['H_min'] = np.nanmin(data['H'],axis=2)
            anemo['H_max'] = np.nanmax(data['H'],axis=2)
       if W:
            anemo['W_mean'] = np.nanmean(data['W'],axis=2)
            anemo['W_std'] = np.nanstd(data['W'],axis=2)
            anemo['W_min'] = np.nanmin(data['W'],axis=2)
            anemo['W_max'] = np.nanmax(data['W'],axis=2)
        if Vx or Dir or Upwind:
            anemo['Vx_mean'] = np.nanmean(vx,axis=2)
            anemo['Vx_std'] = np.nanstd(vx,axis=2)
            anemo['Vx_min'] = np.nanmin(vx,axis=2)
            anemo['Vx_max'] = np.nanmax(vx,axis=2)
        if Vy or Dir or Upwind:
            anemo['Vy_mean'] = np.nanmean(vy,axis=2)
            anemo['Vy_std'] = np.nanstd(vy,axis=2)
            anemo['Vy_min'] = np.nanmin(vy,axis=2)
            anemo['Vy max'] = np.nanmax(vy,axis=2)
        if Dir or Upwind:
            # Calculate mean of direction from Vx_mean and Vy_mean
            # instead of original data to deal with 360-0 discontinuity.
            anemo['Dir_mean'] = (np.rad2deg(np.arctan2(anemo['Vx_mean'],anem
            #vv Physically irrelevant because of 360-0 discontinuity, kept f
            anemo['Dir std'] = (np.rad2deg(np.arctan2(anemo['Vx std'],anemo[
            anemo['Dir_min'] = (np.rad2deg(np.arctan2(anemo['Vx_min'],anemo[
            anemo['Dir max'] = (np.rad2deg(np.arctan2(anemo['Vx max'],anemo[
            #^^ Physically irrelevant because of 360-0 discontinuity, kept f
       if Tv:
            anemo['Tv_mean'] = np.nanmean(data['Tv'],axis=2)
            anemo['Tv std'] = np.nanstd(data['Tv'],axis=2)
            anemo['Tv min'] = np.nanmin(data['Tv'],axis=2)
            anemo['Tv max'] = np.nanmax(data['Tv'],axis=2)
       if AOA:
            anemo['AOA mean'] = np.nanmean(np.rad2deg(np.arctan(data['W']/da
            anemo['AOA_std'] = np.nanstd(np.rad2deg(np.arctan(data['W']/data
            anemo['AOA min'] = np.nanmin(np.rad2deg(np.arctan(data['W']/data
            anemo['AOA_max'] = np.nanmax(np.rad2deg(np.arctan(data['W']/data
```

```
if AOI:
    anemo['AOI_mean'] = np.nanmean(np.where((0<data['Dir'])&(data['D</pre>
    anemo['AOI_std'] = np.nanstd(np.where((0<data['Dir'])&(data['Dir</pre>
    anemo['AOI_min'] = np.nanmin(np.where((0<data['Dir'])&(data['Dir'])</pre>
    anemo['AOI_max'] = np.nanmax(np.where((0<data['Dir'])&(data['Dir'])</pre>
if Aox_W:
    acc['Aox_W_mean'] = np.nanmean(data['Aox_W'],axis=2)
    acc['Aox_W_std'] = np.nanstd(data['Aox_W'],axis=2)
    acc['Aox_W_min'] = np.nanmin(data['Aox_W'],axis=2)
    acc['Aox_W_max'] = np.nanmax(data['Aox_W'],axis=2)
    acc['Aox_W_max_by_std'] = acc['Aox_W_max']/acc['Aox_W_std']
if Aoy_W:
    acc['Aoy_W_mean'] = np.nanmean(data['Aoy_W'],axis=2)
    acc['Aoy_W_std'] = np.nanstd(data['Aoy_W'],axis=2)
    acc['Aoy_W_min'] = np.nanmin(data['Aoy_W'],axis=2)
    acc['Aoy_W_max'] = np.nanmax(data['Aoy_W'],axis=2)
    acc['Aoy_W_max_by_std'] = acc['Aoy_W_max']/acc['Aoy_W_std']
if Aoz_W:
    acc['Aoz_W_mean'] = np.nanmean(data['Aoz_W'],axis=2)
    acc['Aoz_W_std'] = np.nanstd(data['Aoz_W'],axis=2)
    acc['Aoz_W_min'] = np.nanmin(data['Aoz_W'],axis=2)
    acc['Aoz_W_max'] = np.nanmax(data['Aoz_W'],axis=2)
    acc['Aoz_W_max_by_std'] = acc['Aoz_W_max']/acc['Aoz_W_std']
if Aox_E:
    acc['Aox_E_mean'] = np.nanmean(data['Aox_E'],axis=2)
    acc['Aox_E_std'] = np.nanstd(data['Aox_E'],axis=2)
    acc['Aox_E_min'] = np.nanmin(data['Aox_E'],axis=2)
    acc['Aox_E_max'] = np.nanmax(data['Aox_E'],axis=2)
    acc['Aox_E_max_by_std'] = acc['Aox_E_max']/acc['Aox_E_std']
if Aoy_E:
    acc['Aoy_E_mean'] = np.nanmean(data['Aoy_E'],axis=2)
    acc['Aoy_E_std'] = np.nanstd(data['Aoy_E'],axis=2)
    acc['Aoy_E_min'] = np.nanmin(data['Aoy_E'],axis=2)
    acc['Aoy_E_max'] = np.nanmax(data['Aoy_E'],axis=2)
    acc['Aoy_E_max_by_std'] = acc['Aoy_E_max']/acc['Aoy_E_std']
if Aoz E:
    acc['Aoz_E_mean'] = np.nanmean(data['Aoz_E'],axis=2)
    acc['Aoz_E_std'] = np.nanstd(data['Aoz_E'],axis=2)
    acc['Aoz_E_min'] = np.nanmin(data['Aoz_E'],axis=2)
    acc['Aoz_E_max'] = np.nanmax(data['Aoz_E'],axis=2)
    acc['Aoz_E_max_by_std'] = acc['Aoz_E_max']/acc['Aoz_E_std']
if centr:
    acc['Aox_C_mean'] = np.nanmean((data['Aox_W']+data['Aoy_E'])/2,a
    acc['Aox_C_std'] = np.nanstd((data['Aox_W']+data['Aox_E'])/2,axi
    acc['Aox_C_min'] = np.nanmin((data['Aox_W']+data['Aox_E'])/2,axi
    acc['Aox_C_max'] = np.nanmax((data['Aox_W']+data['Aox_E'])/2,axi
    acc['Aox_C_max_by_std'] = acc['Aox_C_max']/acc['Aox_C_std']
    acc['Aoy_C_mean'] = np.nanmean((data['Aoy_W']+data['Aoy_E'])/2,a
    acc['Aoy_C_std'] = np.nanstd((data['Aoy_W']+data['Aoy_E'])/2,axi
    acc['Aoy_C_min'] = np.nanmin((data['Aoy_W']+data['Aoy_E'])/2,axi
    acc['Aoy_C_max'] = np.nanmax((data['Aoy_W']+data['Aoy_E'])/2,axi
    acc['Aoy_C_max_by_std'] = acc['Aoy_C_max']/acc['Aoy_C_std']
    acc['Aoz_C_mean'] = np.nanmean((data['Aoz_W']+data['Aoz_E'])/2,a
    acc['Aoz_C_std'] = np.nanstd((data['Aoz_W']+data['Aoz_E'])/2,axi
```

```
acc['Aoz_C_min'] = np.nanmin((data['Aoz_W']+data['Aoz_E'])/2,axi
        acc['Aoz_C_max'] = np.nanmax((data['Aoz_W']+data['Aoz_E'])/2,axi
        acc['Aoz_C_max_by_std'] = acc['Aoz_C_max']/acc['Aoz_C_std']
    if theta:
        acc['theta_mean'] = np.nanmean(np.rad2deg(np.arctan(((data['Aoz_
        acc['theta_std'] = np.nanstd(np.rad2deg(np.arctan(((data['Aoz_W'
        acc['theta_min'] = np.nanmin(np.rad2deg(np.arctan(((data['Aoz_W'
        acc['theta_max'] = np.nanmax(np.rad2deg(np.arctan(((data['Aoz_W'
        acc['theta_max_by_std'] = acc['theta_max']/acc['theta_std']
    if T:
        weather['T_mean'] = np.nanmean(data['T'],axis=1)
        weather['T std'] = np.nanstd(data['T'],axis=1)
        weather['T_min'] = np.nanmin(data['T'],axis=1)
        weather['T_max'] = np.nanmax(data['T'],axis=1)
    if P:
        weather['P_mean'] = np.nanmean(data['P'],axis=1)
        weather['P_std'] = np.nanstd(data['P'],axis=1)
        weather['P_min'] = np.nanmin(data['P'],axis=1)
        weather['P_max'] = np.nanmax(data['P'],axis=1)
    if Hum:
        weather['Hum_mean'] = np.nanmean(data['Hum'],axis=1)
        weather['Hum_std'] = np.nanstd(data['Hum'],axis=1)
        weather['Hum_min'] = np.nanmin(data['Hum'],axis=1)
        weather['Hum_max'] = np.nanmax(data['Hum'],axis=1)
else:
    if H:
        anemo['H_mean'] = np.mean(data['H'],axis=2)
        anemo['H_std'] = np.std(data['H'],axis=2)
        anemo['H_min'] = np.min(data['H'],axis=2)
        anemo['H_max'] = np.max(data['H'],axis=2)
    if W:
        anemo['W_mean'] = np.mean(data['W'],axis=2)
        anemo['W_std'] = np.std(data['W'],axis=2)
        anemo['W_min'] = np.min(data['W'],axis=2)
        anemo['W max'] = np.max(data['W'],axis=2)
    if Vx or Dir or Upwind:
        anemo['Vx_mean'] = np.mean(vx,axis=2)
        anemo['Vx_std'] = np.std(vx,axis=2)
        anemo['Vx_min'] = np.min(vx,axis=2)
        anemo['Vx max'] = np.max(vx,axis=2)
    if Vy or Dir or Upwind:
        anemo['Vy_mean'] = np.mean(vy,axis=2)
        anemo['Vy_std'] = np.std(vy,axis=2)
        anemo['Vy_min'] = np.min(vy,axis=2)
        anemo['Vy_max'] = np.max(vy,axis=2)
    if Dir or Upwind:
        # Calculate mean of direction from Vx mean and Vy mean
        # instead of original data to deal with 360-0 discontinuity.
        anemo['Dir_mean'] = (np.rad2deg(np.arctan2(anemo['Vx_mean'],anem
        #vv Physically irrelevant because of 360-0 discontinuity, kept f
        anemo['Dir_std'] = (np.rad2deg(np.arctan2(anemo['Vx_std'],anemo[
        anemo['Dir_min'] = (np.rad2deg(np.arctan2(anemo['Vx_min'],anemo[
        anemo['Dir_max'] = (np.rad2deg(np.arctan2(anemo['Vx_max'],anemo[
        #^^ Physically irrelevant because of 360-0 discontinuity, kept f
```

```
if Tv:
    anemo['Tv_mean'] = np.mean(data['Tv'],axis=2)
    anemo['Tv_std'] = np.std(data['Tv'],axis=2)
    anemo['Tv_min'] = np.min(data['Tv'],axis=2)
    anemo['Tv_max'] = np.max(data['Tv'],axis=2)
if AOA:
    anemo['AOA_mean'] = np.mean(np.rad2deg(np.arctan(data['W']/data[
    anemo['AOA_std'] = np.std(np.rad2deg(np.arctan(data['W']/data['H
    anemo['AOA_min'] = np.min(np.rad2deg(np.arctan(data['W']/data['H
    anemo['AOA_max'] = np.max(np.rad2deg(np.arctan(data['W']/data['H
if AOI:
    anemo['AOI_mean'] = np.mean(np.where((0<data['Dir'])&(data['Dir'])</pre>
    anemo['AOI_std'] = np.std(np.where((0<data['Dir'])&(data['Dir'])</pre>
    anemo['AOI_min'] = np.min(np.where((0<data['Dir'])&(data['Dir']</pre>
    anemo['AOI_max'] = np.max(np.where((0<data['Dir'])&(data['Dir']</pre>
if Aox_W:
    acc['Aox_W_mean'] = np.mean(data['Aox_W'],axis=2)
    acc['Aox_W_std'] = np.std(data['Aox_W'],axis=2)
    acc['Aox_W_min'] = np.min(data['Aox_W'],axis=2)
    acc['Aox_W_max'] = np.max(data['Aox_W'],axis=2)
    acc['Aox_W_max_by_std'] = acc['Aox_W_max']/acc['Aox_W_std']
if Aoy_W:
    acc['Aoy_W_mean'] = np.mean(data['Aoy_W'],axis=2)
    acc['Aoy_W_std'] = np.std(data['Aoy_W'],axis=2)
    acc['Aoy_W_min'] = np.min(data['Aoy_W'],axis=2)
    acc['Aoy_W_max'] = np.max(data['Aoy_W'],axis=2)
    acc['Aoy_W_max_by_std'] = acc['Aoy_W_max']/acc['Aoy_W_std']
if Aoz_W:
    acc['Aoz_W_mean'] = np.mean(data['Aoz_W'],axis=2)
    acc['Aoz_W_std'] = np.std(data['Aoz_W'],axis=2)
    acc['Aoz_W_min'] = np.min(data['Aoz_W'],axis=2)
    acc['Aoz_W_max'] = np.max(data['Aoz_W'],axis=2)
    acc['Aoz_W_max_by_std'] = acc['Aoz_W_max']/acc['Aoz_W_std']
if Aox_E:
    acc['Aox_E_mean'] = np.mean(data['Aox_E'],axis=2)
    acc['Aox_E_std'] = np.std(data['Aox_E'],axis=2)
    acc['Aox_E_min'] = np.min(data['Aox_E'],axis=2)
    acc['Aox_E_max'] = np.max(data['Aox_E'],axis=2)
    acc['Aox_E_max_by_std'] = acc['Aox_E_max']/acc['Aox_E_std']
if Aoy E:
    acc['Aoy_E_mean'] = np.mean(data['Aoy_E'],axis=2)
    acc['Aoy_E_std'] = np.std(data['Aoy_E'],axis=2)
    acc['Aoy_E_min'] = np.min(data['Aoy_E'],axis=2)
    acc['Aoy_E_max'] = np.max(data['Aoy_E'],axis=2)
    acc['Aoy_E_max_by_std'] = acc['Aoy_E_max']/acc['Aoy_E_std']
if Aoz_E:
    acc['Aoz_E_mean'] = np.mean(data['Aoz_E'],axis=2)
    acc['Aoz_E_std'] = np.std(data['Aoz_E'],axis=2)
    acc['Aoz_E_min'] = np.min(data['Aoz_E'],axis=2)
    acc['Aoz_E_max'] = np.max(data['Aoz_E'],axis=2)
    acc['Aoz_E_max_by_std'] = acc['Aoz_E_max']/acc['Aoz_E_std']
if centr:
    acc['Aox_C_mean'] = np.mean((data['Aox_W']+data['Aox_E'])/2,axis
    acc['Aox_C_std'] = np.std((data['Aox_W']+data['Aox_E'])/2,axis=2
```

```
acc['Aox_C_min'] = np.min((data['Aox_W']+data['Aox_E'])/2,axis=2
            acc['Aox_C_max'] = np.max((data['Aox_W']+data['Aox_E'])/2,axis=2
            acc['Aox_C_max_by_std'] = acc['Aox_C_max']/acc['Aox_C_std']
            acc['Aoy C mean'] = np.mean((data['Aoy W']+data['Aoy E'])/2,axis
            acc['Aoy_C_std'] = np.std((data['Aoy_W']+data['Aoy_E'])/2,axis=2
            acc['Aoy_C_min'] = np.min((data['Aoy_W']+data['Aoy_E'])/2,axis=2
            acc['Aoy_C_max'] = np.max((data['Aoy_W']+data['Aoy_E'])/2,axis=2
            acc['Aoy_C_max_by_std'] = acc['Aoy_C_max']/acc['Aoy_C_std']
            acc['Aoz_C_mean'] = np.mean((data['Aoz_W']+data['Aoz_E'])/2,axis
            acc['Aoz_C_std'] = np.std((data['Aoz_W']+data['Aoz_E'])/2,axis=2
            acc['Aoz_C_min'] = np.min((data['Aoz_W']+data['Aoz_E'])/2,axis=2
            acc['Aoz_C_max'] = np.max((data['Aoz_W']+data['Aoz_E'])/2,axis=2
            acc['Aoz_C_max_by_std'] = acc['Aoz_C_max']/acc['Aoz_C_std']
        if theta:
            acc['theta_mean'] = np.mean(np.rad2deg(np.arctan(((data['Aoz_W']
            acc['theta_std'] = np.std(np.rad2deg(np.arctan(((data['Aoz_W'] -
            acc['theta_min'] = np.min(np.rad2deg(np.arctan(((data['Aoz_W'] -
            acc['theta_max'] = np.max(np.rad2deg(np.arctan(((data['Aoz_W'] -
            acc['theta_max_by_std'] = acc['theta_C_max']/acc['theta_C_std']
       if T:
            weather['T_mean'] = np.mean(data['T'],axis=1)
            weather['T_std'] = np.std(data['T'],axis=1)
            weather['T_min'] = np.min(data['T'],axis=1)
            weather['T_max'] = np.max(data['T'],axis=1)
        if P:
            weather['P_mean'] = np.mean(data['P'],axis=1)
            weather['P_std'] = np.std(data['P'],axis=1)
            weather['P_min'] = np.min(data['P'],axis=1)
            weather['P_max'] = np.max(data['P'],axis=1)
        if Hum:
            weather['Hum_mean'] = np.mean(data['Hum'],axis=1)
            weather['Hum_std'] = np.std(data['Hum'],axis=1)
            weather['Hum_min'] = np.min(data['Hum'],axis=1)
            weather['Hum_max'] = np.max(data['Hum'],axis=1)
   if Turb:
       if H:
            anemo['H_turb'] = anemo['H_std']/np.sqrt(np.square(anemo['H_mean
        if W:
            anemo['W_turb'] = np.abs(anemo['W_std']/np.sqrt(np.square(anemo[
        if Vx:
            anemo['Vx_turb'] = np.abs(anemo['Vx_std']/np.sqrt(np.square(anem
        if Vy:
            anemo['Vy_turb'] = np.abs(anemo['Vy_std']/np.sqrt(np.square(anem
if Upwind:
    # Create boolean arrays determening if a sensor is up- or downwind
    # at each datapoint, depending on direction measurement.
   anemo['Upwind'] = np.zeros(anemo_shape)
   for ind,anemo_name in enumerate(anemo_names):
        if anemo_name.endswith('W') or anemo_name.endswith('Wb') or anemo_na
            anemo['Upwind'][ind] = np.where(anemo['Dir_mean'][ind]>=180,1,0)
        elif anemo_name.endswith('E') or anemo_name.endswith('Eb') or anemo_
            anemo['Upwind'][ind] = np.where(anemo['Dir_mean'][ind]<180,1,0)</pre>
   anemo['Downwind'] = (~anemo['Upwind'].astype(bool)).astype(int)
if Hanger_num or y_pos:
    anemo['Hanger_num'] = np.zeros(anemo_shape)
```

```
acc['Hanger_num'] = np.zeros(acc_shape)
        for ind,anemo_name in enumerate(anemo_names):
            if anemo_name.startswith('H'):
                anemo['Hanger_num'][ind] = np.repeat(int(anemo_name[1:3]),anemo_
            elif anemo name.startswith('S'):
                anemo['Hanger_num'][ind] = np.repeat(int(self.n_hangers+1),anemo
        for ind,acc_name in enumerate(acc_names):
            if acc name.startswith('H'):
                acc['Hanger_num'][ind] = np.repeat(int(acc_name[1:3]),acc_shape[
            elif acc_name.startswith('S'):
                acc['Hanger_num'][ind] = np.repeat(int(self.n_hangers+1),acc_sha
    if y_pos:
        anemo['y pos'] = np.where(anemo['Hanger num']==0,self.tower dist,np.wher
        acc['y_pos'] = np.where(acc['Hanger_num']==0,self.tower_dist,np.where(action)
    if WestEast:
        anemo['West'] = np.zeros(anemo_shape)
        anemo['East'] = np.zeros(anemo_shape)
        for ind,anemo_name in enumerate(anemo_names):
            if anemo_name.endswith('W') or anemo_name.endswith('Wt') or anemo_na
                anemo['West'][ind] = np.repeat(True, anemo_shape[1])
                anemo['East'][ind] = np.repeat(False, anemo_shape[1])
            elif anemo_name.endswith('E') or anemo_name.endswith('Et') or anemo_
                anemo['West'][ind] = np.repeat(False,anemo_shape[1])
                anemo['East'][ind] = np.repeat(True,anemo_shape[1])
            else: # Assume West for sensors without declaration as they might be
                anemo['West'][ind] = np.repeat(True, anemo_shape[1])
                anemo['East'][ind] = np.repeat(False,anemo_shape[1])
        # Not applicable for accelerometers.
        acc['West'] = np.zeros(acc shape)
        acc['East'] = np.zeros(acc_shape)
    if TopBottom:
        anemo['Top'] = np.zeros(anemo_shape)
        anemo['Bottom'] = np.zeros(anemo_shape)
        for ind,anemo_name in enumerate(anemo_names):
            if anemo_name.endswith('Wb') or anemo_name.endswith('Eb') or anemo_n
                anemo['Top'][ind] = np.repeat(False,anemo_shape[1])
                anemo['Bottom'][ind] = np.repeat(True, anemo_shape[1])
            {\bf elif} \ ane {\bf mo\_name.ends} \\ {\bf with('Wt')} \ {\bf or} \ ane {\bf mo\_name.ends} \\ {\bf with('Et'):} \\
                anemo['Top'][ind] = np.repeat(True,anemo_shape[1])
                anemo['Bottom'][ind] = np.repeat(False,anemo_shape[1])
            else: # Assume Bottom for sensors without declaration as they might
                anemo['Top'][ind] = np.repeat(False,anemo_shape[1])
                anemo['Bottom'][ind] = np.repeat(True,anemo_shape[1])
        # Not applicable for accelerometers.
        acc['Top'] = np.zeros(acc shape)
        acc['Bottom'] = np.zeros(acc shape)
    if delete_data_after_import:
        # Delete original data after import to free up memory.
        del data
        gc.collect()
    return anemo names, acc names, time array, t array, anemo, acc, weather
def define units(self,accs in SI units=True):
    """Method to convert units and define units of all measurements in a diction
    Parameters
    accs_in_SI_units : bool, default True
```

```
0.00
    self.units = {}
    for key in self.anemo.keys():
        if key.startswith('H_') or key.startswith('W_') or key.startswith('Vx_')
            self.units[key]='[m/s]'
        elif key.startswith('Dir_') or key.startswith('AOA_') or key.startswith(
    self.units[key]='[°]'
        elif key.startswith('Tv_'):
            self.units[key]='[°C]'
        elif key.startswith('Upwind') or key.startswith('Downwind') or key.start
            self.units[key]=''
        elif key.startswith('y_pos'):
            self.units[key]='[m]'
        if key.endswith('_turb'):
            self.units[key]=''
    for key in self.weather.keys():
        if key.startswith('T'):
            self.units[key]='[°C]'
        elif key.startswith('P'):
            self.units[key]='[hPa]'
        elif key.startswith('Hum'):
            self.units[key]='[%]'
    for key in self.acc.keys():
        if key.startswith('Ao') and not key.endswith('_by_std'):
            if accs_in_SI_units:
                if self.acc unit == 'µG':
                    self.acc[key] = self.acc[key]*(1e-6*self.g)
                self.units[key]='[m s$^{-2}$]'
            else:
                if self.acc_unit == 'SI':
                    self.acc[key] = self.acc[key]/(1e-6*self.g)
                self.units[key]='[μG]'
        elif key.startswith('theta') and not key.endswith('_by_std'):
            self.units[key]='[° s$^{-2}$]'
        elif key.endswith('_by_std'):
            self.units[key]='
    if accs_in_SI_units:
        self.acc_unit = 'SI'
    else:
        self.acc\_unit = '\mu G'
def load data(self,print data structure=False,delete data after import=True,igno
    """Wrapper-method to import and combine multiple days of data using `convert
    Convert Lysefjord Bridge dataExtracted.mat files imported via `scipy.io.load
    Parameters
    print data structure : bool, default False
        Print the structure of the original data. Primarily used for developemen
    delete_data_after_import : bool, default True
        Delete original data from memory after import to free up memory
    ignore nans : bool, default True
        Ignores nans when calculating mean, std, min and max, using the remainin
    rename_H20_acc : bool, default True
        Rename accelerometers H20 to H24, as there seems to be a systematic erro
    replace_invalid : bool, default True
```

Whether to have measurements from accelerometers in m/s (SI-unit) or μG

```
Replace invalid sensor readings (outside of technical sensor range) with
    full_detail : bool, default False
       Keep full detail of data, sampled at 50Hz instead of resampling to every
   H ... TopBottom : bool, default True
       Select which part of the data should be imported or generated during imp
    See Also
    `convert MATLAB`
    `define_units`
    # Initialize with data of the first day in the list of file_names.
    print('Day',1,':',self.file_names[0][:-4][14:])
    temp data = scipy.io.loadmat(self.file path+self.file names[0])
    if print_data_structure:
        print(temp_data)
    self.anemo names, self.acc names, self.time array, self.t array, self.anemo,
    del temp_data
    gc.collect()
    # Batch-processing of further days of data, if any,
    # with temporary variables being created for each day
    # and deleted afterwards to free up memory for processing of the next day.
    for day in range(1,len(self.file_names)):
       print('Day',day+1,':',self.file_names[day][:-4][14:])
        temp_data = scipy.io.loadmat(self.file_path+self.file_names[day])
       temp_anemo_names, temp_acc_names, temp_time_array, temp_t_array, temp_an
       del temp_data
       gc.collect()
       anemo names, ind = np.unique(np.append(self.anemo names, temp anemo names)
       self.anemo_names = anemo_names[np.argsort(ind)]
       acc_names,ind = np.unique(np.append(self.acc_names,temp_acc_names), retu
       self.acc_names = acc_names[np.argsort(ind)]
       for key in temp_anemo.keys():
            if key in self.anemo.keys():
                self.anemo[key] = np.hstack((self.anemo[key],temp anemo[key]))
            else:
                self.anemo[key] = np.hstack((np.zeros_like(self.time_array),temp
       for key in temp_acc.keys():
            if key in self.acc.keys():
                self.acc[key] = np.hstack((self.acc[key],temp_acc[key]))
            else:
                self.acc[key] = np.hstack((np.zeros like(self.time array),temp a
        for key in temp_weather.keys():
            if key in self.weather.keys():
                self.weather[key] = np.hstack((self.weather[key],temp_weather[key])
            else:
                self.weather[key] = np.hstack((np.zeros_like(self.time_array),te
        self.time array = np.hstack((self.time array, temp time array))
        self.t array = np.hstack((self.t array, temp t array))
       del temp_anemo_names, temp_acc_names, temp_time_array, temp_t_array, tem
        gc.collect()
    self.define_units(accs_in_SI_units)
# Processing
```

```
def find_invalid_sensors(self,data,threshold=0.5,lp_cutoff=np.inf,hp_cutoff=-np.
    """Helper-method for data cleaning finding invalid sensors in `data`.
   Parameters
    _____
    data : array_like
       Measurement data in which invalid sensors are to be found.
    threshold: float, default 0.5
        Fraction of data from a specific sensor that is allowed to be invalid be
    lp_cutoff : float or int, default np.inf
       Lowpass cutoff point: If a value is higher than `lp_cutoff`it is interpr
   hp_cutoff : float or int, default -np.inf
       Highpass cutoff point: If a value is lower than `hp_cutoff`it is interpr
    zeros : bool, default False
       Zeros are interpreted as invalid values.
    nans : bool, default True
       nans are interpreted as invalid values.
    lowpass : bool, default False
       Values above `lp_cutoff` are interpreted as invalid values.
   highpass : bool, default False
       Values below `hp_cutoff` are interpreted as invalid values.
   Returns
    invalid_sensor_id : array_like
       ids of invalid sensors.
   ok_sensor_id : array_like
       ids of ok sensors.
   See Also
    `find_common_ok_sensors`
    `remove_invalid_sensors`
   invalid_sensor_id = np.array([])
    if zeros:
       potentially_invalid_sensors, count = np.unique(np.where(data==0)[0],retu
        invalid_sensor_id = np.unique(np.append(invalid_sensor_id,potentially_in
    if nans:
        potentially_invalid_sensors, count = np.unique(np.where(np.isnan(data))[
        invalid_sensor_id = np.unique(np.append(invalid_sensor_id,potentially_in
    if lowpass:
        potentially_invalid_sensors, count = np.unique(np.where(data>lp_cutoff)[
        invalid_sensor_id = np.unique(np.append(invalid_sensor_id,potentially_in
    if highpass:
        potentially_invalid_sensors, count = np.unique(np.where(data<hp_cutoff)[</pre>
        invalid sensor id = np.unique(np.append(invalid sensor id,potentially in
    invalid_sensor_id = np.array([int(i) for i in invalid_sensor_id]).astype(int
    ok_sensor_id = np.array(list(set(np.arange(data.shape[0]))-(set(invalid_sens
    return invalid_sensor_id, ok_sensor_id
def find common ok sensors(self,ok sensor ids s1,ok sensor ids s2):
    """Method to find common ok sensors.
   Usefull for preparation of post-processing.
   Parameters
    -----
```

```
ok_sensor_ids_s1 : list or array_like of ints
        ids of ok sensors from measurement type 1.
    ok_sensor_ids_s2 : list or array_like of ints
        ids of ok sensors from measurement type 2.
    Returns
    _____
    common sensor id : list
       Sensor ids of ok sensors in both sets of measurements.
    s1_ind : list
       Sensor indices of common ok sensors for measurement type 1.
   s2_ind : list
       Sensor indices of common ok sensors for measurement type 2.
   See Also
    `find invalid sensors`
    `get_ok_sensor_ind`
   s1_ind = []
   for ind, sensor_id in enumerate(ok_sensor_ids_s1):
        if sensor_id in ok_sensor_ids_s2:
            s1_ind.append(ind)
    s2_ind = []
    for ind, sensor_id in enumerate(ok_sensor_ids_s2):
        if sensor_id in ok_sensor_ids_s1:
            s2_ind.append(ind)
    common_sensor_id = list(set(set(ok_sensor_ids_s1) & set(ok_sensor_ids_s2)))
    return common_sensor_id, s1_ind, s2_ind
def remove_invalid_sensors(self,data,ok_sensor_id):
    """Helper-method for data cleaning removing invalid sensors from `data`.
   Parameters
    _____
    data : array_like
       Measurement data in which invalid sensors are to be removed.
    ok_sensor_id : array_like
        Index of ok sensors in measurement data.
   Returns
    data_cleaned : array_like
        `data` without invalid sensors.
   See Also
    _____
    `find invalid sensors`
   `find_common_ok_sensors`
    if len(ok_sensor_id)>0:
        data_cleaned = data[ok_sensor_id]
       data_cleaned = []
    return data cleaned
def idx data(self,data,nans=False,zeros=False,lp cutoff=np.inf,hp cutoff=-np.inf
    """Helper-method indexing data.
   Parameters
    data: array like
       Measurement data in which data is to be indexed.
```

```
lp_cutoff : float or int, default np.inf
        Lowpass cutoff point: If a value is higher than `lp_cutoff`it is indexed
   hp_cutoff : float or int, default -np.inf
       Highpass cutoff point: If a value is lower than `lh_cutoff`it is indexed
    nans : bool, default False
       Nans are indexed.
    zeros : bool, default False
       Zeros are indexed.
    lowpass : bool, default False
       Values above `lp_cutoff` are indexed.
   highpass : bool, default False
       Values below `hp_cutoff` are indexed.
    Returns
    _____
    idx : array_like
       Indices of data.
    if len(data):
       idx = np.array([])
       if nans:
            idx = np.union1d(idx,np.argwhere(np.any(np.isnan(data[..., :]), axis
       if zeros:
            idx = np.union1d(idx,np.argwhere(np.any(data[..., :] == 0, axis=0)))
       if lowpass:
            idx = np.union1d(idx,np.argwhere(np.any(data[..., :] > lp_cutoff, ax
       if highpass:
            idx = np.union1d(idx,np.argwhere(np.any(data[..., :] < hp_cutoff, ax
        idx = np.unique(idx).astype(int)
       return idx
        raise ValueError('Data is empty.')
def clean_data(self,delete_original_data=False,threshold=0.5,detailed_report=Fal
    """Wrapper-method for data cleaning using `find_invalid_sensors`, `remove_in
   Notes
    If `remove_invalid` is `True` in `load_data`, `clean_data` might not find mo
   Parameters
    delete_original_data : bool, default False
       Delete the original (un-cleaned) `data` to free up memory.
    threshold : float, default 0.5
       Fraction of data from a specific sensor that is allowed to be invalid be
    detailed_report : bool, default False
       Print out a detailed report of the data cleaning. Used for de-bugging an
   See Also
    `find_invalid_sensors`
    `find_common_ok_sensors`
    `get_ok_sensor_ind`
    `remove_invalid_sensors`
    `idx_data`
   # Initialize dicts for cleaned data.
    self.anemo cleaned = {}
    self.anemo invalid sensor id = {}
    self.anemo_ok_sensor_id = {}
    self.acc_cleaned = {}
    self.acc_invalid_sensor_id = {}
    self.acc_ok_sensor_id = {}
```

```
self.weather_cleaned = {}
if self.acc_unit == 'µG':
    acc_thresh_unit_fact = 1e6
else:
    acc thresh unit fact = self.g
# Anemometers
for key in self.anemo.keys():
   # Find invalid sensors in each key.
   if key.startswith('H_m'):
        self.anemo_invalid_sensor_id[key], self.anemo_ok_sensor_id[key] = se
   elif key.startswith('Vx_m') or key.startswith('Vy_m') or key.startswith(
        self.anemo_invalid_sensor_id[key], self.anemo_ok_sensor_id[key] = se
   elif key.startswith('Dir m'):
        self.anemo_invalid_sensor_id[key], self.anemo_ok_sensor_id[key] = se
   elif key.endswith('_std') or key.endswith('_turb'):
        self.anemo_invalid_sensor_id[key], self.anemo_ok_sensor_id[key] = se
   else:
        self.anemo_invalid_sensor_id[key], self.anemo_ok_sensor_id[key] = se
   # Combine invalid sensors from keys of same sensor.
   if not key.endswith('_turb'): # Not applicable for turbulence calculatio
        if key[:key.find('_')] not in self.anemo_invalid_sensor_id:
            self.anemo_invalid_sensor_id[key[:key.find('_')]] = self.anemo_i
       else:
            self.anemo_invalid_sensor_id[key[:key.find('_')]] = np.unique(np
    if len(self.anemo_ok_sensor_id[key]) == 0:
        print(key, 'all sensors deemed invalid')
       try:
            del self.anemo cleaned[key], self.anemo invalid sensor id[key],
        except:
            print(key, 'already deleted')
   elif len(self.anemo_invalid_sensor_id[key]) == 0:
        if detailed report:
            print(key, 'all sensors deemed ok')
   else:
        if detailed_report:
            print(key, 'ok sensors:', self.anemo_names[self.anemo_ok_sensor_id
            print(key,'invalid sensors:',self.anemo names[self.anemo invalid
# Remove invalid sensors for all keys of same sensor.
for key in self.anemo.keys():
    self.anemo_invalid_sensor_id[key] = self.anemo_invalid_sensor_id[key[:ke
   if key.startswith('AOA') or key.endswith('_turb'): # AOA and turbulence
        self.anemo invalid sensor id[key] = np.unique(np.append(self.anemo i
        self.anemo invalid sensor id[key] = np.unique(np.append(self.anemo i
   elif key.startswith('Vx') or key.startswith('Vy') or key.startswith('Dir
        self.anemo invalid sensor id[key] = np.unique(np.append(self.anemo i
    self.anemo_ok_sensor_id[key] = np.array(list(set(np.arange(self.anemo[ke
   self.anemo_cleaned[key] = self.remove_invalid_sensors(self.anemo[key],se
   if len(self.anemo ok sensor id[key]) == 0:
        print(key, 'all sensors deemed invalid')
        try:
            del self.anemo_cleaned[key], self.anemo_invalid_sensor_id[key],
            print(key, 'already deleted')
   elif len(self.anemo_invalid_sensor_id[key]) == 0:
        if detailed report:
            print(key, 'all sensors deemed ok')
```

```
else:
        if detailed report:
            print(key, 'ok sensors:', self.anemo_names[self.anemo_ok_sensor_id
            print(key, 'invalid sensors:', self.anemo_names[self.anemo_invalid
# Accelerometers
for key in self.acc.keys():
    # Find invalid sensors in each key.
   if key.endswith('_max'):
        if key.startswith('Aoz_'):
            self.acc_invalid_sensor_id[key], self.acc_ok_sensor_id[key] = se
        elif key.startswith('Ao'):
            self.acc_invalid_sensor_id[key], self.acc_ok_sensor_id[key] = se
            self.acc_invalid_sensor_id[key], self.acc_ok_sensor_id[key] = se
   elif key.endswith('_min'):
        if key.startswith('Aoz_'):
            self.acc_invalid_sensor_id[key], self.acc_ok_sensor_id[key] = se
        elif key.startswith('Ao'):
            self.acc_invalid_sensor_id[key], self.acc_ok_sensor_id[key] = se
       else:
            self.acc_invalid_sensor_id[key], self.acc_ok_sensor_id[key] = se
   else:
        self.acc_invalid_sensor_id[key], self.acc_ok_sensor_id[key] = self.f
   # Combine invalid sensors from keys of same sensor.
   if key.startswith('Aox_W') or key.startswith('Aoy_W') or key.startswith(
        if 'W_all' not in self.acc_invalid_sensor_id:
            self.acc_invalid_sensor_id['W_all'] = self.acc_invalid_sensor_id
       else:
            self.acc invalid sensor id['W all'] = np.unique(np.append(self.a
   elif key.startswith('Aox_E') or key.startswith('Aoy_E') or key.startswit
        if 'E_all' not in self.acc_invalid_sensor_id:
            self.acc_invalid_sensor_id['E_all'] = self.acc_invalid_sensor_id
       else:
           self.acc_invalid_sensor_id['E_all'] = np.unique(np.append(self.a
   elif key.startswith('Aox_C') or key.startswith('Aoy_C') or key.startswit
        if 'C_all' not in self.acc_invalid_sensor_id:
            self.acc invalid sensor id['C all'] = self.acc invalid sensor id
            self.acc_invalid_sensor_id['C_all'] = np.unique(np.append(self.a
   if len(self.acc ok sensor id[key]) == 0:
       print(key, 'all sensors deemed invalid')
        try:
            del self.acc_cleaned[key], self.acc_invalid_sensor_id[key], self
        except:
            print(key, 'already deleted')
   elif len(self.acc invalid sensor id[key]) == 0:
        if detailed_report:
            print(key, 'all sensors deemed ok')
   else:
       if detailed report:
            print(key, 'ok sensors:', self.acc_names[self.acc_ok_sensor_id[key
            print(key, 'invalid sensors:', self.acc_names[self.acc_invalid_sen
# Remove invalid sensors for all keys of same sensor.
for key in self.acc.keys():
   if key.startswith('Aox_W') or key.startswith('Aoy_W') or key.startswith(
        self.acc invalid sensor id[key] = self.acc invalid sensor id['W all'
   elif key.startswith('Aox_E') or key.startswith('Aoy_E') or key.startswit
        self.acc_invalid_sensor_id[key] = self.acc_invalid_sensor_id['E_all'
   elif key.startswith('Aox_C') or key.startswith('Aoy_C') or key.startswit
        self.acc_invalid_sensor_id[key] = self.acc_invalid_sensor_id['C_all'
```

```
if key.startswith('Aox_C'): #A ox_C dependent on Aox_W and Aox_E.
        self.acc invalid sensor id[key] = np.unique(np.append(self.acc inval
        self.acc_invalid_sensor_id[key] = np.unique(np.append(self.acc_inval
   elif key.startswith('Aoy C'): # Aoy C dependent on Aoy W and Aoy E.
        self.acc_invalid_sensor_id[key] = np.unique(np.append(self.acc_inval)
        self.acc_invalid_sensor_id[key] = np.unique(np.append(self.acc_inval
    if key.startswith('Aoz C') or key.startswith('theta'): # Aoz C and theta
        self.acc_invalid_sensor_id[key] = np.unique(np.append(self.acc_inval)
        self.acc_invalid_sensor_id[key] = np.unique(np.append(self.acc_inval
   self.acc_ok_sensor_id[key] = np.array(list(set(np.arange(self.acc[key].s
   self.acc_cleaned[key] = self.remove_invalid_sensors(self.acc[key],self.a
   if len(self.acc_ok_sensor_id[key]) == 0:
        print(key, 'all sensors deemed invalid')
        try:
            del self.acc_cleaned[key], self.acc_invalid_sensor_id[key], self
        except:
            print(key, 'already deleted')
   elif len(self.acc_invalid_sensor_id[key]) == 0:
        if detailed report:
            print(key, 'all sensors deemed ok')
   else:
        if detailed_report:
            print(key, 'ok sensors:', self.acc_names[self.acc_ok_sensor_id[key
            print(key, 'invalid sensors:', self.acc_names[self.acc_invalid_sen
# Find outliers in remaining sensors.
idx = np.array([])
# Anemometers
for key in self.anemo_cleaned.keys():
   if key.startswith('Dir_m'):
        idx = np.union1d(idx,self.idx_data(self.anemo_cleaned[key],nans=True
   elif key.startswith('H_m'):
        idx = np.union1d(idx,self.idx_data(self.anemo_cleaned[key],nans=True
   elif key.startswith('Vx_m') or key.startswith('Vy_m') or key.startswith(
        idx = np.union1d(idx,self.idx data(self.anemo cleaned[key],nans=True
   elif key.endswith('_std') or key.endswith('_turb'):
        idx = np.union1d(idx,self.idx data(self.anemo cleaned[key],nans=True
   else:
        idx = np.union1d(idx,self.idx_data(self.anemo_cleaned[key],nans=True
   if detailed report:
       print(key,' cummulative data loss:',np.round(100*(len(idx)/self.time
# Accelerometers
for key in self.acc cleaned.keys():
   if key.endswith(' max'):
        if key.startswith('Aoz_'):
            idx = np.union1d(idx,self.idx data(self.acc cleaned[key],nans=Tr
        elif key.startswith('Ao'):
            idx = np.union1d(idx,self.idx_data(self.acc_cleaned[key],nans=Tr
            idx = np.union1d(idx,self.idx_data(self.acc_cleaned[key],nans=Tr
   elif key.endswith(' min'):
        if key.startswith('Aoz '):
            idx = np.union1d(idx,self.idx data(self.acc cleaned[key],nans=Tr
        elif key.startswith('Ao'):
           idx = np.union1d(idx,self.idx data(self.acc cleaned[key],nans=Tr
       else:
            idx = np.union1d(idx,self.idx_data(self.acc_cleaned[key],nans=Tr
   else:
        idx = np.union1d(idx,self.idx_data(self.acc_cleaned[key],nans=True,z
```

```
idx = idx.astype(int)
    # Remove outliers from all sensors.
    self.time_array_cleaned = np.delete(self.time_array,idx,axis=0)
    self.t array cleaned = np.delete(self.t array,idx,axis=0)
    for key in self.weather.keys():
        self.weather_cleaned[key] = np.delete(self.weather[key],idx,axis=0)
    for key in self.anemo_cleaned.keys():
        self.anemo_cleaned[key] = np.delete(self.anemo_cleaned[key],idx,axis=1)
    for key in self.acc cleaned.keys():
        self.acc cleaned[key] = np.delete(self.acc cleaned[key],idx,axis=1)
    print('Total data loss:',np.round(100*(1-self.time_array_cleaned.shape[0]/se
    # Delete original data after cleaning to free up memory.
    if delete_original_data:
       del self.anemo, self.acc, self.weather, self.time_array, self.t_array, i
       gc.collect()
def get_ok_sensor_ind(self,sensor_names=[],sensor_type='anemo',key='H_mean'):
    ""Method to get sensor indices of ok sensors for a given `key`.
   Parameters
    sensor_names : list or str, optional
        List of sensor names to find in ok sensors of type `sensor_type` for `ke
   sensor_type : {'anemo', 'acc'}
       Type of the sensors.
   key : str, default 'H_mean'
       Key of measurement type from sensor.
   Returns
    _____
    s ind : list
       Sensor indices of ok sensors for a given `key`.
   Notes
    Requires `anemo ok sensor id` or `acc ok sensor id`.
    s_{ind} = []
    if len(sensor_names):
        if type(sensor_names)!=list:
            if type(sensor_names)==str:
                sensor names=[sensor names]
                raise TypeError('sensor_names must be list or str.')
        if sensor type == 'anemo':
            for sensor in sensor_names:
                if sensor in self.anemo_names[self.anemo_ok_sensor_id[key]]:
                    s_ind.append(np.where(self.anemo_names[self.anemo_ok_sensor_
                else:
                    raise ValueError(sensor+' not in ok anemometers of key '+key
       elif sensor type == 'acc':
            for sensor in sensor_names:
                if sensor in self.acc_names[self.acc_ok_sensor_id[key]]:
                    s ind.append(np.where(self.acc names[self.acc ok sensor id[k
                else:
                    raise ValueError(sensor+' not in ok accelerometers of key '+
        else:
            raise ValueError('sensor_type must be "anemo" or "acc".')
```

```
else:
        raise ValueError('No sensor_names provided')
    return(s_ind)
def find traffic(self,traffic thresh=8,cleaned=True):
    """Method to find traffic dominated vibrations in accelerometers data using
    Parameters
   traffic_thresh : float, default 8
       Threshold for Aoz_C_max_by_std to use for filtering. Recommended 6 ... 8
   cleaned : bool, default True
       Create the array `traffic cleaned` for the cleaned data.
   Notes
    ____
    Requires `acc['Aoz_C_max_by_std']`.
    if 'Aoz_C_max_by_std' in self.acc.keys():
        self.traffic = np.zeros(self.time_array.shape[0])
        idx = self.idx_data(self.acc['Aoz_C_max_by_std'],zeros=False,lp_cutoff=t
        self.traffic[idx] = 1
       if cleaned:
            self.traffic_cleaned = np.zeros(self.time_array_cleaned.shape[0])
            idx_cleaned = self.idx_data(self.acc_cleaned['Aoz_C_max_by_std'],zer
            self.traffic_cleaned[idx_cleaned] = 1
    else:
        raise KeyError('find_traffic requires Aoz_C_max_by_std.')
def feature time(self,cleaned=True):
    """Method to create time arrays in days, hours, minutes and seconds, startin
    Parameters
    cleaned : bool, default True
        Create the time arrays for the cleaned data aswell.
    self.days = self.time array-self.time array[0]
    self.hours = self.days*24
    self.minutes = self.hours*60
    self.seconds = self.minutes*60
    if cleaned:
        self.days_cleaned = self.time_array_cleaned-self.time_array_cleaned[0]
        self.hours_cleaned = self.days_cleaned*24
        self.minutes_cleaned = self.hours_cleaned*60
        self.seconds cleaned = self.minutes cleaned*60
def filter_data(self,data,prior_idxs=None,nans=False,zeros=False,lp_cutoff=np.in
    """Method to filter data.
   Parameters
    -----
    data: array_like
       Measurement data in which data is to be indexed.
    prior idxs : array like, optional
        Indices of prior filterings with which new indices will be combined.
    lp cutoff : float or int, default np.inf
        Lowpass cutoff point: If a value is lower than `lp cutoff`it is indexed
    hp_cutoff : float or int, default -np.inf
       Highpass cutoff point: If a value is higher than `lh_cutoff`it is indexe
    nans : bool, default False
       Nans are indexed.
```

```
zeros : bool, default False
    Zeros are indexed.
lowpass : bool, default False
    Values above `lp_cutoff` are indexed.
highpass : bool, default False
    Values below `hp_cutoff` are indexed.
method : {'all','any'}, default 'all'
    Method to use for filtering. Index a datapoint when the filtercondition
mode : {'and','or'}, default 'and'
    Mode in which indices are to be combined. 'and' if all filterconditions
prior_mode : {'and','or'}, default 'and'
    Mode in which indices are to be combined with indices of prior filtering
Returns
_____
idx : array_like
    Indices of filtered data.
See Also
_____
`idx_data`
if len(data):
    if mode == 'or':
        idx = np.array([])
    elif mode == 'and':
        idx = np.arange(np.shape(data)[-1])
    else:
        if type(mode)==str:
            raise ValueError('Incompatible mode. mode needs to be "and" or "
            raise TypeError('mode needs to be a string, either "and" or "or"
    if len(np.shape(data))==1:
        if mode == 'or':
            if nans:
                idx = np.union1d(idx,np.where(np.isnan(data)))
            if zeros:
                idx = np.union1d(idx,np.where(data[..., :] == 0))
            if lowpass:
                idx = np.union1d(idx,np.where(data[..., :] < lp_cutoff))</pre>
            if highpass:
                idx = np.union1d(idx,np.where(data[..., :] > hp_cutoff))
        elif mode == 'and':
            if nans:
                idx = np.intersect1d(idx,np.where(np.isnan(data)))
            if zeros:
                idx = np.intersect1d(idx,np.where(data[..., :] == 0))
            if lowpass:
                idx = np.intersect1d(idx,np.where(data[..., :] < lp_cutoff))</pre>
                idx = np.intersect1d(idx,np.where(data[..., :] > hp_cutoff))
    else:
        if method == 'all':
            if mode == 'or':
                if nans:
                    idx = np.union1d(idx,np.argwhere(np.all(np.isnan(data[...
                if zeros:
                    idx = np.union1d(idx,np.argwhere(np.all(data[..., :] ==
                if lowpass:
                    idx = np.union1d(idx,np.argwhere(np.all(data[..., :] < 1</pre>
                if highpass:
                    idx = np.union1d(idx,np.argwhere(np.all(data[..., :] > h
            elif mode == 'and':
```

```
idx = np.intersect1d(idx,np.argwhere(np.all(np.isnan(dat
                    if zeros:
                        idx = np.intersect1d(idx,np.argwhere(np.all(data[..., :]
                    if lowpass:
                        idx = np.intersect1d(idx,np.argwhere(np.all(data[..., :]
                    if highpass:
                        idx = np.intersect1d(idx,np.argwhere(np.all(data[..., :]
            elif method == 'any':
                if mode == 'or':
                    if nans:
                        idx = np.union1d(idx,np.argwhere(np.any(np.isnan(data[...
                        idx = np.union1d(idx,np.argwhere(np.any(data[..., :] ==
                    if lowpass:
                        idx = np.union1d(idx,np.argwhere(np.any(data[..., :] < 1</pre>
                    if highpass:
                        idx = np.union1d(idx,np.argwhere(np.any(data[..., :] > h
                elif mode == 'and':
                    if nans:
                        idx = np.intersect1d(idx,np.argwhere(np.any(np.isnan(dat
                    if zeros:
                        idx = np.intersect1d(idx,np.argwhere(np.any(data[..., :]
                    if lowpass:
                        idx = np.intersect1d(idx,np.argwhere(np.any(data[..., :]
                    if highpass:
                        idx = np.intersect1d(idx,np.argwhere(np.any(data[..., :]
            else:
                if type(method)==str:
                    raise ValueError('Incompatible method. method needs to be "a
                else:
                    raise TypeError('method needs to be a string, either "any" o
        if type(prior_idxs)!=type(None):
            if prior_mode == 'or':
                idx = np.union1d(idx, np.array(prior_idxs).astype(int))
            elif prior_mode == 'and':
                idx = np.intersect1d(idx,np.array(prior_idxs).astype(int))
                if type(prior_mode)==str:
                    raise ValueError('Incompatible prior mode. prior mode needs
                    raise TypeError('prior_mode needs to be a string, either "an
        idx = np.unique(idx).astype(int)
        return idx
    else:
        raise ValueError('data is empty.')
# Post-processing
def bridge_layout(self,b_anemo_height_above_deck=6,t_anemo_height_above_deck=10,
    """Method to create a bridge layout showing the sensor positions for the sel
    Parameters
    _____
    b anemo height above deck : float, default 6
       Height above the bridge deck in meters, at which the bottom row anemomet
    t anemo height above deck : float, default 10
       Height above the bridge deck in meters, at which the top row anemometers
    d_acc_height_above_deck : float, default -0.3
       Default height above the bridge deck in meters, at which the acceleromet
    top_view : bool, default True
       Create a top-view layout of the bridge.
```

if nans:

```
side_view : bool, default True
    Create a side-view layout of the bridge.
show_cables : bool, default True
    Show the main supporting cables of the brige.
show deck : bool, default True
    Show the deck of the brige.
show_girder : bool, default True
    Show the bridge girder.
show_hangers : bool, default True
    Show the hangers on which the deck is suspended.
show_towers : bool, default True
    Show the north- and south-tower of the bridge.
show COMs : bool, default False
    Show the center of mass for each element of the bridge model.
show_joints : bool, default False
    Show the joints between elements of the bridge model.
show_sensors : bool, default True
    Show the locations of anemometers and accelerometers that were active on
show_water : bool, default True
    Show the waterline in the side-view layout.
invert_xaxis : bool, default True
    Invert the x-axis to start at hanger 1 (at the north tower) from the lef
title_suffix : str, optional
   Add a suffix to the title.
save : bool, default False:
    Save the plot in ../images/. Note: Requires the prior existence of that
# Calculate y_{-} and z_{-} positions of cables and deck.
y_ = np.zeros(self.n_hangers+2)
y_[1:-1] = np.linspace(self.first_hanger_y_tower_dist,self.tower_dist-self.l
y [-1] = self.tower dist
z_cable = np.zeros_like(y_)
z_cable[0] = z_cable[-1] = self.h_towers
z_cable[len(z_cable)//2] = self.h_towers - self.sag
def parabola(x,a,h,k):
    y = a*np.square(x-h)+k
    return y
h cable = self.tower dist/2
k_cable = self.h_towers - self.sag
popt_cable, pcov_cable = scipy.optimize.curve_fit(parabola,[y_[0],y_[(self.n
z_cable = parabola(y_,popt_cable[0],h_cable,k_cable)
z_deck = np.zeros_like(z_cable)
z_deck[(self.n_hangers+2)//2] = self.mid_span_deck_height
z deck[0] = self.tower 1 deck support height+self.girder height
z_deck[-1] = self.tower_2_deck_support_height+self.girder_height
h deck = y [(self.n hangers+2)//2]
k_deck = z_deck[(self.n_hangers+2)//2]
popt_deck, pcov_deck = scipy.optimize.curve_fit(parabola,[y_[0],y_[(self.n_h
z_deck = parabola(y_,popt_deck[0],popt_deck[1],popt_deck[2])
# Get sensor positions from sensor names.
anemo_hanger_num = np.zeros(len(self.anemo_names))
acc_hanger_num = np.zeros(len(self.acc_names))
x anemometer = np.zeros(len(self.anemo names))
anemo_height_above_deck = np.zeros(len(self.anemo_names))
acc_height_above_deck = np.zeros(len(self.acc_names))
for ind,anemo_name in enumerate(self.anemo_names):
```

```
if anemo_name.startswith('H'):
        anemo_hanger_num[ind] = int(anemo_name[1:3])
    elif anemo_name.startswith('N'):
        anemo_hanger_num[ind] = 0
        anemo_height_above_deck[ind] = self.h_towers-self.tower_2_deck suppo
        x_anemometer[ind] = -self.cable_x_dist/2
    elif anemo_name.startswith('S'):
        anemo_hanger_num[ind] = self.n_hangers+1
        anemo_height_above_deck[ind] = self.h_towers-self.tower_1_deck_suppo
        x_anemometer[ind] = -self.cable_x_dist/2
    if anemo_name.endswith('W') or anemo_name.endswith('Wb') or anemo_name.e
       x_anemometer[ind] = -self.cable_x_dist/2
   elif anemo_name.endswith('E') or anemo_name.endswith('Eb') or anemo_name
        x_anemometer[ind] = self.cable_x_dist/2
   if anemo_name.endswith('W') or anemo_name.endswith('Wb') or anemo_name.e
        anemo_height_above_deck[ind] = b_anemo_height_above_deck
    elif anemo_name.endswith('Wt') or anemo_name.endswith('Et'):
        anemo_height_above_deck[ind] = t_anemo_height_above_deck
for ind,acc_name in enumerate(self.acc_names):
   if acc_name.startswith('H'):
        acc_hanger_num[ind] = int(acc_name[1:3])
        acc_height_above_deck[ind] = d_acc_height_above_deck
   elif acc_name.startswith('N'):
        acc_hanger_num[ind] = 0
        acc_height_above_deck[ind] = self.h_towers-self.tower_2_deck_support
    elif acc_name.startswith('S'):
        acc_hanger_num[ind] = self.n_hangers+1
        acc_height_above_deck[ind] = self.h_towers-self.tower_1_deck_support
y anemometer = y [np.subtract(self.n hangers+1, anemo hanger num).astype(int
y_accelerometer = y_[np.subtract(self.n_hangers+1, acc_hanger_num).astype(in
z_anemometer = np.interp(y_anemometer,y_,z_deck) + anemo_height_above_deck
z_accelerometer = np.interp(y_accelerometer,y_,z_deck) + acc_height_above_de
# Calculate COMs, joint positions, lengths and masses.
hanger_COM = [y_[1:-1],(z_{cable}[1:-1]+z_{deck}[1:-1])/2]
hanger\_top\_joint = [y_[1:-1], z_cable[1:-1]]
hanger_bottom_joint = [y_[1:-1], z_deck[1:-1]]
hanger_length = z_cable[1:-1]-z_deck[1:-1]
hanger_mass = self.hanger_section_weight*hanger_length
cable_segment_COM = np.zeros((2,self.n_hangers+1))
cable_segment_length = np.zeros(self.n_hangers+1)
deck_segment_COM = np.zeros((2,self.n_hangers+1))
deck segment length = np.zeros(self.n hangers+1)
for ind in range(self.n_hangers+1):
    cable_segment_COM[0][ind] = (y_[ind+1]+y_[ind])/2
    cable_segment_COM[1][ind] = (z_cable[ind+1]+z_cable[ind])/2
    cable_segment_length[ind] = np.linalg.norm(x=[np.array([y_[ind+1],z_cabl
    deck_segment_COM[0][ind] = (y_[ind+1]+y_[ind])/2
    deck_segment_COM[1][ind] = ((z_deck[ind+1]-(self.girder_height/2))+(z_de
    deck_segment_length[ind] = np.linalg.norm(x=[np.array([y_[ind+1],z_deck[
cable_segment_south_joint = [y_[:-1],z_cable[:-1]]
cable_segment_north_joint = [y_[1:],z_cable[1:]]
cable_segment_mass = self.cable_section_weight*cable_segment_length
deck_segment_south_joint = [y_[:-1],z_deck[:-1]]
deck_segment_north_joint = [y_[1:],z_deck[1:]]
```

```
deck_segment_mass = self.girder_section_weight*deck_segment_length
tot_cable_length = np.sum(cable_segment_length)
tot_deck_length = np.sum(deck_segment_length)
tot cable mass = np.sum(cable segment mass)
tot_deck_mass = np.sum(deck_segment_mass)
# Create bridge Layout.
if top_view:
   plt.figure(figsize=(12,4))
   if show_cables:
       plt.plot(y_,np.repeat(self.cable_x_dist/2,len(y_)),'-',color='b',lab
        plt.plot(y_,np.repeat(-self.cable_x_dist/2,len(y_)),'-',color='g',la
   if show_deck:
        plt.plot(y_,np.repeat(self.deck_width/2,len(y_)),'-',color='dimgrey'
        plt.plot(y_,np.repeat(0,len(y_)),'--',color='dimgrey',label='centerl
        plt.plot(y_,np.repeat(-self.deck_width/2,len(y_)),'-',color='dimgrey
        plt.fill_between(y_,self.deck_width/2,-self.deck_width/2,color='ligh
   if show_girder:
        plt.plot(y_,np.repeat(self.girder_width/2,len(y_)),'--',color='darkg
        plt.plot(y_,np.repeat(-self.girder_width/2,len(y_)),'--',color='dark
   if show hangers:
        plt.plot(y_,np.repeat(self.cable_x_dist/2,len(y_)),'.',color='b',lab
       plt.plot(y_,np.repeat(-self.cable_x_dist/2,len(y_)),'.',color='g',la
   if show_towers:
        plt.plot([y_[0]],self.cable_x_dist/2,'d',ms=10,color='black',label='
        plt.plot([y [0]],-self.cable x dist/2,'d',ms=10,color='black')
        plt.plot([y_[-1]],self.cable_x_dist/2,'d',ms=10,color='red',label='N
       plt.plot([y_[-1]],-self.cable_x_dist/2,'d',ms=10,color='red')
   if show_COMs:
       plt.plot(hanger_COM[0],np.repeat(self.cable_x_dist/2,len(hanger_COM[
        plt.plot(hanger_COM[0],np.repeat(-self.cable_x_dist/2,len(hanger_COM
       plt.plot(cable_segment_COM[0],np.repeat(self.cable_x_dist/2,len(cabl
        plt.plot(cable_segment_COM[0],np.repeat(-self.cable_x_dist/2,len(cab
       plt.plot(deck_segment_COM[0],np.repeat(0,len(deck_segment_COM[0])),'
   if show joints:
       plt.plot(hanger_top_joint[0],np.repeat(self.cable_x_dist/2,len(hange
        plt.plot(hanger_top_joint[0],np.repeat(-self.cable_x_dist/2,len(hang
        plt.plot(hanger_bottom_joint[0],np.repeat(self.cable_x_dist/2,len(ha
        plt.plot(hanger_bottom_joint[0],np.repeat(-self.cable_x_dist/2,len(h
       plt.plot(cable segment south joint[0],np.repeat(self.cable x dist/2,
       plt.plot(cable_segment_south_joint[0],np.repeat(-self.cable_x_dist/2
       plt.plot(cable_segment_north_joint[0],np.repeat(self.cable_x_dist/2,
        plt.plot(cable segment north joint[0],np.repeat(-self.cable x dist/2
        plt.vlines(deck_segment_south_joint[0],-self.deck_width/2,self.deck_
        plt.vlines(deck_segment_north_joint[0],-self.deck_width/2,self.deck_
   if show sensors:
        plt.plot(y accelerometer,np.repeat(self.acc x dist from centerline,l
        plt.plot(y_accelerometer,np.repeat(-self.acc_x_dist_from_centerline,
        plt.plot(y_anemometer,x_anemometer,'^',ms=10,mec='black',color='gray
   if xticks h num:
       xtick_labels = list(np.arange(0,self.n_hangers+2,1))[::-1]
        xtick_labels[0] = 'S_Tower'
        xtick_labels[-1] = 'N_Tower'
```

```
plt.xticks(y_,xtick_labels)
       plt.xlabel('hanger number')
   else:
        plt.xticks(np.arange(0,self.tower_dist+10,10),np.arange(0,self.tower
       plt.xlabel('distance [m]')
   if invert xaxis:
       plt.xlim(self.tower_dist+1,-1)
   else:
       plt.xlim(-1, self.tower_dist+1)
   plt.yticks(np.arange(-1*np.round(max((self.girder_width,self.cable_x_dis
   plt.ylim(-1.5*np.round(max((self.girder_width,self.cable_x_dist,self.ded
   plt.legend(bbox to anchor=(1, 0.5), loc='center left')
   plt.grid()
   plt.ylabel('distance from centerline [m]')
   plt.title(self.file_names[0][:-4][14:]+' - '+self.file_names[-1][:-4][14
   if save:
       plt.savefig(('../images/'+self.file_names[0][:-4]+'-'+self.file_name
   plt.show()
   plt.close()
   gc.collect()
if side view:
   plt.figure(figsize=(12,4))
   if show_cables:
        if invert_xaxis:
            plt.plot(y_,z_cable,'-',color='g',label='cable')
       else:
            plt.plot(y ,z cable,'-',color='b',label='cable')
   if show deck:
        plt.plot(y_,z_deck,'-',color='dimgrey',label='deck')
   if show_girder:
        plt.plot(y_,z_deck-self.girder_height,'-',color='darkgrey',label='gi
       plt.fill_between(y_,z_deck,z_deck-self.girder_height,color='darkgrey
    if show hangers:
        if invert xaxis:
            plt.vlines(hanger_bottom_joint[0],hanger_bottom_joint[1],hanger_
            plt.vlines(hanger_bottom_joint[0],hanger_bottom_joint[1],hanger_
   if show towers:
        plt.vlines([y_[0]],[0],[z_cable[0]],color='black',label='South Tower
        plt.vlines([y_[-1]],[0],[z_cable[-1]],color='red',label='North Tower
   if show water:
        plt.hlines(0,0,self.tower dist,linestyle='-.',color='blue',label='Wa
   if show_COMs:
        plt.plot(hanger_COM[0],hanger_COM[1],'o',color='m',label='hanger COM
        plt.plot(cable_segment_COM[0], cable_segment_COM[1], 'o', color='y', lab
       plt.plot(deck_segment_COM[0],deck_segment_COM[1],'o',color='c',label
   if show joints:
        plt.plot(hanger_top_joint[0],hanger_top_joint[1],'.',color='m',label
        plt.plot(hanger bottom joint[0], hanger bottom joint[1],'.',color='m'
       plt.plot(cable_segment_south_joint[0],cable_segment_south_joint[1],'
        plt.plot(cable segment north joint[0],cable segment north joint[1],
```

```
plt.plot(deck_segment_south_joint[0],deck_segment_south_joint[1],'.'
            plt.plot(deck_segment_north_joint[0],deck_segment_north_joint[1],'.'
        if show_sensors:
            plt.plot(y accelerometer, z accelerometer, 's', ms=10, mec='black', color
            plt.plot(y_anemometer,z_anemometer,'^',ms=10,mec='black',color='gray
       if xticks_h_num:
            xtick_labels = list(np.arange(0,self.n_hangers+2,1))[::-1]
            xtick_labels[0] = 'S_Tower'
            xtick_labels[-1] = 'N_Tower'
            plt.xticks(y_,xtick_labels)
            plt.xlabel('hanger number')
       else.
            plt.xticks(np.arange(0,self.tower_dist+10,10),np.arange(0,self.tower_
            plt.xlabel('distance [m]')
       if invert_xaxis:
            plt.xlim(self.tower_dist+1,-1)
       else:
            plt.xlim(-1, self.tower_dist+1)
       plt.yticks(np.arange(0,self.h_towers,10),np.arange(0,self.h_towers,10))
       plt.legend(bbox_to_anchor=(1, 0.5), loc='center left')
       plt.grid()
       plt.ylabel('height above water [m]')
       plt.title(self.file_names[0][:-4][14:]+' - '+self.file_names[-1][:-4][14
            plt.savefig(('../images/'+self.file_names[0][:-4]+'-'+self.file_name
       plt.show()
       plt.close()
       gc.collect()
def plot_data(self,x_array,y_arrays,labels=[],title_suffix='',xlabel='x',ylabel=
    """Method to plot Lysefjord Bridge data in a consistent manner.
   Parameters
    _____
   x_array : array_like
       Array of x-values to be plotted.
   y_arrays : array_like or list of array_likes
       Array(s) of y-values to be plotted.
   labels : list of str, optional
        Labels for the data series.
   title_suffix : str, optional
       Add a suffix to the title.
    xlabel : str, default 'x'
       Label for the x-axis.
   ylabel : str, default 'y'
        Label for the y-axis.
   yunit : str, default '[]'
       Unit of y-axis.
    grid : bool, default True
       Show a grid on the plot.
    legend : bool, default True
       Show a legend on the plot.
    split_sensors : bool, default False
       Split the plot into the different sensors.
   xlim : tuple of (float, float), optional
        Tuple of two values specifying the x-axis limits.
   ylim : tuple of (float, float), optional
        Tuple of two values specifying the y-axis limits.
    axhlines : list of float, optional
```

```
List of y-values for horizontal lines to be plotted on the plot.
axhline_colors : list of str, default ['r','r','gold','g']
    List of colors for the horizontal lines.
yticks : array_like, optional
    Array of y-axis tick values.
ignored_sensors : list of str, optional
    List of sensors to be ignored in the plot.
save : bool, default False:
    Save the plot in ../images/. Note: Requires the prior existence of that
# Manage Labels.
if len(y_arrays.shape)!=1:
    if len(labels)<np.shape(y_arrays)[0]:</pre>
        difference = np.shape(y_arrays)[0]-len(labels)
        for i in range(difference):
            labels=np.append(labels,'data '+str(len(labels)+1))
if self.full detail:
    ylabel=ylabel.replace('_mean','')
# Plot single dataseries.
if len(y_arrays.shape)==1:
    plt.figure(figsize=(12,5))
    plt.plot(x_array,y_arrays,label=labels[0])
    for ind,y in enumerate(axhlines):
        try:
            plt.axhline(y,linestyle='--',label=y,color=axhline_colors[ind])
        except:
                plt.axhline(y,linestyle='--',label=y,color=axhline_colors[-1
            except:
                plt.axhline(y,linestyle='--',label=y)
    if grid:
        plt.grid()
    if legend:
        plt.legend(bbox_to_anchor=(1, 0.5), loc='center left')
    plt.xlabel(xlabel)
    plt.ylabel(ylabel+' '+yunit)
    plt.title(self.file_names[0][:-4][14:]+' - '+self.file_names[-1][:-4][14
    plt.xlim(xlim)
    plt.ylim(ylim)
    plt.yticks(yticks)
elif len(y_arrays)==0:
    raise ValueError('No Data.')
    return
# Plot multiple dataseries.
else:
    if split sensors:
        fig = plt.figure(figsize=(12,7),constrained_layout=True)
        axes = []
        for i in range(np.shape(y_arrays)[0]):
            if labels[i] not in ignored_sensors:
                if i == 0:
                    axes.append(plt.subplot(len(y arrays),1,i+1))
                    axes.append(plt.subplot(len(y_arrays),1,i+1,sharex=axes[
                plt.plot(x_array,y_arrays[i],label=labels[i])
                for ind,y in enumerate(axhlines):
                    try:
                        plt.axhline(y,linestyle='--',label=y,color=axhline_c
                    except:
```

```
try:
                                plt.axhline(y,linestyle='--',label=y,color=axhli
                            except:
                                plt.axhline(y,linestyle='--',label=y)
                    if grid:
                        plt.grid()
                    if legend:
                        plt.legend(bbox_to_anchor=(1, 0.5), loc='center left')
                    if i == 0:
                        plt.title(self.file_names[0][:-4][14:]+' - '+self.file_n
                    plt.xlim(xlim)
                    plt.ylim(ylim)
                    plt.yticks(yticks)
            fig.supxlabel(xlabel)
            fig.supylabel(ylabel+' '+yunit)
        else:
            plt.figure(figsize=(12,5))
            for i in range(np.shape(y_arrays)[0]):
                if labels[i] not in ignored_sensors:
                    plt.plot(x_array,y_arrays[i],label=labels[i])
            for ind,y in enumerate(axhlines):
                    plt.axhline(y,linestyle='--',label=y,color=axhline_colors[in
                except:
                    try:
                        plt.axhline(y,linestyle='--',label=y,color=axhline_color
                    except:
                        plt.axhline(y,linestyle='--',label=y)
            if grid:
                plt.grid()
            if legend:
                plt.legend(bbox_to_anchor=(1, 0.5), loc='center left')
            plt.xlabel(xlabel)
            plt.ylabel(ylabel+' '+yunit)
            plt.title(self.file_names[0][:-4][14:]+' - '+self.file_names[-1][:-4
            plt.xlim(xlim)
            plt.ylim(ylim)
            plt.yticks(yticks)
    if save:
        plt.savefig(('../images/'+self.file names[0][:-4]+'-'+self.file names[-1
    plt.show()
    plt.close()
    gc.collect()
def hist(self,data,bins=50,xlabel='data',xunit='[]',mode='relative frequency [%]
    """Method to create histograms on bridge data in a consistent manner.
    Parameters
    data : array_like
        Data to create the histogram on.
    bins : int, default 50
        Number of bins.
    xlabel : str, default 'data'
        Label describing the `data`.
    xunit : str, default '[]'
        Unit of `data`.
   mode : {'absolute frequency','relative frequency [%]','probability density'}
        Mode of the histogram. 'absolute frequency' has the bars height equal to
    title suffix : str, optional
        Add a suffix to the title.
    split_sensors : bool, default False
        Split the histogram into the different sensors.
    sensors : list of str, optional
```

```
List of sensor labels to place above seperate histograms if `split_senso
ncol : int, default 4
    Number of columns defining the grid to place the histograms on if `split
bridge_model : bool, default False
    Whether to place the histograms on a gird based on their location at the
Hanger_num : list of int, optional
    List of the hanger numbers at which each sensor is located.
West, Top: list of bool, optional
    List of booleans defining whether each sensor is located on the West sid
save : bool, default False
    Save the histogram in ../images/. Note: Requires the prior existence of
See Also
_____
`hist2d`
`windrose`
# Manage Labels.
if len(data.shape)!=1:
    if len(sensors)<len(data):</pre>
        difference = len(data)-len(sensors)
        for i in range(difference):
            sensors=np.append(sensors, 'sensor '+str(len(sensors)+1))
if self.full detail:
    xlabel=xlabel.replace('_mean','')
if len(np.shape(data))==1 or split_sensors==False:
    # Create one histogram for one or multiple sensors.
    plt.figure(figsize=(10,8))
    if mode == 'absolute frequency':
        plt.hist(data.flatten(),density=False,bins=bins)
    elif mode == 'relative frequency [%]':
        plt.hist(data.flatten(),density=False,weights=np.zeros_like(data.fla
    elif mode == 'probability density':
        plt.hist(data.flatten(),density=True,bins=bins)
    else:
        raise ValueError('Invalid mode. mode needs to be "absolute frequency
    plt.xlabel(xlabel+' '+xunit)
    plt.ylabel(mode)
    plt.title(self.file_names[0][:-4][14:]+' - '+self.file_names[-1][:-4][14
else:
    # Create multiple histograms for multiple sensors.
    if bridge_model:
        # Place histograms on a grid based on the sensors' locations on the
        # Assign a level based on West/East and Top/Bottom location of the s
        1v1 = []
        for i in range(np.shape(data)[0]):
            if West[i] == 1:
                if Top[i] == 1:
                    lvl.append(2)
                else:
                    lvl.append(3)
            else:
                if Top[i] == 1:
                    lvl.append(0)
                else:
                    lvl.append(1)
        # Skip empty rows and cols.
        Hanger_nums = np.unique(Hanger_num)
        ncol = len(Hanger_nums)
```

```
col = []
            unique_lvls = np.unique(lvl)
            nrow = len(unique_lvls)
            row = []
            for i in range(np.shape(data)[0]):
                col.append(np.where(Hanger_nums==Hanger_num[i])[0][0])
                row.append(np.where(unique_lvls==lvl[i])[0][0])
            # Plot the histograms.
            fig = plt.figure(figsize=(5*ncol,5*nrow),constrained_layout=True)
            axes = []
            for i in range(np.shape(data)[0]):
                if i == 0:
                    axes.append(plt.subplot2grid((nrow,ncol),(row[i],col[i])))
                else:
                    axes.append(plt.subplot2grid((nrow,ncol),(row[i],col[i]),sha
                if mode == 'absolute frequency':
                    plt.hist(data[i],density=False,bins=bins)
                elif mode == 'relative frequency [%]':
                    plt.hist(data[i],density=False,weights=np.zeros_like(data[i])
                elif mode == 'probability density':
                    plt.hist(data[i],density=True,bins=bins)
                else:
                    raise ValueError('Invalid mode. mode needs to be "absolute f
                plt.title(sensors[i])
            fig.supxlabel(xlabel+' '+xunit)
            fig.supylabel(mode)
            fig.suptitle(self.file_names[0][:-4][14:]+' - '+self.file_names[-1][
       else:
            nrow = np.ceil(len(data)/ncol).astype(int)
            fig = plt.figure(figsize=(5*ncol,5*nrow),constrained layout=True)
            axes = []
            for i in range(np.shape(data)[0]):
                if i == 0:
                    axes.append(plt.subplot(nrow,ncol,i+1))
                else:
                    axes.append(plt.subplot(nrow,ncol,i+1,sharex=axes[0],sharey=
                if mode == 'absolute frequency':
                    plt.hist(data[i],density=False,bins=bins)
                elif mode == 'relative frequency [%]':
                    plt.hist(data[i],density=False,weights=np.zeros_like(data[i])
                elif mode == 'probability density':
                    plt.hist(data[i],density=True,bins=bins)
                else:
                    raise ValueError('Invalid mode. mode needs to be "absolute f
                plt.title(sensors[i])
            fig.supxlabel(xlabel+' '+xunit)
            fig.supylabel('probability density')
            fig.suptitle(self.file names[0][:-4][14:]+' - '+self.file names[-1][
        plt.savefig(('../images/'+self.file_names[0][:-4]+'-'+self.file_names[-1]
    plt.show()
    plt.close()
    gc.collect()
def scatterplot(self,data1,data2,data3,label1='data1',label2='data2',label3='dat
    """Method to create scatterplots on bridge data in a consistent manner.
    Parameters:
    data1 : array_like
       Data for x-axis.
    data2 : array_like
```

```
Data for y-axis.
data3 : array_like
    Data for color-axis.
label1 : str, default 'data1'
    Label for x-axis.
label2 : str, default 'data2'
    Label for y-axis.
label3 : str, default 'data3'
    Label for colorbar.
units: list of str, default ['[]','[]','[]']
    Units for x-,y- and color-axis.
title_suffix : str, optional
    Add a suffix to the title.
color: bool, default True
    The scatterplot is colored based on data3.
plot_in_order_of_color : bool, default True
    Plot the datapoints of higher color ontop of datapoints of lower color.
cmap : colormap or str, default 'viridis'
    Colormap to use for the scatterplot.
vmin : float, optional
    Lower limit for the color-axis.
vmax : float, optional
    Upper limit for the color-axis.
curve_fit : bool, default False
    Fit a curve to the scatterplot. Note: Only works for single scatterplot,
func : {'quadratic', 'linear'}
    Function for curve fitting.
upper_lim : float, default np.inf
    Upper limit for data3 values.
lower_lim : float, default -np.inf
    Lower limit for data3 values.
bounds : tuple, default ([-np.inf,-np.inf,-np.inf],[np.inf,np.inf,np.inf])
    Bounds for curve fitting parameters.
res : int, default 1000
    Number of points for the curve fitting.
pred : float, default 1.5
   Value for prediction of curve fitting.
curve_fit_return : bool, default False
    Return the parameters of the curve fit.
split_sensors : bool, default False
    Split the scatterplot into the different sensors.
sensors : list of str, optional
    List of sensor labels to place above seperate scatterplots if `split_sen
ncol : int, default 4
    Number of columns defining the grid to place the scatterplots on if `spl
bridge_model : bool, default False
    Whether to place the scatterplots on a gird based on their location at t
Hanger num : list of int, optional
    List of the hanger numbers at which each sensor is located.
West, Top: list of bool, optional
    List of booleans defining whether each sensor is located on the West sid
save : bool, default False
    Save the scatterplot in ../images/. Note: Requires the prior existence of
Returns:
popt1, popt2, pcov1, pcov2 : array like, optional
    If `curve_fit_return` is True, returns the parameters of the curve fit.
See Also
`polar_scatterplot`
# Checking for miss-shaped data.
```

```
if color:
    if not (data1.shape == data2.shape == data3.shape):
        raise IndexError('data1',data1.shape,', data2',data2.shape,' and dat
else:
    if not (data1.shape == data2.shape):
       raise IndexError('data1',data1.shape,' and data2',data2.shape,' must
# Manage Labels.
if len(data1.shape)!=1:
    if len(sensors)<len(data1):</pre>
       difference = len(data1)-len(sensors)
        for i in range(difference):
            sensors=np.append(sensors, 'sensor '+str(len(sensors)+1))
if self.full detail:
    label1=label1.replace('_mean','')
   label2=label2.replace('_mean','')
    label3=label3.replace('_mean','')
if vmin == None:
   vmin=np.min(data3)
if vmax == None:
   vmax=np.max(data3)
if type(cmap)==str:
   cmap=mpl.colormaps[cmap]
if len(np.shape(data1))==1 or split_sensors==False:
    # Create one scatterplot for one or multiple sensors.
   plt.figure(figsize=(10,8))
   if color:
        if plot_in_order_of_color:
            ind=np.argsort(data3.flatten())
            data1=data1.flatten()[ind]
            data2=data2.flatten()[ind]
            data3=data3.flatten()[ind]
        plt.scatter(data1,data2,c=data3,vmin=vmin,vmax=vmax,cmap=cmap)
        plt.colorbar(label=label3+' '+units[2])
       plt.title(self.file_names[0][:-4][14:]+' - '+self.file_names[-1][:-4
   else:
        plt.scatter(data1,data2)
       plt.title(self.file_names[0][:-4][14:]+' - '+self.file_names[-1][:-4
   plt.xlabel(label1+' '+units[0])
   plt.ylabel(label2+' '+units[1])
   if curve_fit:
        if func=='quadratic':
            def quadratic function(x,a,h,k):
                y = a*(x-h)*(x-h)+k
            popt1,pcov1=scipy.optimize.curve_fit(quadratic_function,data1[da
            popt2,pcov2=scipy.optimize.curve_fit(quadratic_function,data1[da
            plt.plot(np.linspace(np.mean(data1)-pred*np.abs(np.mean(data1)-n
            plt.plot(np.linspace(np.mean(data1)-pred*np.abs(np.mean(data1)-n
            plt.ylim(np.mean(data2)-pred*np.abs(np.mean(data2)-np.min(data2)
            plt.legend(bbox to anchor=(1, 0), loc='lower right',ncol=2)
        elif func=='linear':
            def linear_function(x,a,b):
                y = a*x+b
                return y
            popt1,pcov1=scipy.optimize.curve_fit(linear_function,data1[data3
            popt2,pcov2=scipy.optimize.curve_fit(linear_function,data1[data3
            plt.plot(np.linspace(np.mean(data1)-pred*np.abs(np.mean(data1)-n
```

```
plt.plot(np.linspace(np.mean(data1)-pred*np.abs(np.mean(data1)-n
            plt.ylim(np.mean(data2)-pred*np.abs(np.mean(data2)-np.min(data2)
            plt.legend(bbox_to_anchor=(1, 0), loc='lower right',ncol=2)
       else:
            raise NotImplementedError('Only "quadratic" and "linear" functio
else:
    # Create multiple scatterplots for multiple sensors.
   if bridge model:
        # Place scatterplots on a grid based on the sensors' locations on th
        # Assign Level based on West/East and Top/Bottom Location.
       1v1 = []
        for i in range(np.shape(data1)[0]):
            if West[i] == 1:
                if Top[i] == 1:
                    lvl.append(2)
                else:
                    lvl.append(3)
            else:
                if Top[i] == 1:
                    lvl.append(0)
                else:
                    lvl.append(1)
        # Skip empty rows and cols.
       Hanger_nums = np.unique(Hanger_num)
       ncol = len(Hanger_nums)
        col = []
       unique_lvls = np.unique(lvl)
       nrow = len(unique_lvls)
       row = []
        for i in range(np.shape(data1)[0]):
            col.append(np.where(Hanger nums==Hanger num[i])[0][0])
            row.append(np.where(unique_lvls==lvl[i])[0][0])
        # Plot the scatterplots.
       fig = plt.figure(figsize=(5*ncol,5*nrow),constrained_layout=True)
        axes = []
        for i in range(np.shape(data1)[0]):
            if i == 0:
                axes.append(plt.subplot2grid((nrow,ncol),(row[i],col[i])))
            else:
                axes.append(plt.subplot2grid((nrow,ncol),(row[i],col[i]),sha
            if color:
                if plot_in_order_of_color:
                    ind=np.argsort(data3[i])
                    data1[i]=data1[i][ind]
                    data2[i]=data2[i][ind]
                    data3[i]=data3[i][ind]
                sct = plt.scatter(data1[i],data2[i],c=data3[i],vmin=vmin,vma
                plt.scatter(data1[i],data2[i])
            plt.title(sensors[i])
        if color:
            fig.suptitle(self.file_names[0][:-4][14:]+' - '+self.file_names[
            fig.colorbar(sct, ax=axes,label=label3+' '+units[2])
        else:
            fig.suptitle(self.file names[0][:-4][14:]+' - '+self.file names[
       fig.supxlabel(label1+' '+units[0])
        fig.supylabel(label2+' '+units[1])
   else:
       nrow = np.ceil(len(data1)/ncol).astype(int)
       fig = plt.figure(figsize=(5*ncol,5*nrow),constrained_layout=True)
       axes = []
        for i in range(np.shape(data1)[0]):
            if i == 0:
```

```
axes.append(plt.subplot(nrow,ncol,i+1))
                else:
                    axes.append(plt.subplot(nrow,ncol,i+1,sharex=axes[0],sharey=
                if color:
                    if plot in order of color:
                        ind=np.argsort(data3[i])
                        data1[i]=data1[i][ind]
                        data2[i]=data2[i][ind]
                        data3[i]=data3[i][ind]
                    sct = plt.scatter(data1[i],data2[i],c=data3[i],vmin=vmin,vma
                    plt.scatter(data1[i],data2[i])
                plt.title(sensors[i])
            if color:
                fig.suptitle(self.file_names[0][:-4][14:]+' - '+self.file_names[
                fig.colorbar(sct, ax=axes,label=label3+' '+units[2])
            else:
                fig.suptitle(self.file_names[0][:-4][14:]+' - '+self.file_names[
            fig.supxlabel(label1+' '+units[0])
            fig.supylabel(label2+' '+units[1])
    if save:
        if color:
            plt.savefig(('../images/'+self.file_names[0][:-4]+'-'+self.file_name
        else:
            plt.savefig(('../images/'+self.file_names[0][:-4]+'-'+self.file_name
    plt.show()
    plt.close()
    gc.collect()
    if curve_fit:
        if curve fit return:
            return popt1, popt2, pcov1, pcov2
def polar_scatterplot(self,data1,data2,data3,label1='Direction',label2='data2',l
    """Method to create polar scatterplots on bridge data in a consistent manner
   Parameters:
    data1 : array like
       Data for theta-axis.
    data2 : array_like
       Data for r-axis.
    data3 : array like
       Data for color-axis.
    label1 : str, default 'data1'
       Label for theta-axis.
    label2 : str, default 'data2'
       Label for r-axis.
    label3 : str, default 'data3'
       Label for colorbar.
    units: list of str, default ['[]','[]','[]']
       Units for x-,y- and color-axis.
    title_suffix : str, optional
       Add a suffix to the title.
    bridge_offset : float, default -42
       Offset of the bridge-axis from the geographic north-south-axis in degree
    bridge north : bool, default False
       Orient the polar scatterplot with 'bridge-north' at the top.
    color : bool, default True
       The polar scatterplot is colored based on data3.
    plot_in_order_of_color : bool, default True
       Plot the datapoints of higher color ontop of datapoints of lower color.
    cmap : colormap or str, default 'viridis'
       Colormap to use for the polar scatterplot.
```

```
vmin : float, optional
    Lower limit for the color-axis.
vmax : float, optional
    Upper limit for the color-axis.
split sensors : bool, default False
    Split the polar scatterplot into the different sensors.
sensors: list of str, optional
    List of sensor labels to place above seperate polar scatterplots if `spl
ncol: int, default 4
    Number of columns defining the grid to place the polar scatterplots on i
bridge_model : bool, default False
    Whether to place the polar scatterplots on a gird based on their locatio
Hanger_num : list of int, optional
    List of the hanger numbers at which each sensor is located.
West, Top: list of bool, optional
    List of booleans defining whether each sensor is located on the West sid
save : bool, default False
    Save the polar scatterplot in ../images/. Note: Requires the prior exist
See Also
`scatterplot`
`windrose`
# Checking for miss-shaped data.
if color:
    if not (data1.shape == data2.shape == data3.shape):
        raise IndexError('data1',data1.shape,', data2',data2.shape,' and dat
    if not (data1.shape == data2.shape):
        raise IndexError('data1',data1.shape,' and data2',data2.shape,' must
# Manage labels.
if len(data1.shape)!=1:
    if len(sensors)<len(data1):</pre>
        difference = len(data1)-len(sensors)
        for i in range(difference):
            sensors=np.append(sensors, 'sensor '+str(len(sensors)+1))
if self.full detail:
    label1=label1.replace('_mean','')
    label2=label2.replace('_mean','')
    label3=label3.replace('_mean','')
if vmin == None:
    vmin=np.min(data3)
if vmax == None:
    vmax=np.max(data3)
if type(cmap)==str:
    cmap=mpl.colormaps[cmap]
if bridge_north:
    bridge_offset=0
if len(np.shape(data1))==1 or split sensors==False:
    # Create one polar scatterplot for one or multiple sensors.
    fig = plt.figure(figsize=(10,8))
    ax = fig.add subplot(projection='polar')
    plt.axvline(np.deg2rad(bridge offset),color='r',label='Bridge North')
    plt.axvline(np.deg2rad(180+bridge_offset),color='black',label='Bridge So
    if color:
        if plot in order of color:
            ind=np.argsort(data3.flatten())
```

```
data1=data1.flatten()[ind]
            data2=data2.flatten()[ind]
            data3=data3.flatten()[ind]
        sct = ax.scatter(np.deg2rad(data1+bridge_offset),data2,c=data3,vmin=
        fig.colorbar(sct,label=label3+' '+units[2])
        fig.suptitle(self.file_names[0][:-4][14:]+' - '+self.file_names[-1][
   else:
        ax.scatter(np.deg2rad(data1+bridge offset),data2)
        fig.suptitle(self.file_names[0][:-4][14:]+' - '+self.file_names[-1][
    ax.set_xlabel(label1+' '+units[0])
    ax.set_ylabel(label2+' '+units[1], rotation=55)
   ax.yaxis.set_label_coords(0.72, 0.8,transform=ax.transAxes)
   ax.set theta zero location('N', offset=0)
   ax.set theta direction(-1)
   plt.legend(bbox_to_anchor=(0.9, 0.05), loc='lower right',bbox_transform=
else:
    # Create multiple polar scatterplots for multiple sensors.
   if bridge_model:
        # Place polar scatterplots on a grid based on the sensors' locations
        # Assign Level based on West/East and Top/Bottom Location.
       1v1 = []
        for i in range(np.shape(data1)[0]):
            if West[i] == 1:
                if Top[i] == 1:
                    lvl.append(2)
                else:
                    lvl.append(3)
            else:
                if Top[i] == 1:
                    lvl.append(0)
                else:
                    lvl.append(1)
        # Skip empty rows and cols.
       Hanger_nums = np.unique(Hanger_num)
       ncol = len(Hanger_nums)
        col = []
       unique_lvls = np.unique(lvl)
       nrow = len(unique lvls)
        for i in range(np.shape(data1)[0]):
            col.append(np.where(Hanger nums==Hanger num[i])[0][0])
            row.append(np.where(unique lvls==lvl[i])[0][0])
        # Plot the polar scatterplots.
        fig = plt.figure(figsize=(5*ncol,5*nrow),constrained_layout=True)
        axes = []
        for i in range(np.shape(data1)[0]):
            if i == 0:
                axes.append(plt.subplot2grid((nrow,ncol),(row[i],col[i]),pro
                plt.axvline(np.deg2rad(bridge offset),color='r',label='Bridg
                plt.axvline(np.deg2rad(180+bridge_offset),color='black',labe
            else:
                axes.append(plt.subplot2grid((nrow,ncol),(row[i],col[i]),pro
                plt.axvline(np.deg2rad(bridge_offset),color='r')
                plt.axvline(np.deg2rad(180+bridge offset),color='black')
            if color:
                if plot_in_order_of_color:
                    ind=np.argsort(data3[i])
                    data1[i]=data1[i][ind]
                    data2[i]=data2[i][ind]
                    data3[i]=data3[i][ind]
                sct = axes[i].scatter(np.deg2rad(data1[i]+bridge_offset),dat
            else:
```

```
axes[i].set_theta_zero_location('N', offset=0)
                axes[i].set_theta_direction(-1)
                plt.title(sensors[i])
            if color:
                fig.suptitle(self.file_names[0][:-4][14:]+' - '+self.file_names[
                fig.colorbar(sct, ax=axes,label=label3+' '+units[2])
                fig.suptitle(self.file_names[0][:-4][14:]+' - '+self.file_names[
            fig.legend(bbox_to_anchor=(0.9, 0), loc='lower right',bbox_transform
            fig.supxlabel(label1+' '+units[0])
            fig.supylabel(label2+' '+units[1],rotation=67.5)
       else:
            nrow = np.ceil(len(data1)/ncol).astype(int)
            fig = plt.figure(figsize=(5*ncol,5*nrow),constrained_layout=True)
            axes = []
            for i in range(np.shape(data1)[0]):
                if i == 0:
                    axes.append(plt.subplot(nrow,ncol,i+1,projection='polar'))
                    plt.axvline(np.deg2rad(bridge_offset),color='r',label='Bridg
                    plt.axvline(np.deg2rad(180+bridge_offset),color='black',labe
                else:
                    axes.append(plt.subplot(nrow,ncol,i+1,projection='polar',sha
                    plt.axvline(np.deg2rad(bridge_offset),color='r')
                    plt.axvline(np.deg2rad(180+bridge_offset),color='black')
                if color:
                    if plot_in_order_of_color:
                        ind=np.argsort(data3[i])
                        data1[i]=data1[i][ind]
                        data2[i]=data2[i][ind]
                        data3[i]=data3[i][ind]
                    sct = axes[i].scatter(np.deg2rad(data1[i]+bridge_offset),dat
                else:
                    axes[i].scatter(np.deg2rad(data1[i]+bridge_offset),data2[i])
                axes[i].set_theta_zero_location('N', offset=0)
                axes[i].set_theta_direction(-1)
                plt.title(sensors[i])
            if color:
                fig.suptitle(self.file_names[0][:-4][14:]+' - '+self.file_names[
                fig.colorbar(sct, ax=axes,label=label3+' '+units[2])
            else:
                fig.suptitle(self.file_names[0][:-4][14:]+' - '+self.file_names[
            fig.legend(bbox to anchor=(0.9, 0), loc='lower right',bbox transform
            fig.supxlabel(label1+' '+units[0])
            fig.supylabel(label2+' '+units[1],rotation=67.5)
    if save:
       if color:
            plt.savefig(('../images/'+self.file names[0][:-4]+'-'+self.file name
            plt.savefig(('../images/'+self.file_names[0][:-4]+'-'+self.file_name
    plt.show()
    plt.close()
    gc.collect()
def windrose(self,Dir,data,bridge_offset=-42,label='data',unit='[]',title_suffix
    """Method to create wind roses on bridge data in a consistent manner.
    Parameters:
    ______
   Dir : array like
       Directional data for theta-axis.
    data : array_like
       Data for wind rose.
    bridge_offset : float, default -42
```

axes[i].scatter(np.deg2rad(data1[i]+bridge_offset),data2[i])

```
Offset of the bridge-axis from the geographic north-south-axis in degree
label : str, default 'data'
    Label for color-legend.
unit : str, default '[]'
    Unit of `data`.
title_suffix : str, optional
    Add a suffix to the title.
bridge_north : bool, default False
    Orient the wind rose with 'bridge-north' at the top.
bins : array_like, optional
    Bins to use for the wind rose.
nbins : int, default 6
    Number of bins to use for the wind rose if `bins` is not provided.
cmap : colormap or str, default 'viridis'
    Colormap to use for the wind rose.
split_sensors : bool, default False
    Split the wind rose into the different sensors.
sensors : list of str, optional
    List of sensor labels to place above seperate wind roses if `split_senso
ncol: int, default 4
    Number of columns defining the grid to place the wind roses on if `split
bridge_model : bool, default False
    Whether to place the wind roses on a gird based on their location at the
Hanger_num : list of int, optional
    List of the hanger numbers at which each sensor is located.
West, Top: list of bool, optional
    List of booleans defining whether each sensor is located on the West sid
save : bool, default False
    Save the polar scatterplot in ../images/. Note: Requires the prior exist
See Also
_____
`polar_scatterplot`
`hist`
`hist2d`
# Checking for miss-shaped data.
if not (Dir.shape == data.shape):
    raise IndexError('Dir',Dir.shape,' and data',data.shape,' must be of the
# Manage Labels.
if len(data.shape)!=1:
    if len(sensors)<len(data):</pre>
        difference = len(data)-len(sensors)
        for i in range(difference):
            sensors=np.append(sensors, 'sensor '+str(len(sensors)+1))
if self.full_detail:
    label=label.replace(' mean','')
if bridge north:
    bridge_offset=0
if len(bins)==0:
    bins=np.linspace(np.min(data),np.max(data),nbins)
if type(cmap)==str:
    cmap=mpl.colormaps[cmap]
if len(np.shape(data))==1 or split_sensors==False:
    # Create one wind rose for one or multiple sensors.
    fig = plt.figure(figsize=(10,10))
    ax = WindroseAxes.from_ax(fig=fig)
    # Plot the wind rose.
```

```
ax.bar(Dir.flatten()+bridge_offset, data.flatten(), normed=True, opening
   # Setup additional elements.
   ax.axvline(np.deg2rad(90-bridge_offset),color='r',label='Bridge North')
    ax.axvline(np.deg2rad(270-bridge offset),color='black',label='Bridge Sou
    ax.set_ylabel('relative frequency [%]', rotation=55)
   ax.yaxis.set_label_coords(0.72, 0.8,transform=ax.transAxes)
    ax.set_legend(title=label+' '+unit,bbox_to_anchor=(0.9, 0.1),bbox_transf
    fig.legend(bbox_to_anchor=(0.9, 0.1),bbox_transform=fig.transFigure, loc
    plt.title(self.file_names[0][:-4][14:]+' - '+self.file_names[-1][:-4][14
else:
   # Create multiple wind roses for multiple sensors.
    if bridge model:
        # Place the wind roses on a grid based on the sensors' locations on
        # Assign a level based on West/East and Top/Bottom location of the s
        1v1 = []
        for i in range(np.shape(data)[0]):
            if West[i] == 1:
                if Top[i] == 1:
                    lvl.append(2)
                else:
                    lvl.append(3)
            else:
                if Top[i] == 1:
                    lvl.append(0)
                else:
                    lvl.append(1)
        # Skip empty rows and cols.
        Hanger nums = np.unique(Hanger num)
        ncol = len(Hanger_nums)
        col = []
        unique_lvls = np.unique(lvl)
        nrow = len(unique_lvls)
        row = []
        for i in range(np.shape(data)[0]):
            col.append(np.where(Hanger nums==Hanger num[i])[0][0])
            row.append(np.where(unique lvls==lvl[i])[0][0])
        # Create the wind rose axes.
        fig = plt.figure(figsize=(6*ncol,6*nrow),constrained_layout=True)
        axes = []
        for i in range(np.shape(data)[0]):
            temp_ax=plt.subplot2grid((nrow,ncol),(row[i],col[i]))
            rect=temp_ax.get_position()
            temp ax.remove()
            axes.append(WindroseAxes.from ax(fig=fig,rect=rect))
            # Plot the wind roses.
            axes[i].bar(Dir[i]+bridge_offset, data[i], normed=True, opening=
            # Setup additional elements.
            if i == 0:
                axes[i].axvline(np.deg2rad(90-bridge offset),color='r',label
                axes[i].axvline(np.deg2rad(270-bridge offset),color='black',
            else:
                axes[i].axvline(np.deg2rad(90-bridge offset),color='r')
                axes[i].axvline(np.deg2rad(270-bridge offset),color='black')
            plt.title(sensors[i])
        axes[-1].set_legend(title=label+' '+unit,bbox_to_anchor=(0.9, 0.1),
        fig.suptitle(self.file names[0][:-4][14:]+' - '+self.file names[-1][
        fig.legend(bbox_to_anchor=(0.9, 0.1), loc='upper left',bbox_transfor
```

```
fig.supylabel('relative frequency [%]',rotation=67.5)
       else:
            # Define the plot grid
            nrow = np.ceil(len(data)/ncol).astype(int)
            # Create the wind rose axes.
            fig = plt.figure(figsize=(6*ncol,6*nrow),constrained_layout=True)
            axes = []
            for i in range(np.shape(data)[0]):
                temp_ax=plt.subplot(nrow,ncol,i+1)
                rect=temp_ax.get_position()
                temp_ax.remove()
                axes.append(WindroseAxes.from_ax(fig=fig,rect=rect))
                # Plot the wind roses.
                axes[i].bar(Dir[i]+bridge_offset, data[i], normed=True, opening=
                # Setup additional elements.
                if i == 0:
                    axes[i].axvline(np.deg2rad(90-bridge_offset),color='r',label
                    axes[i].axvline(np.deg2rad(270-bridge_offset),color='black',
                else:
                    axes[i].axvline(np.deg2rad(90-bridge_offset),color='r')
                    axes[i].axvline(np.deg2rad(270-bridge_offset),color='black')
                plt.title(sensors[i])
            axes[-1].set_legend(title=label+' '+unit,bbox_to_anchor=(0.9, 0.1),
            fig.suptitle(self.file_names[0][:-4][14:]+' - '+self.file_names[-1][
            fig.legend(bbox_to_anchor=(0.9, 0.1), loc='upper left',bbox_transfor
            fig.supylabel('relative frequency [%]',rotation=67.5)
    if save:
       plt.savefig(('../images/'+self.file_names[0][:-4]+'-'+self.file_names[-1]
    plt.show()
    plt.close()
    gc.collect()
def hist2d(self,data1,data2,label1='data1',label2='data2',units=['[]','[]'],titl
    """Method to create 2D histograms on bridge data in a consistent manner.
   Parameters
    _____
    data1 : array like
       Data for x-axis of the 2d histogram.
    data2 : array_like
       Data for y-axis of the 2d histogram.
    label1 : str, default 'data1'
       Label describing `data1`.
    label2 : str, default 'data2'
       Label describing `data2`.
   units : list of str, default ['[]','[]']
       Units of `data1` and `data2`.
    title_suffix : str, optional
       Add a suffix to the title.
    bins : tuple of ints, default (20,20)
       Tuple of two values specifying the number of bins in x- and y-direction.
    save : bool, default False
       Save the 2D histogram in ../images/. Note: Requires the prior existence
   See Also
    _____
    `hist`
    `windrose`
   if self.full_detail:
```

```
label1=label1.replace('_mean','')
        label2=label2.replace('_mean','')
    plt.figure(figsize=(10,8))
    plt.hist2d(data1,data2,bins,density=True,cmin=0,cmax=1)
    plt.xlabel(label1+' '+units[0])
    plt.ylabel(label2+' '+units[1])
    plt.colorbar(label='probability density')
   plt.title(self.file_names[0][:-4][14:]+' - '+self.file_names[-1][:-4][14:]+'
    if save:
        plt.savefig(('../images/'+self.file_names[0][:-4]+'-'+self.file_names[-1]
    plt.show()
    plt.close()
    gc.collect()
def boxplot(self,data,labels,ylabel='data',yunit='[]',title_suffix='',save=False
    """Method to create boxplots on bridge data in a consistent manner.
   Parameters
    _____
    data: array_like
       Data for the boxplots with first axis as sensor id and second axis as me
   labels : list of str
       Sensor labels for the different boxplots.
   ylabel : str, default 'data'
       Label describing `data`.
   yunit : str, optional
       Unit of `data`.
    title_suffix : str, optional
       Add a suffix to the title.
    save : bool, default False
       Save the boxplot in ../images/. Note: Requires the prior existence of the
    if self.full detail:
       ylabel=ylabel.replace('_mean','')
   plt.figure(figsize=(10,8))
   plt.boxplot(data.T, vert=True, labels=labels)
   plt.ylabel(ylabel+' '+yunit)
   plt.title(self.file_names[0][:-4][14:]+' - '+self.file_names[-1][:-4][14:]+'
   if save:
        plt.savefig(('../images/'+self.file_names[0][:-4]+'-'+self.file_names[-1]
    plt.show()
   plt.close()
    gc.collect()
def correlation_matrix(self,data1,data2,labels_data1=[],labels_data2=[],title1='
    """Method to create heatmaps of correlation matrices on bridge data in a con
   Parameters
    _____
    data1 : array_like
        Input data for `data1` to be corelated with itself and `data2`.
    data2 : array_like
        Input data for `data2` to be corelated with itself and `data1`.
    labels data1 : list of str, optional
        Labels for `data1`.
    labels_data2 : list of str, optional
       Labels for `data2`.
   title1 : str, default 'data1'
       Title describing `data1`.
    title2 : str, default 'data2'
        Title describing `data2`.
    title_suffix : str, optional
```

```
Add a suffix to the title.

save : bool, default False

Save the correlation matrix heatmap in ../images/. Note: Requires the pr

"""

Correlation_matrix = np.corrcoef(data1,data2)

cm_labels=[title1+' '+label for label in list(labels_data1)]+[title2+' '+lab plt.figure(figsize=(12,10))

try:

sn.heatmap(Correlation_matrix,cmap='coolwarm',vmin=-1,vmax=1,xticklabels except:

sn.heatmap(Correlation_matrix,cmap='coolwarm',vmin=-1,vmax=1)

plt.title(self.file_names[0][:-4][14:]+' - '+self.file_names[-1][:-4][14:]+'

if save:

plt.savefig(('../images/'+self.file_names[0][:-4]+'-'+self.file_names[-1 plt.show())

plt.close()
gc.collect()
```

Example of how to use the BridgeData class

The code below is an example to showcase how to use the BridgeData class. Note that the code generally has to be run from top to bottom, although some code blocks might be able to run on their own, depending on the state of other code blocks. Should you experience errors or unexpected result when experimenting with the code try running the code from the top after you made your changes.

Initialize a BridgeData class instance

Set the file_path.

```
In [ ]: file_path = '../Data/Bridge/dataExtracted/' # Adjust filepath to where your data is
```

Set the file_names . Un-comment one of the pre-set list of file_names or create your own. Make sure the data files are located in the location defined by file path

```
In []: # file_names = ['dataExtracted_2014_05_22.mat'] # From Etienne's analysis
    # file_names = ['dataExtracted_2014_08_01.mat', 'dataExtracted_2014_08_02.mat', 'dataE
    # file_names = ['dataExtracted_2014_08_09.mat'] # Up to 25m/s from SSW and NNE
    # file_names = ['dataExtracted_2014_08_18.mat', 'dataExtracted_2014_08_19.mat'] # Up
    # file_names = ['dataExtracted_2014_10_07.mat'] # From Etienne's analysis N-NE up to
    # file_names = ['dataExtracted_2014_10_26.mat'] # From Etienne's analysis S-SW up to
    # file_names = ['dataExtracted_2014_10_25.mat', 'dataExtracted_2014_10_26.mat', 'dataE
    # file_names = ['dataExtracted_2017_02_20.mat', 'dataExtracted_2017_02_21.mat', 'dataE
    # file_names = ['dataExtracted_2017_04_21.mat', 'dataExtracted_2017_04_22.mat', 'dataE
    # file_names = ['dataExtracted_2017_04_21.mat', 'dataExtracted_2017_04_22.mat', 'dataE
# file_names = ['dataExtracted_2017_04_24.mat'] # Peak of 16m/s
```

```
# file_names = ['dataExtracted_2017_10_01.mat', 'dataExtracted_2017_10_02.mat', 'dataE
# file_names = ['dataExtracted_2018_01_14.mat', 'dataExtracted_2018_01_15.mat'] # Up
# file_names = ['dataExtracted_2018_09_18.mat', 'dataExtracted_2018_09_19.mat']
# file_names = ['dataExtracted_2018_09_19.mat']
# file_names = ['dataExtracted_2018_09_19.mat', 'dataExtracted_2018_09_20.mat', 'dataE
# file_names = ['dataExtracted_2018_09_18.mat', 'dataExtracted_2018_09_19.mat', 'dataE
file_names = ['dataExtracted_2018_09_18.mat', 'dataExtracted_2018_09_19.mat', 'dataExt
# file_names = ['dataExtracted_2018_10_02.mat', 'dataExtracted_2018_10_03.mat']
# file_names = ['dataExtracted_2018_10_11.mat', 'dataExtracted_2018_10_12.mat'] # Up
```

Create an instance of the BridgeData class.

```
In [ ]: LFB = BridgeData(file_names=file_names,file_path=file_path)
```

Load data

Use the load_data method to import the MATLAB files defined by file_names . refer to the documentation (using help(BridgeData.load_data)) to learn more about the different options for the import of the data, such as the full_detail mode, which allows acces to the full 50Hz sample rate data.

Caution: It is recommended to only use the full_detail mode on **one day** of data that you have previously singled out from a larger dataset for detailed analysis. This is because of the large ammount of data that needs to be processed (4.32 million datapoints per sensor for each day of data).

```
In [ ]: help(BridgeData.load_data)
```

Help on function load_data in module __main__:

load_data(self, print_data_structure=False, delete_data_after_import=True, ignore_na ns=True, rename_H20_acc=True, replace_invalid=True, full_detail=False, H=True, W=Tru e, Vx=True, Vy=True, Dir=True, Tv=True, Turb=True, Aox_W=True, Aoy_W=True, Aoz_W=True e, Aox_E=True, Aoy_E=True, T=True, P=True, Hum=True, AOA=True, AOI=True, Upwind=True, theta=True, centr=True, Hanger_num=True, y_pos=True, accs_in_SI_units=True, WestEast=True, TopBottom=True)

Wrapper-method to import and combine multiple days of data using `convert_MATLAB`. Parameters are passed on to this helper-method.

Convert Lysefjord Bridge dataExtracted.mat files imported via `scipy.io.loadmat` to a more usable structure of numpy arrays, partially grouped in dictionaries, for f urther processing. 10-min datapackages are condensed into one sample described by th e mean, std, min and max of that package, unless `full_detail` is used.

```
Parameters
-----
print_data_structure : bool, default False
Print the structure of the original data. Primarily used for developement and bug-fixing
```

delete_data_after_import : bool, default True
 Delete original data from memory after import to free up memory
ignore_nans : bool, default True

Ignores nans when calculating mean, std, min and max, using the remaining no n-nan values in the 10-min data package for the calculations, instead of setting the value representing the whole 10-min data package to nan. This results in the return of more non-nan values, decreasing data loss during cleaning, but increasing import time.

rename_H20_acc : bool, default True

Rename accelerometers H20 to H24, as there seems to be a systematic error in the MATLAB files.

replace_invalid : bool, default True

Replace invalid sensor readings (outside of technical sensor range) with nan during import. Allows to retain more data during data cleaning with sleightly higher import time.

full_detail : bool, default False

Keep full detail of data, sampled at 50Hz instead of resampling to every 10m in. It is recommended to not use this for more than 1 day of data at a time. Note: T he values are represented as _mean arrays, although no mean is calculated. Not all f unctions of this class are designed to work with this form of data, but it allows mo re detailed insights in special cases

H ... TopBottom : bool, default True

Select which part of the data should be imported or generated during import. Only select the measurement types you are interested in to keep import times lower.

```
See Also
-----
`convert_MATLAB`
`define_units`
```

Note that it is alternatively possible to load the data from a previously saved analysis using dill.load.

```
LFB.load_data(print_data_structure=False,delete_data_after_import=True,replace_inval
# LFB = dill.load(open(file_path+file_names[0][:-4]+'-'+file_names[-1][:-4],'rb')) #
```

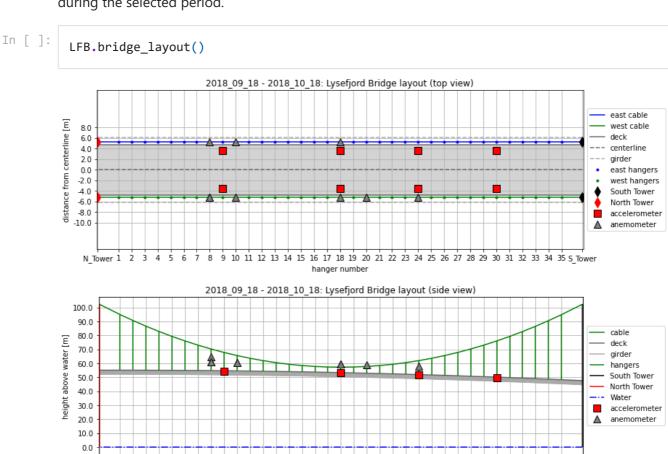
```
Day 1 : 2018_09_18
Day 2 : 2018_09_19
Day 3 : 2018_09_20
Day 4 : 2018_09_21
Day 5 : 2018_09_22
Day 6: 2018 09 23
Day 7: 2018 09 24
Day 8 : 2018 09 25
Day 9 : 2018_09_26
Day 10 : 2018_09_27
Day 11 : 2018_09_28
Day 12: 2018 09 29
Day 13 : 2018_09_30
Day 14 : 2018_10_01
Day 15 : 2018 10 02
Day 16 : 2018 10 03
Day 17 : 2018 10 04
Day 18 : 2018 10 05
Day 19 : 2018_10_06
Day 20 : 2018_10_07
Day 21 : 2018_10_08
Day 22 : 2018_10_10
Day 23 : 2018_10_11
Day 24 : 2018 10 12
Day 25 : 2018_10_13
```

Day 26 : 2018_10_14
Day 27 : 2018_10_15
Day 28 : 2018_10_16
Day 29 : 2018_10_17
Day 30 : 2018_10_18

Bridge layout

The names of active anemometers can be obtained from <code>anemo_names</code> .

The bridge_layout method creates a layout of the active instrumentation on the bridge during the selected period.



Traffic classification

The find_traffic method classifies each datapoint to be traffic- (1) or wind-dominated (0) using the *max_by_std* criteria on vertical accelerations. This can be used to filter the data. Note that this method is not available in full_detail mode. Also note that the keyword cleaned is set to *False*, as we are dealing with un-processed (un-cleaned) data.

N_Tower 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25 26 27 28 29 30 31 32 33 34 35 5_Tower

```
if LFB.full_detail==False:
    LFB.find_traffic(traffic_thresh=8,cleaned=False)
    print('Traffic percentage:',np.round(100*np.count_nonzero(LFB.traffic)/len(LFB.t
```

Traffic percentage: 68.24 %

Filter

The filter_data method allows filtering the data in various ways. Note that multiple filters can be combined in different ways aswell. It is good practise to add a remark to the title of plots that use filtered data using the title_suffix keyword. Uncomment one of the filter lines below to see it in effect, or use it as a template to create your own filter.

```
In [ ]:
    filter_idxs = np.arange(len(LFB.time_array)); title_suffix = ''
    if LFB.full_detail:
        title_suffix+= ' - full detail'
    # filter_idxs = LFB.filter_data(LFB.anemo['H_mean'],prior_idxs=filter_idxs,hp_cutoff
    # filter_idxs = LFB.filter_data(LFB.anemo['AOA_mean'],prior_idxs=filter_idxs,hp_cuto
    # filter_idxs = LFB.filter_data(LFB.traffic,prior_idxs=filter_idxs,zeros=True,mode='
```

Plot un-processed data

Below we will examin how to plot some of the un-processed (un-cleaned) time series data.

Setting your keys_of_interest beforehand allows batch-post-processing in the visualisation of data using for-loops over all keys and if-conditions on the name of the keys.

```
In [ ]:
    keys_of_interest = ['H_mean','H_max','H_turb','W_mean','W_turb','AOA_mean','AOA_std'
    # keys_of_interest = ['H_mean','Aoz_C_mean','Aoz_C_max_by_std','Aoz_C_st
    # keys_of_interest = ['H_mean','Aoz_C_mean','Aoz_C_max_by_std']
```

Time settings

The method feature_time is used to to initialize time series in days, hours, minutes and seconds for your data, starting at the first datapoint. Note that the keyword cleaned is set to False, as we are dealing with un-processed (un-cleaned) data.

You can set your prefered timescale and time_of_interest prior to batch-post-processing.

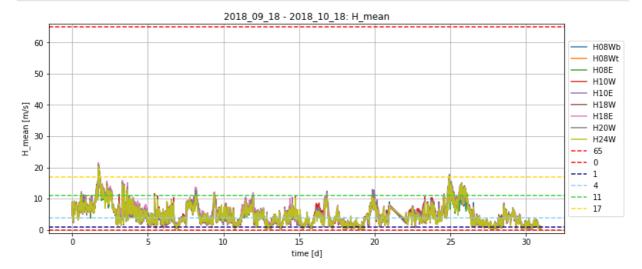
```
In []:
    LFB.feature_time(cleaned=False) #Initiate time series for un-cleaned data.
    timescale='days' #Change this variable to 'days', 'hours', 'minutes' or 'seconds' to
    if timescale=='days':
        plot_time=LFB.days
        plot_time_label = 'time [d]'
    elif timescale=='hours':
        plot_time=LFB.hours
        plot_time_label = 'time [h]'
    elif timescale=='minutes':
        plot_time=LFB.minutes
        plot_time_label = 'time [min]'
    elif timescale=='seconds':
        plot_time=LFB.seconds
```

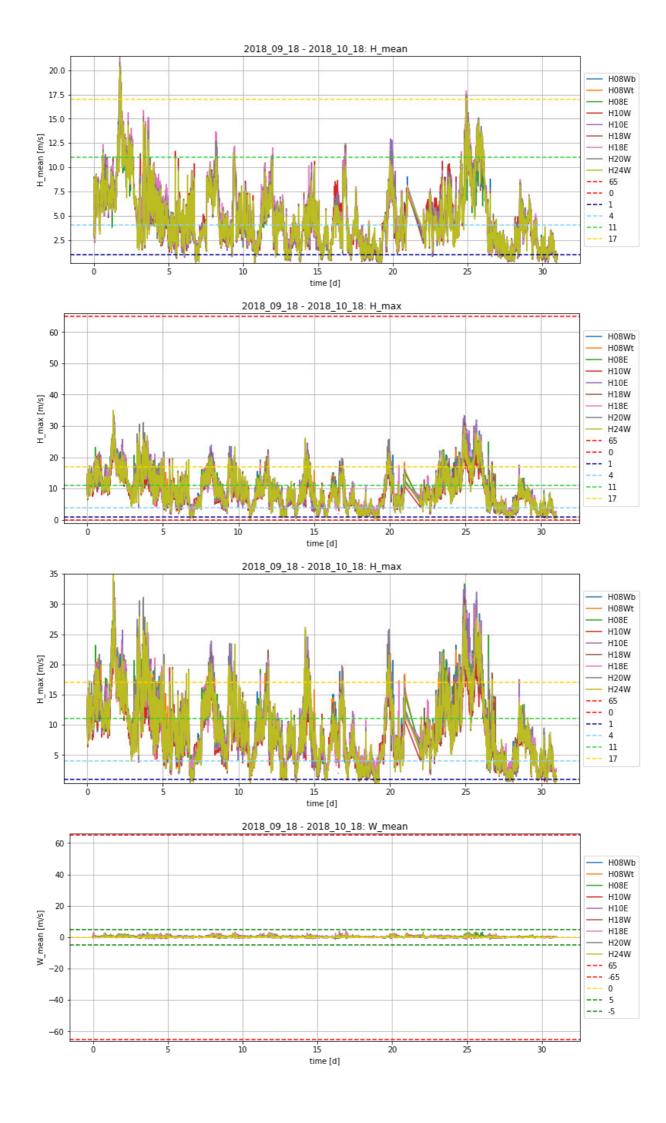
```
plot_time_label = 'time [s]'
# time_of_interest=(0,24) #use this line instead of the one below to zoom in on deta
time_of_interest=(None,None) #default
```

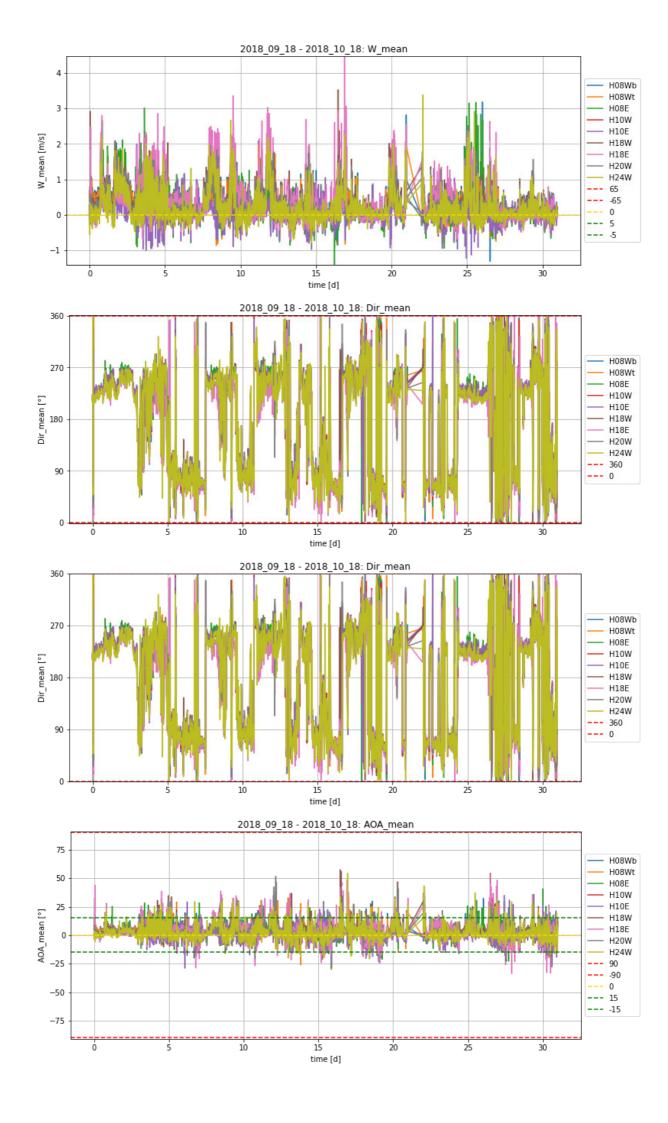
Anemometers

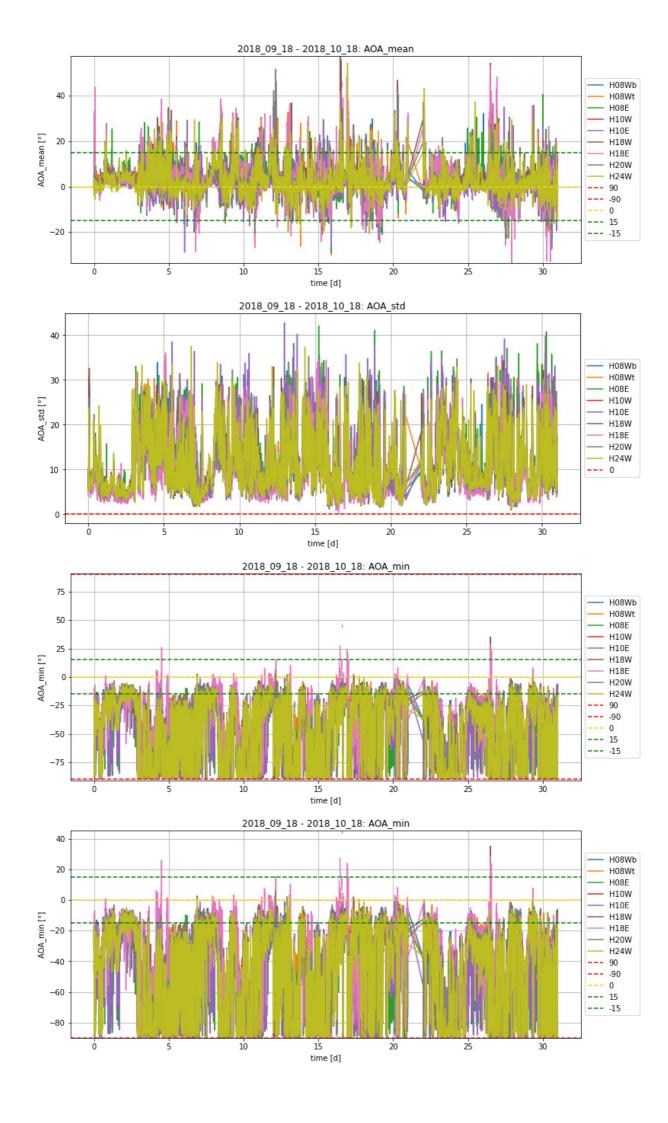
Below is an example for batch post-processing of **anemometer** data using a *for-loop* and *if-statements* on the *keys* previously defined by keys_of_interest. This allows to set specific *plot parameters* in the plot_data method for different *keys*. The names of anemometers that are not of interest can be given to the ignored_anemos keyword as a list.

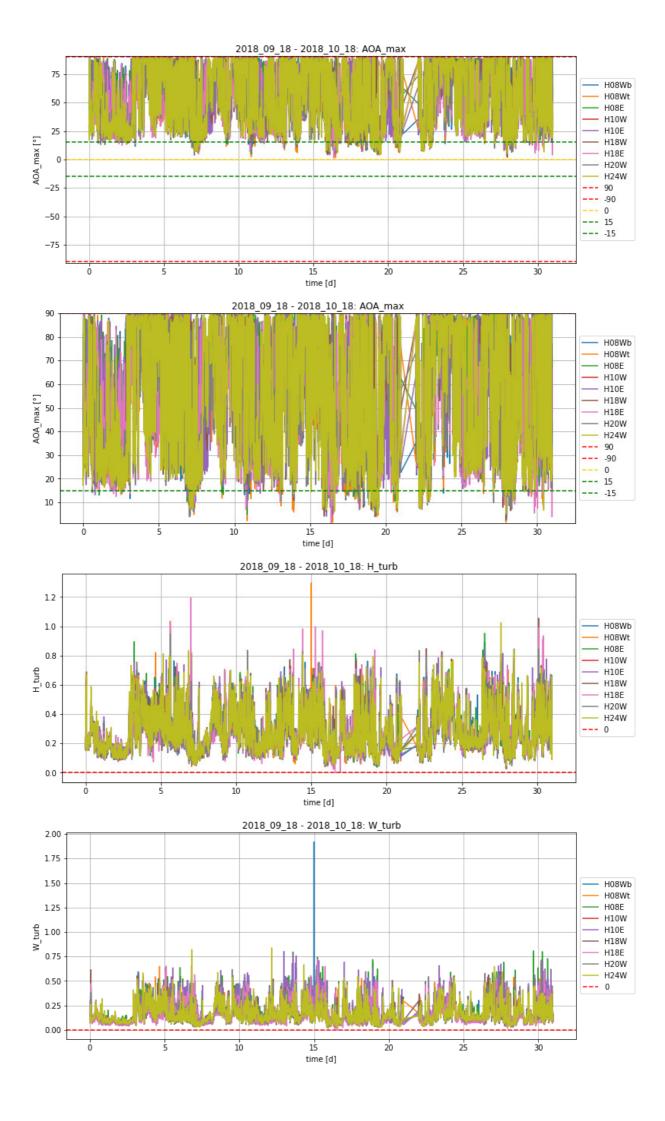
```
In [ ]:
         ignored_anemos = []
         for key in LFB.anemo.keys():
             if key in keys_of_interest:
                 if key.startswith('H_m'):
                     LFB.plot_data(plot_time[filter_idxs], LFB.anemo[key].T[filter_idxs].T,yla
                     LFB.plot_data(plot_time[filter_idxs], LFB.anemo[key].T[filter_idxs].T,yla
                 elif key.startswith('Dir_m'):
                     LFB.plot_data(plot_time[filter_idxs], LFB.anemo[key].T[filter_idxs].T,yla
                     LFB.plot_data(plot_time[filter_idxs], LFB.anemo[key].T[filter_idxs].T,yla
                 elif key.startswith('W_m'):
                     LFB.plot_data(plot_time[filter_idxs], LFB.anemo[key].T[filter_idxs].T,yla
                     LFB.plot_data(plot_time[filter_idxs], LFB.anemo[key].T[filter_idxs].T,yla
                 elif key.startswith('Vx_m') or key.startswith('Vy_m'):
                     LFB.plot_data(plot_time[filter_idxs], LFB.anemo[key].T[filter_idxs].T,yla
                     LFB.plot_data(plot_time[filter_idxs], LFB.anemo[key].T[filter_idxs].T,yla
                 elif key.startswith('AOA_m'):
                     LFB.plot_data(plot_time[filter_idxs], LFB.anemo[key].T[filter_idxs].T,yla
                     LFB.plot_data(plot_time[filter_idxs], LFB.anemo[key].T[filter_idxs].T,yla
                 elif key.startswith('AOI_m'):
                     LFB.plot_data(plot_time[filter_idxs], LFB.anemo[key].T[filter_idxs].T,yla
                     LFB.plot data(plot time[filter idxs], LFB.anemo[key].T[filter idxs].T, yla
                 else:
                     LFB.plot_data(plot_time[filter_idxs], LFB.anemo[key].T[filter_idxs].T,yla
```

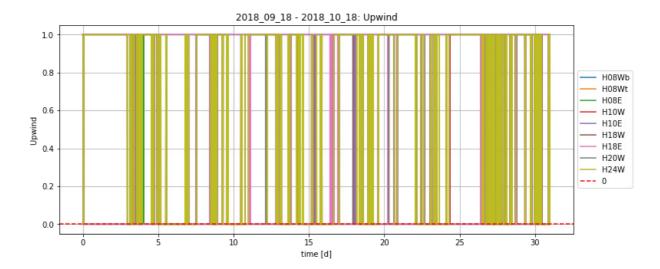








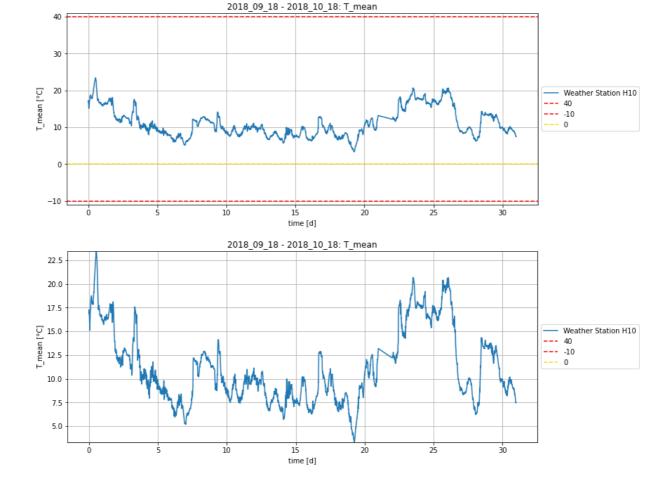


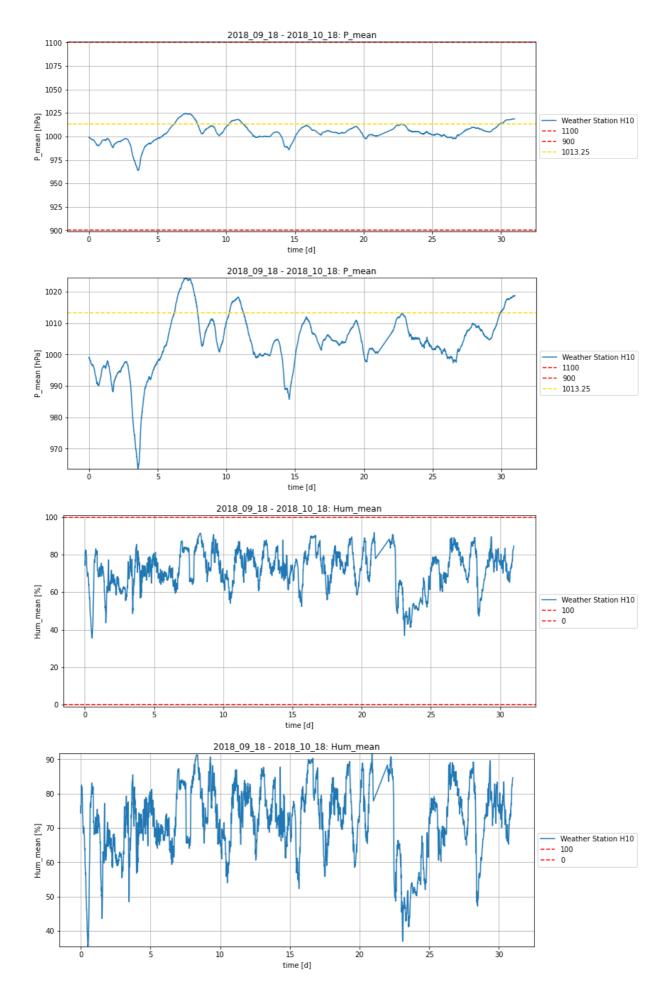


Weather

Similarly the weather data from the weather station on Hanger 10 can be plotted.

```
for key in LFB.weather.keys():
    if key in keys_of_interest:
        if key.startswith('Hum_mean'):
            LFB.plot_data(plot_time[filter_idxs], LFB.weather[key][filter_idxs], ylabe
            LFB.plot_data(plot_time[filter_idxs], LFB.weather[key][filter_idxs], ylabe
        elif key.startswith('T_mean'):
            LFB.plot_data(plot_time[filter_idxs], LFB.weather[key][filter_idxs], ylabe
            LFB.plot_data(plot_time[filter_idxs], LFB.weather[key][filter_idxs], ylabe
        elif key.startswith('P_mean'):
            LFB.plot_data(plot_time[filter_idxs], LFB.weather[key][filter_idxs], ylabe
            LFB.plot_data(plot_time[filter_idxs], LFB.weather[key][filter_idxs], ylabe
```





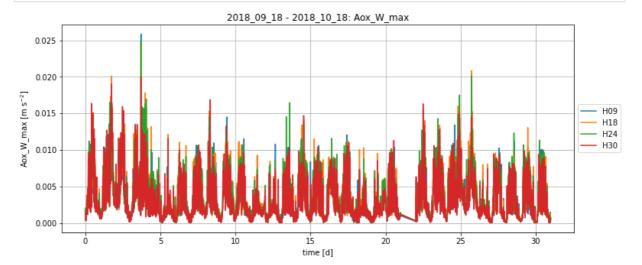
Accelerometers

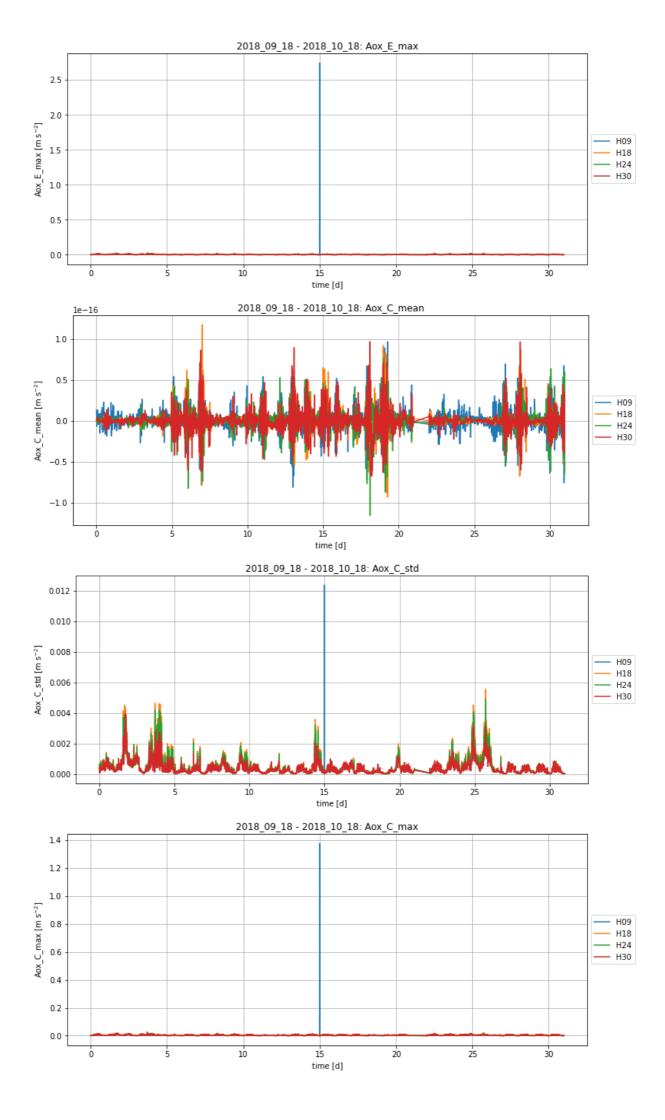
Similarly the data of **accelerometers** can be plotted.

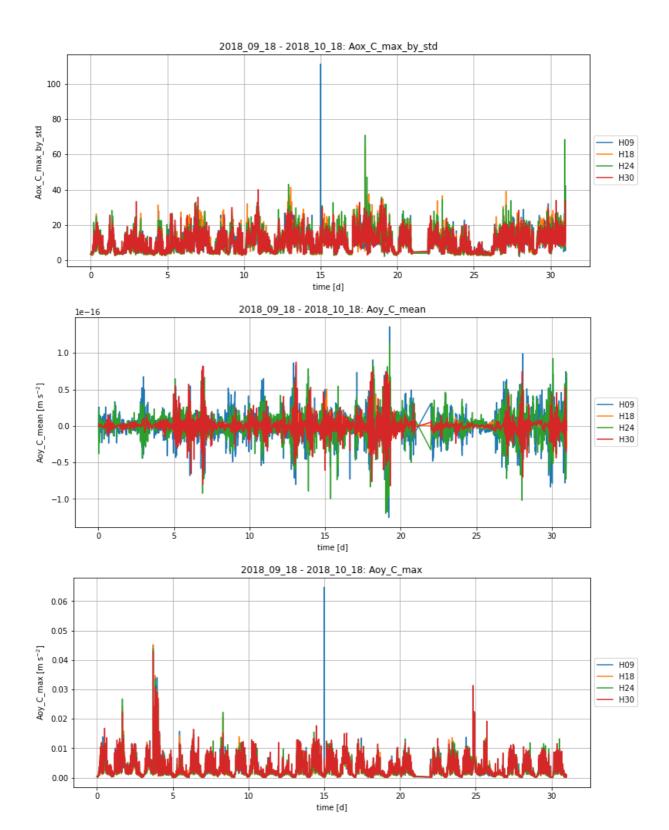
Note how the status of the full_detail state of the BridgeData class is used to perform additional analysis when using the full 50Hz sample rate data. The full_detail mode has to be enabled during the import of the data in the load_data method.

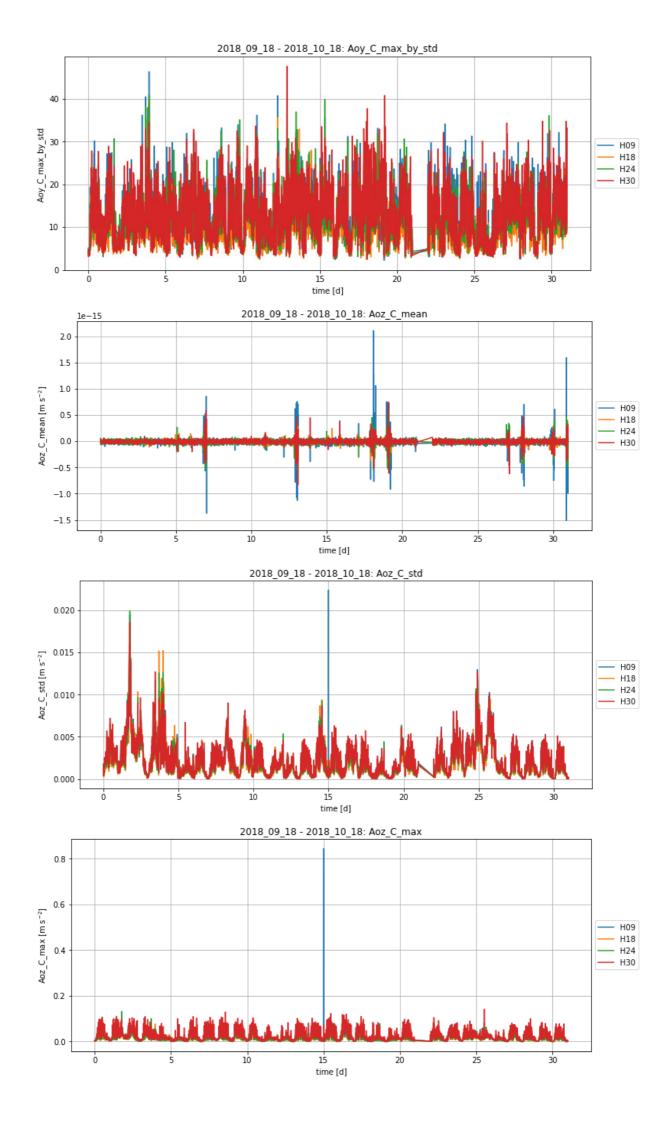
Caution: It is recommended to only use the full_detail mode on **one day** of data that you have previously singled out from a larger dataset for detailed analysis. This is because of the large ammount of data that needs to be processed (4.32 million datapoints per sensor for each day of data)..

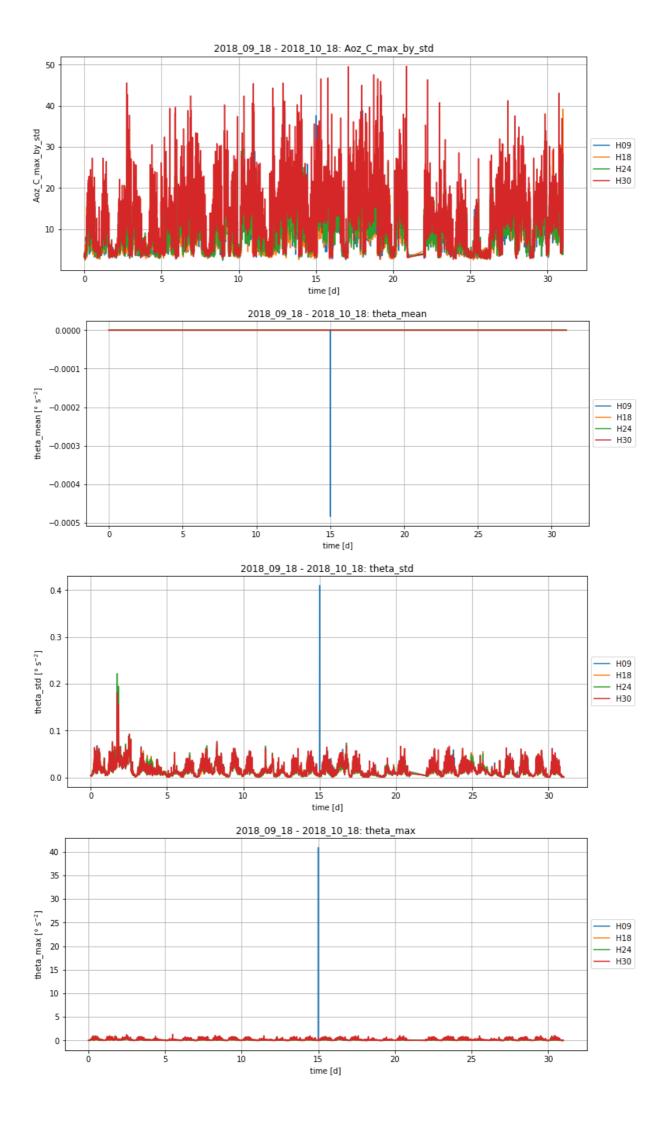
```
In [ ]:
         ignored acc = []
         for key in LFB.acc.keys():
             if key in keys_of_interest:
                 if key == 'Aoz_C_mean':
                     if LFB.full_detail:
                         LFB.plot_data(plot_time[filter_idxs], LFB.acc[key].T[filter_idxs].T,y
                         for sensor_id, sensor in enumerate(LFB.acc_names):
                             if sensor not in ignored_acc:
                                 if type(time of interest[0]) == type(None) and type(time of
                                      Aoz_C_max = LFB.acc['Aoz_C_mean'][sensor_id][filter_idxs
                                      Aoz_C_std = LFB.acc['Aoz_C_mean'][sensor_id][filter_idxs
                                 elif type(time_of_interest[0]) != type(None) and type(time_d
                                      Aoz_C_max = LFB.acc['Aoz_C_mean'][sensor_id][filter_idxs
                                      Aoz_C_std = LFB.acc['Aoz_C_mean'][sensor_id][filter_idxs
                                 elif type(time_of_interest[0]) == type(None) and type(time_o
                                      Aoz_C_max = LFB.acc['Aoz_C_mean'][sensor_id][filter_idxs
                                      Aoz_C_std = LFB.acc['Aoz_C_mean'][sensor_id][filter_idxs
                                 elif type(time of interest[0]) != type(None) and type(time d
                                      Aoz_C_max = LFB.acc['Aoz_C_mean'][sensor_id][filter_idxs
                                      Aoz_C_std = LFB.acc['Aoz_C_mean'][sensor_id][filter_idxs
                                 print(LFB.acc names[sensor id])
                                 print('Aoz_C_max =',np.round(Aoz_C_max,2),'\nAoz_C_std =',np
                     else:
                         LFB.plot_data(plot_time[filter_idxs], LFB.acc[key].T[filter_idxs].T,y
                 else:
                     LFB.plot_data(plot_time[filter_idxs], LFB.acc[key].T[filter_idxs].T,ylabe
```

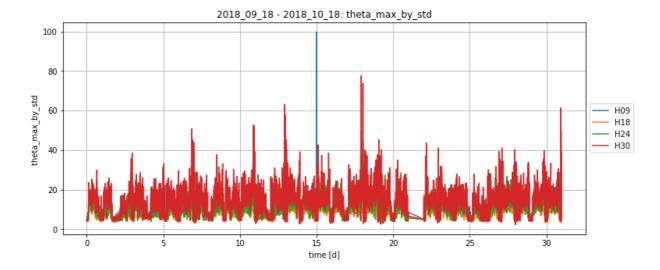






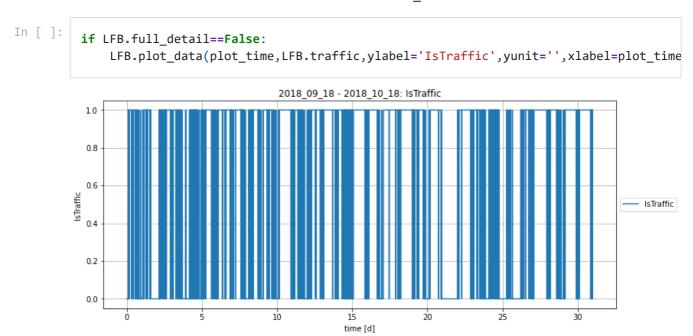






Traffic

Below is a visualisation of the traffic classification previously created using the find_traffic method. Note that this method is not available in full_detail mode.



Clean the data

The clean_data method is used to remove 'invalid' sensors, that produce too much invalid data, as defined by the threshold keyword and remove invalid data from the remaining sensors. Note that some data cleaning already takes place during the import of the data if the replace_invalid keyword in the load_data method is set to *True*.

```
In [ ]:
         LFB.clean_data(threshold=0.5,detailed_report=True)
        H_mean all sensors deemed ok
        H std all sensors deemed ok
        H min all sensors deemed ok
        H_max all sensors deemed ok
        W_mean ok sensors: ['H08Wb' 'H08Wt' 'H08E' 'H10E' 'H18W' 'H18E' 'H20W' 'H24W']
        W_mean invalid sensors: ['H10W']
        W_std ok sensors: ['H08Wb' 'H08Wt'
                                           'H08E' 'H10E'
                                                          'H18W'
                                                                 'H18E'
                                                                         'H20W'
                                                                                'H24W']
        W_std invalid sensors: ['H10W']
        W_min ok sensors: ['H08Wb' 'H08Wt' 'H08E' 'H10E' 'H18W' 'H18E' 'H20W' 'H24W']
```

```
W_min invalid sensors: ['H10W']
W_max ok sensors: ['H08Wb' 'H08Wt' 'H08E' 'H10E' 'H18W' 'H18E' 'H20W' 'H24W']
W_max invalid sensors: ['H10W']
Vx_mean all sensors deemed ok
Vx std all sensors deemed ok
Vx_min all sensors deemed ok
Vx_max all sensors deemed ok
Vy_mean all sensors deemed ok
Vy_std all sensors deemed ok
Vy_min all sensors deemed ok
Vy_max all sensors deemed ok
Dir_mean all sensors deemed ok
Dir_std all sensors deemed ok
Dir min all sensors deemed ok
Dir_max all sensors deemed ok
AOA_mean ok sensors: ['H08Wb' 'H08Wt' 'H08E' 'H10E' 'H18W' 'H18E' 'H20W' 'H24W']
AOA_mean invalid sensors: ['H10W']
AOA_std ok sensors: ['H08Wb' 'H08Wt' 'H08E' 'H10E' 'H18W' 'H18E' 'H20W' 'H24W']
AOA_std invalid sensors: ['H10W']
AOA_min ok sensors: ['H08Wb' 'H08Wt' 'H08E' 'H10E' 'H18W' 'H18E' 'H20W' 'H24W']
AOA_min invalid sensors: ['H10W']
AOA_max ok sensors: ['H08Wb' 'H08Wt' 'H08E' 'H10E' 'H18W' 'H18E' 'H20W' 'H24W']
AOA_max invalid sensors: ['H10W']
H_turb ok sensors: ['H08Wb' 'H08Wt' 'H08E' 'H10E' 'H18W' 'H18E' 'H20W' 'H24W']
H_turb invalid sensors: ['H10W']
W_turb ok sensors: ['H08Wb' 'H08Wt' 'H08E' 'H10E' 'H18W' 'H18E' 'H20W' 'H24W']
W_turb invalid sensors: ['H10W']
Vx_turb ok sensors: ['H08Wb' 'H08Wt' 'H08E' 'H10E' 'H18W' 'H18E' 'H20W' 'H24W']
Vx_turb invalid sensors: ['H10W']
Vy_turb ok sensors: ['H08Wb' 'H08Wt' 'H08E' 'H10E' 'H18W' 'H18E' 'H20W' 'H24W']
Vy turb invalid sensors: ['H10W']
Upwind all sensors deemed ok
Downwind all sensors deemed ok
Hanger_num all sensors deemed ok
y_pos all sensors deemed ok
West all sensors deemed ok
East all sensors deemed ok
Top all sensors deemed ok
Bottom all sensors deemed ok
H mean all sensors deemed ok
H_std all sensors deemed ok
H min all sensors deemed ok
H max all sensors deemed ok
W_mean ok sensors: ['H08Wb' 'H08Wt' 'H08E' 'H10E' 'H18W' 'H18E' 'H20W' 'H24W']
W_mean invalid sensors: ['H10W']
W_std ok sensors: ['H08Wb' 'H08Wt' 'H08E' 'H10E' 'H18W' 'H18E' 'H20W' 'H24W']
W_std invalid sensors: ['H10W']
W min ok sensors: ['H08Wb' 'H08Wt' 'H08E' 'H10E' 'H18W' 'H18E' 'H20W' 'H24W']
W_min invalid sensors: ['H10W']
W_max ok sensors: ['H08Wb' 'H08Wt' 'H08E' 'H10E' 'H18W' 'H18E' 'H20W' 'H24W']
W max invalid sensors: ['H10W']
Vx_mean all sensors deemed ok
Vx_std all sensors deemed ok
Vx_min all sensors deemed ok
Vx_max all sensors deemed ok
Vy mean all sensors deemed ok
Vy std all sensors deemed ok
Vy_min all sensors deemed ok
Vy max all sensors deemed ok
Dir mean all sensors deemed ok
Dir_std all sensors deemed ok
Dir_min all sensors deemed ok
Dir max all sensors deemed ok
AOA_mean ok sensors: ['H08Wb' 'H08Wt' 'H08E' 'H10E' 'H18W' 'H18E' 'H20W' 'H24W']
```

```
AOA_mean invalid sensors: ['H10W']
AOA_std ok sensors: ['H08Wb' 'H08Wt' 'H08E' 'H10E' 'H18W' 'H18E' 'H20W' 'H24W']
AOA std invalid sensors: ['H10W']
AOA_min ok sensors: ['H08Wb' 'H08Wt' 'H08E' 'H10E' 'H18W' 'H18E' 'H20W' 'H24W']
AOA min invalid sensors: ['H10W']
AOA_max ok sensors: ['H08Wb' 'H08Wt' 'H08E' 'H10E' 'H18W' 'H18E' 'H20W' 'H24W']
AOA max invalid sensors: ['H10W']
H turb ok sensors: ['H08Wb' 'H08Wt' 'H08E' 'H10E' 'H18W' 'H18E' 'H20W' 'H24W']
H_turb invalid sensors: ['H10W']
W_turb ok sensors: ['H08Wb' 'H08Wt' 'H08E' 'H10E' 'H18W' 'H18E' 'H20W' 'H24W']
W turb invalid sensors: ['H10W']
Vx_turb ok sensors: ['H08Wb' 'H08Wt' 'H08E' 'H10E' 'H18W' 'H18E' 'H20W' 'H24W']
Vx turb invalid sensors: ['H10W']
Vy turb ok sensors: ['H08Wb' 'H08Wt' 'H08E' 'H10E' 'H18W' 'H18E' 'H20W' 'H24W']
Vy turb invalid sensors: ['H10W']
Upwind all sensors deemed ok
Downwind all sensors deemed ok
Hanger_num all sensors deemed ok
y_pos all sensors deemed ok
West all sensors deemed ok
East all sensors deemed ok
Top all sensors deemed ok
Bottom all sensors deemed ok
Aox_W_mean all sensors deemed ok
Aox_W_std all sensors deemed ok
Aox W min all sensors deemed ok
Aox_W_max all sensors deemed ok
Aox_W_max_by_std all sensors deemed ok
Aoy_W_mean all sensors deemed ok
Aoy_W_std all sensors deemed ok
Aoy W min all sensors deemed ok
Aoy W max all sensors deemed ok
Aoy_W_max_by_std all sensors deemed ok
Aox_E_mean all sensors deemed ok
Aox E_std all sensors deemed ok
Aox_E_min all sensors deemed ok
Aox_E_max all sensors deemed ok
Aox_E_max_by_std all sensors deemed ok
Aoy E mean all sensors deemed ok
Aoy E std all sensors deemed ok
Aoy_E_min all sensors deemed ok
Aoy E max all sensors deemed ok
Aoy E max by std all sensors deemed ok
Aox_C_mean all sensors deemed ok
Aox C std all sensors deemed ok
Aox_C_min all sensors deemed ok
Aox_C_max all sensors deemed ok
Aox C max by std all sensors deemed ok
Aoy C mean all sensors deemed ok
Aoy C std all sensors deemed ok
Aoy C min all sensors deemed ok
Aoy_C_max all sensors deemed ok
Aoy_C_max_by_std all sensors deemed ok
Aoz_C_mean all sensors deemed ok
Aoz C std all sensors deemed ok
Aoz_C_min all sensors deemed ok
Aoz C max all sensors deemed ok
Aoz C max by std all sensors deemed ok
theta mean all sensors deemed ok
theta std all sensors deemed ok
theta min all sensors deemed ok
theta_max all sensors deemed ok
theta max by std all sensors deemed ok
```

Hanger num all sensors deemed ok

```
y_pos all sensors deemed ok
West all sensors deemed ok
East all sensors deemed ok
Top all sensors deemed ok
Bottom all sensors deemed ok
Aox W mean all sensors deemed ok
Aox W std all sensors deemed ok
Aox W min all sensors deemed ok
Aox_W_max all sensors deemed ok
Aox_W_max_by_std all sensors deemed ok
Aoy W mean all sensors deemed ok
Aoy_W_std all sensors deemed ok
Aoy W min all sensors deemed ok
Aoy W max all sensors deemed ok
Aoy_W_max_by_std all sensors deemed ok
Aox E mean all sensors deemed ok
Aox_E_std all sensors deemed ok
Aox_E_min all sensors deemed ok
Aox_E_max all sensors deemed ok
Aox_E_max_by_std all sensors deemed ok
Aoy_E_mean all sensors deemed ok
Aoy E std all sensors deemed ok
Aoy E min all sensors deemed ok
Aoy_E_max all sensors deemed ok
Aoy_E_max_by_std all sensors deemed ok
Aox_C_mean all sensors deemed ok
Aox_C_std all sensors deemed ok
Aox_C_min all sensors deemed ok
Aox_C_max all sensors deemed ok
Aox_C_max_by_std all sensors deemed ok
Aoy C mean all sensors deemed ok
Aoy C std all sensors deemed ok
Aoy_C_min all sensors deemed ok
Aoy C_max all sensors deemed ok
Aoy_C_max_by_std all sensors deemed ok
Aoz_C_mean all sensors deemed ok
Aoz_C_std all sensors deemed ok
Aoz_C_min all sensors deemed ok
Aoz C max all sensors deemed ok
Aoz C max by std all sensors deemed ok
theta mean all sensors deemed ok
theta std all sensors deemed ok
theta min all sensors deemed ok
theta max all sensors deemed ok
theta_max_by_std all sensors deemed ok
Hanger_num all sensors deemed ok
y_pos all sensors deemed ok
West all sensors deemed ok
East all sensors deemed ok
Top all sensors deemed ok
Bottom all sensors deemed ok
H mean cummulative data loss: 0.39 %
H std cummulative data loss: 0.42 %
H min cummulative data loss: 0.42 %
H max cummulative data loss: 0.42 %
W mean cummulative data loss: 0.42 %
W std cummulative data loss: 0.42 %
W min cummulative data loss: 0.42 %
W max cummulative data loss: 0.42 %
Vx mean cummulative data loss: 0.42 %
Vx std cummulative data loss: 0.42 %
Vx min cummulative data loss: 0.42 %
Vx max cummulative data loss: 0.42 %
Vy mean cummulative data loss: 0.42 %
```

```
Vy_std cummulative data loss: 0.42 %
Vy_min cummulative data loss: 0.42 %
Vy max cummulative data loss: 0.42 %
Dir_mean cummulative data loss: 0.42 %
Dir_std cummulative data loss: 0.42 %
Dir_min cummulative data loss: 0.42 %
Dir max cummulative data loss: 0.42 %
AOA mean cummulative data loss: 0.42 %
AOA_std cummulative data loss: 0.42 %
AOA_min cummulative data loss: 0.42 %
AOA_max cummulative data loss: 0.42 %
H_turb cummulative data loss: 0.42 %
W turb cummulative data loss: 0.42 %
Vx turb cummulative data loss: 0.42 %
Vy_turb cummulative data loss: 0.42 %
Upwind cummulative data loss: 0.42 %
Downwind cummulative data loss: 0.42 %
Hanger_num cummulative data loss: 0.42 %
y_pos cummulative data loss: 0.42 %
West cummulative data loss: 0.42 %
East cummulative data loss: 0.42 %
Top cummulative data loss: 0.42 %
Bottom cummulative data loss: 0.42 %
Total data loss: 0.42 %
```

Save BridgeData state

dill.dump can be used to save the BridgeData class instance in its current state, including imported and processed data.

```
# Save the BridgeData class instance (incl. data)
dill.dump(LFB,file=open(LFB.file_path+LFB.file_names[0][:-4]+'-'+LFB.file_names[-1][
```

Load BridgeData state

dill.load can be used to load the previously saved BridgeData class instance in its respective state, at the time of saving, including imported and processed data. This is usefull when returning to the analysis of a larger dataset, as the long import process (load_data) can be skipped.

```
# Re-load the file.
LFB = dill.load(open(file_path+file_names[0][:-4]+'-'+file_names[-1][:-4],'rb'))
```

Traffic classification

The traffic classification needs to be re-done for processed (cleaned) data, by setting the cleaned keyword to *True* when using the find_traffic method.

```
if LFB.full_detail==False:
    LFB.find_traffic(traffic_thresh=8,cleaned=True)
    print('Traffic percentage:',np.round(100*np.count_nonzero(LFB.traffic_cleaned)/1
```

Traffic percentage: 68.15 %

Filter

Similarly to the traffic classification, filtering needs to be re-done for processed (cleaned) data, by providing the _cleaned data array to the filter_data method.

```
filter_idxs = np.arange(len(LFB.time_array_cleaned)); title_suffix = ' - cleaned'
if LFB.full_detail:
    title_suffix+= ' - full detail'
# filter_idxs = LFB.filter_data(LFB.anemo_cleaned['H_mean'],prior_idxs=filter_idxs,h
# filter_idxs = LFB.filter_data(LFB.anemo_cleaned['AOA_mean'],prior_idxs=filter_idxs
# filter_idxs = LFB.filter_data(LFB.traffic_cleaned,prior_idxs=filter_idxs,zeros=Tru
# filter_idxs = LFB.filter_data(LFB.anemo_cleaned['Dir_mean'][LFB.get_ok_sensor_ind(
# filter_idxs = LFB.filter_data(LFB.anemo_cleaned['AOA_mean'][LFB.get_ok_sensor_ind(
```

Plot cleaned data

Below you will find examples for plotting the *cleaned* time series data, similar to what was done in the plotting of the un-processed (un-cleaned) data.

Time settings

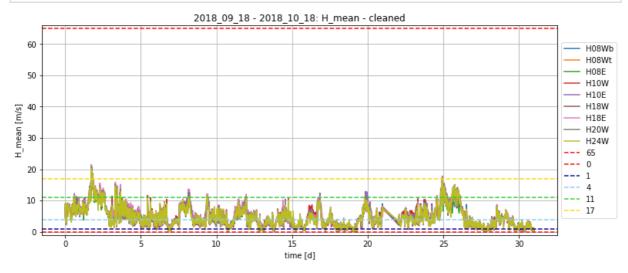
Similarly to the traffic classification, the time arrays need to be re-initialized for processed (cleaned) data, by setting the cleaned keyword to *True* when using the feature_time method.

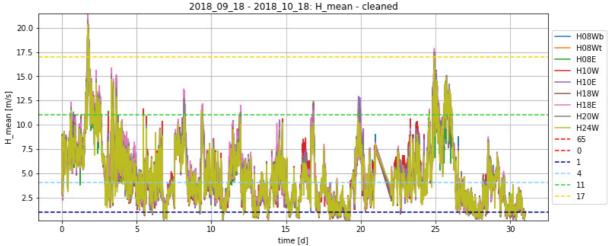
```
In [ ]:
         LFB.feature_time(cleaned=True) # Initialize time series for cleaned data.
         timescale='days' #Change this variable to 'days', 'hours', 'minutes' or 'seconds' to
         if timescale=='days':
             plot_time=LFB.days_cleaned
             plot_time_label = 'time [d]'
         elif timescale=='hours':
             plot_time=LFB.hours_cleaned
             plot_time_label = 'time [h]'
         elif timescale=='minutes':
             plot_time=LFB.minutes_cleaned
             plot_time_label = 'time [min]'
         elif timescale=='seconds':
             plot_time=LFB.seconds_cleaned
             plot_time_label = 'time [s]'
         # time of interest=(600,610) # Use this line instead of the one below to zoom in on
         time of interest=(None, None) # Default
```

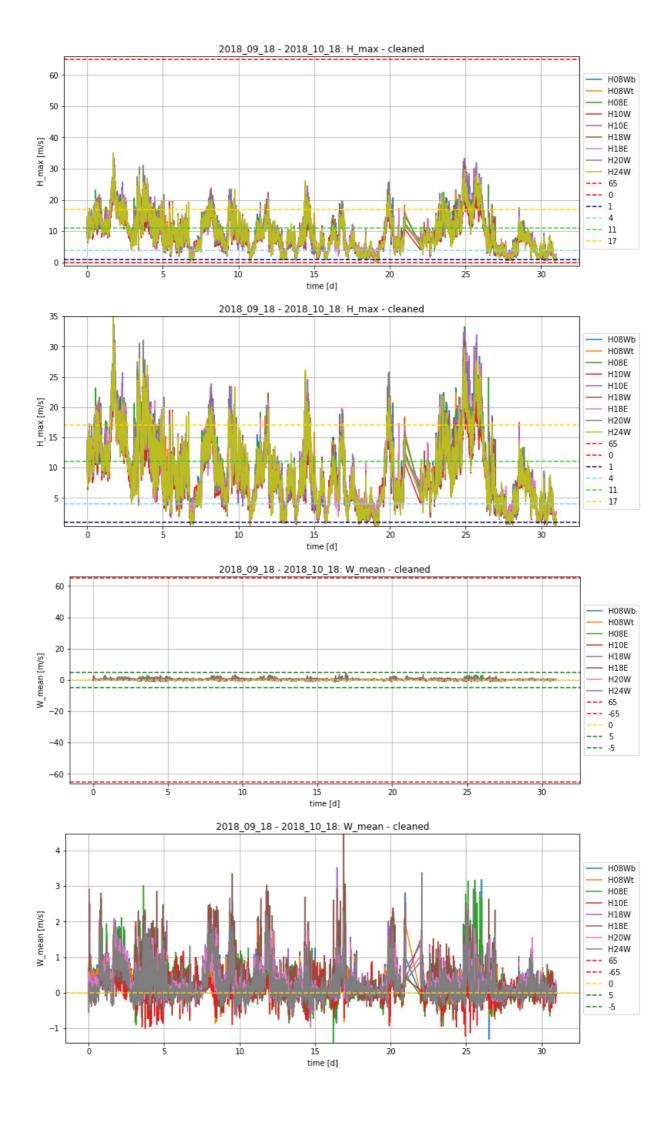
Anemometers

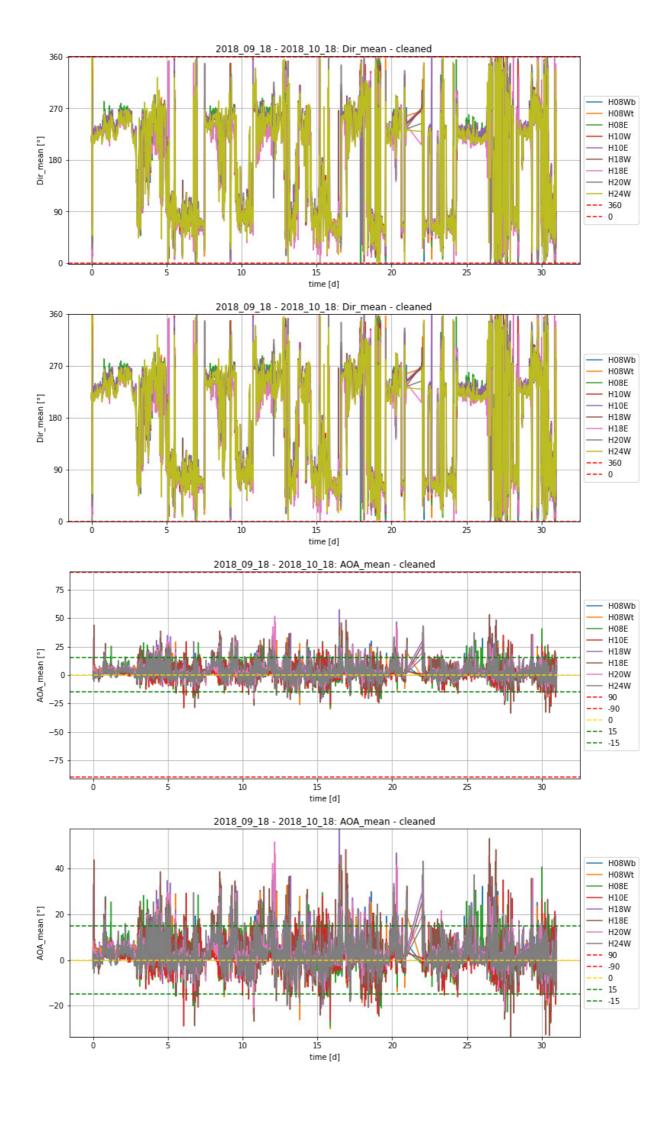
Below is an example for batch post-processing of **anemometer** data using a *for-loop* and *if-statements* on the *keys* previously defined by keys_of_interest. This allows to set specific *plot parameters* in the plot_data method for different *keys*. The names of anemometers that are not of interest can be given to the ignored_anemos keyword as a list.

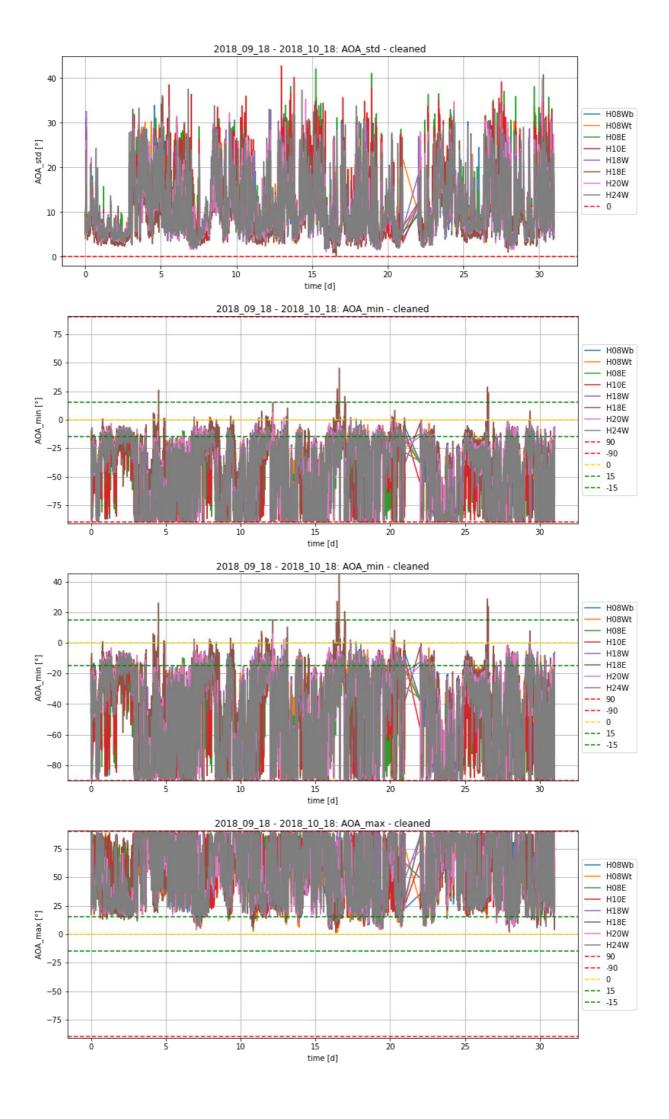
```
elif key.startswith('Dir_m'):
   LFB.plot_data(plot_time[filter_idxs], LFB.anemo_cleaned[key].T[filter_idx
    LFB.plot_data(plot_time[filter_idxs], LFB.anemo_cleaned[key].T[filter_idx
elif key.startswith('W_m'):
    LFB.plot data(plot time[filter idxs], LFB.anemo cleaned[key].T[filter idx
    LFB.plot_data(plot_time[filter_idxs], LFB.anemo_cleaned[key].T[filter_idx
elif key.startswith('Vx_m') or key.startswith('Vy_m'):
    LFB.plot_data(plot_time[filter_idxs], LFB.anemo_cleaned[key].T[filter_idx
    LFB.plot_data(plot_time[filter_idxs], LFB.anemo_cleaned[key].T[filter_idx
elif key.startswith('AOA_m'):
    LFB.plot_data(plot_time[filter_idxs], LFB.anemo_cleaned[key].T[filter_idx
    LFB.plot_data(plot_time[filter_idxs], LFB.anemo_cleaned[key].T[filter_idx
elif key.startswith('AOI_m'):
    LFB.plot_data(plot_time[filter_idxs], LFB.anemo_cleaned[key].T[filter_idx
    LFB.plot_data(plot_time[filter_idxs], LFB.anemo_cleaned[key].T[filter_idx
else:
    LFB.plot_data(plot_time[filter_idxs], LFB.anemo_cleaned[key].T[filter_idx
```

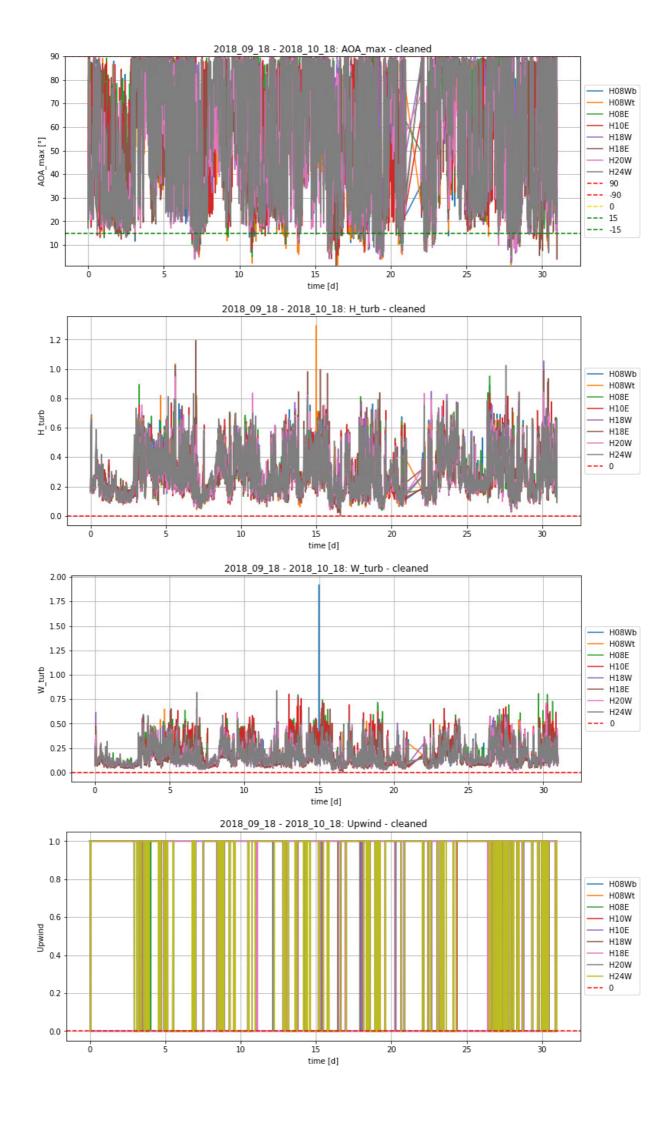










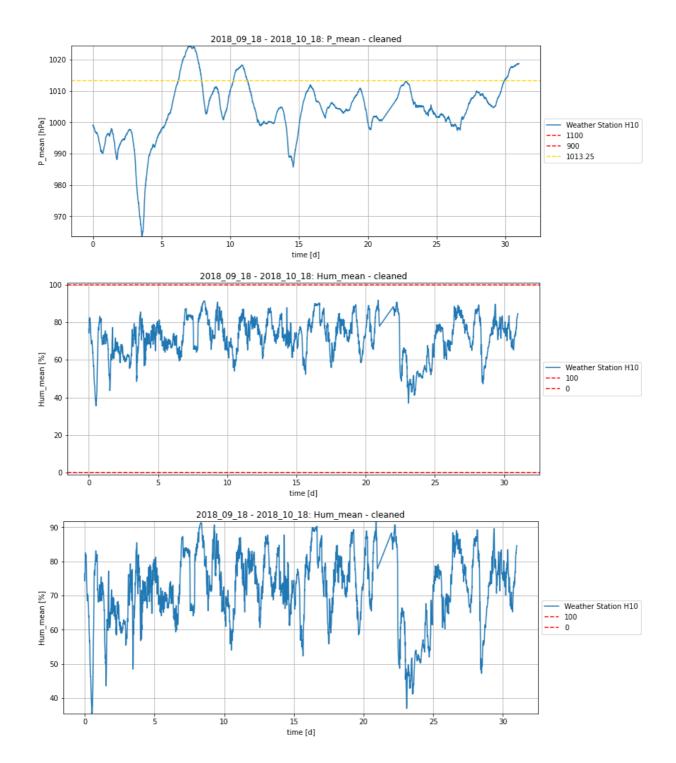


Weather

Similarly the weather data from the weather station on Hanger 10 can be plotted.

```
In [ ]:
           for key in LFB.weather_cleaned.keys():
                if key in keys_of_interest:
                     if key.startswith('Hum_mean'):
                          LFB.plot_data(plot_time[filter_idxs], LFB.weather_cleaned[key][filter_idx
                          LFB.plot_data(plot_time[filter_idxs], LFB.weather_cleaned[key][filter_idx
                     elif key.startswith('T_mean'):
                          LFB.plot_data(plot_time[filter_idxs], LFB.weather_cleaned[key][filter_idx
                          LFB.plot_data(plot_time[filter_idxs], LFB.weather_cleaned[key][filter_idx
                     elif key.startswith('P_mean'):
                          LFB.plot_data(plot_time[filter_idxs], LFB.weather_cleaned[key][filter_idx
                          LFB.plot_data(plot_time[filter_idxs],LFB.weather_cleaned[key][filter_idx
                                       2018 09 18 - 2018 10 18: T mean - cleaned
             40
             30
          T_mean [°C]
                                                                                                     Weather Station H10
                                                                                                  --- -10
                                                                                                     0
             10
             0
            -10
                                                      time [d]
                                       2018_09_18 - 2018_10_18: T_mean - cleaned
            20.0
            17.5
          <u></u> 15.0
                                                                                                     Weather Station H10
                                                                                                 --- 40
          12.5
                                                                                                 --- -10
                                                                                                  --- 0
            10.0
             7.5
            5.0
                                                      time [d]
                                        2018_09_18 - 2018_10_18: P_mean - cleaned
            1100
            1075
            1050
            1025
          P_mean [hPa]
                                                                                                     Weather Station H10
                                                                                                     1100
            1000
                                                                                                  --- 900
                                                                                                  --- 1013.25
            975
             950
            925
             900
                                          10
```

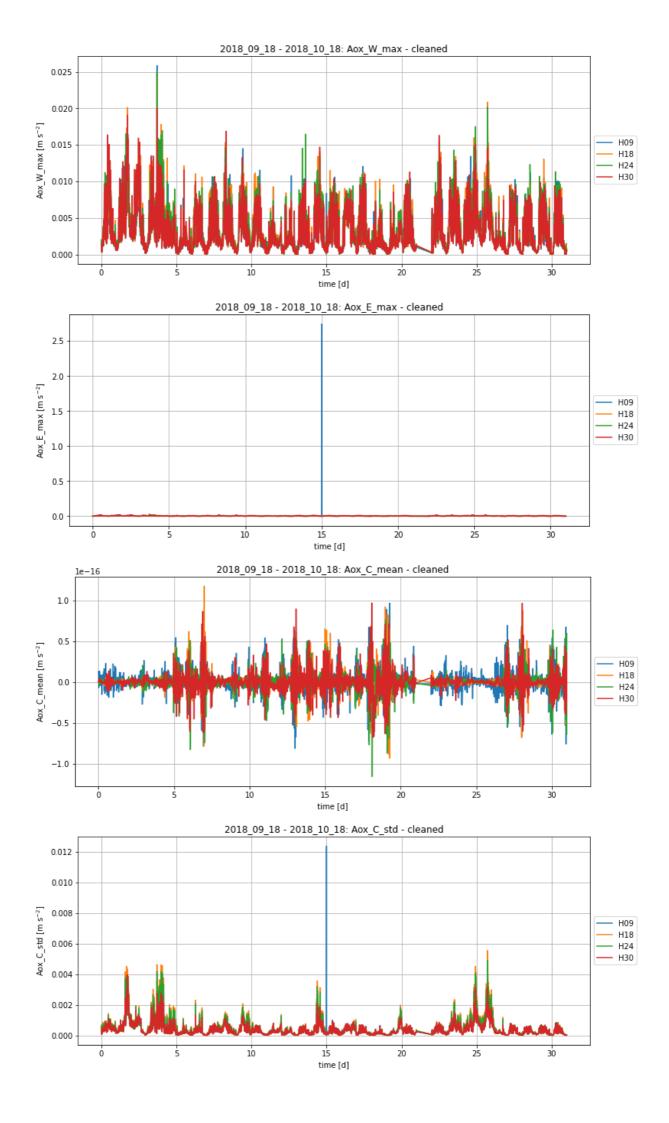
time [d]

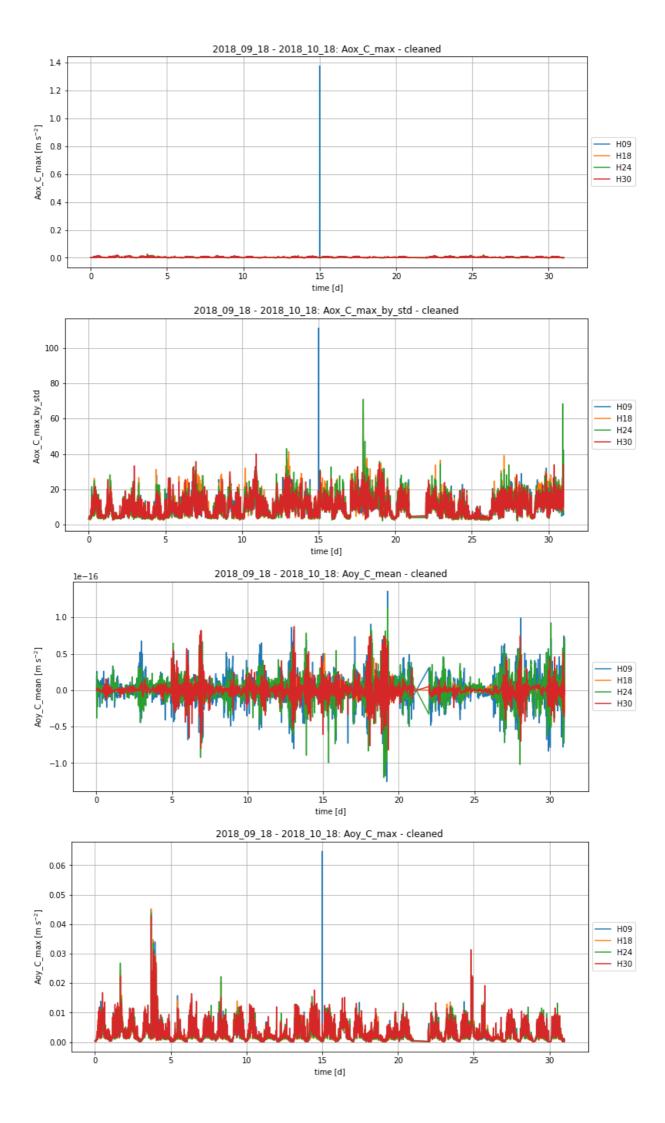


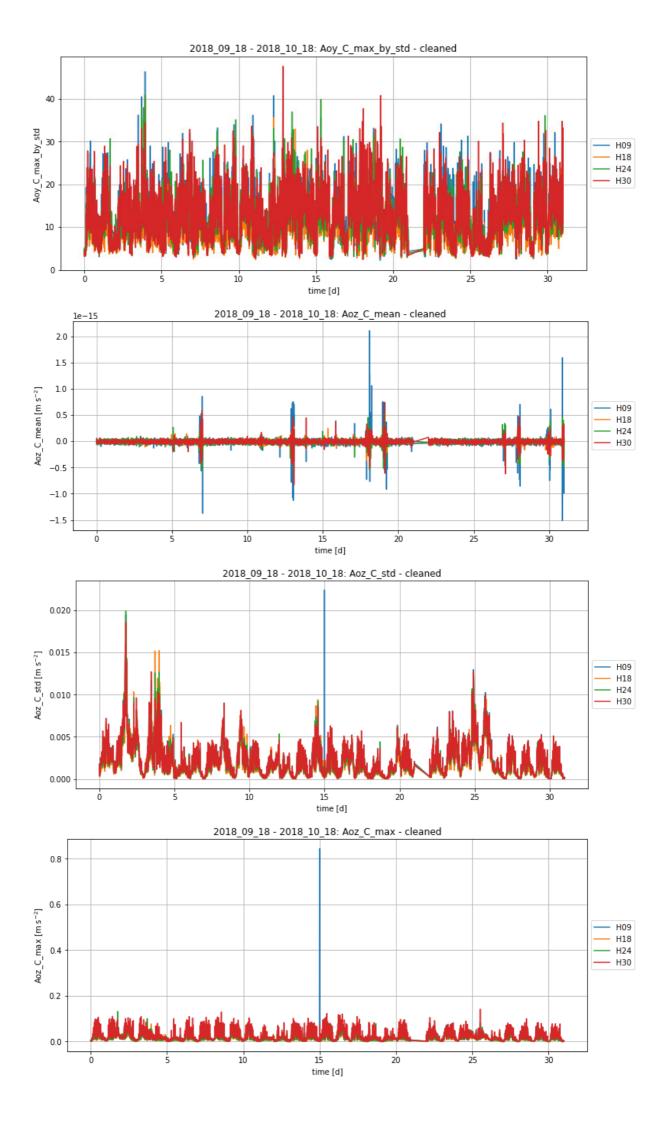
Accelerometers

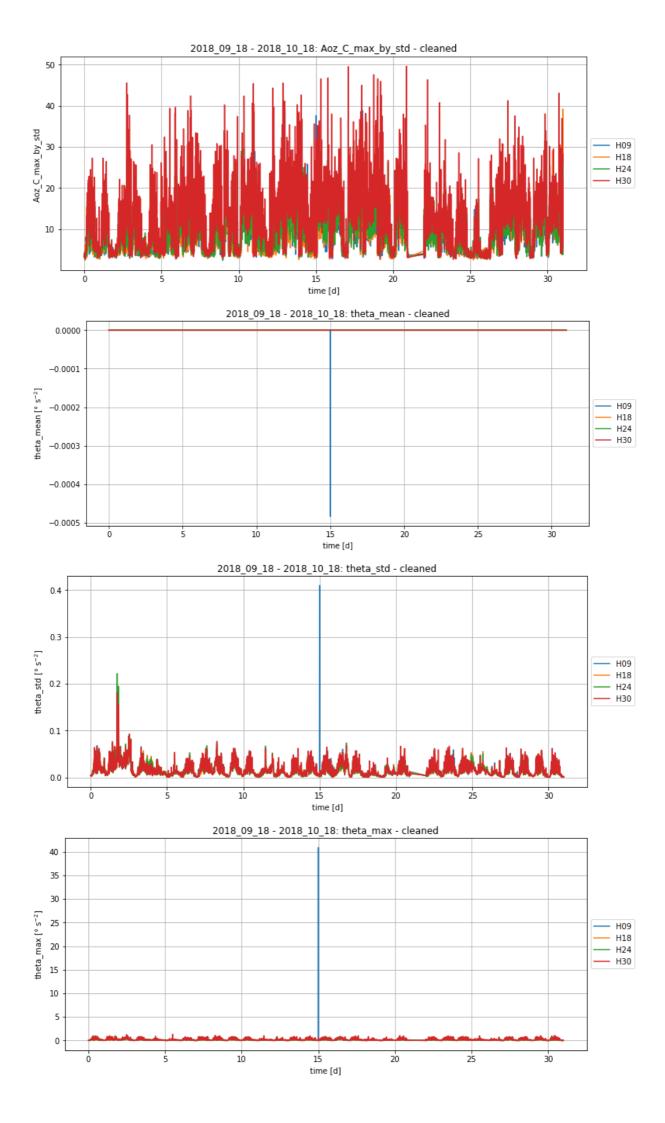
Similarly the accelerometer data can be plotted.

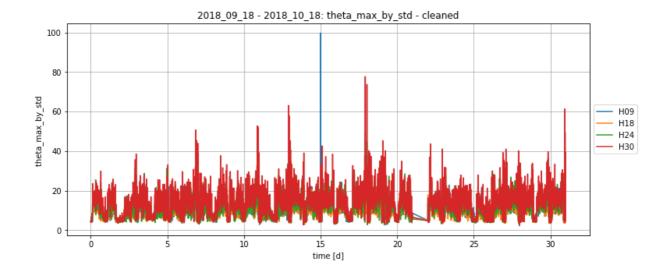
```
ignored_acc=[]
for key in LFB.acc_cleaned.keys():
    if key in keys_of_interest:
        LFB.plot_data(plot_time[filter_idxs], LFB.acc_cleaned[key].T[filter_idxs].T,y
```











Traffic

Below is a visualisation of the traffic classification previously created using the find_traffic method. Note that this method is not available in full detail mode.

Histograms

Below are some examples on creating histograms using the hist method. Note that, as in the time series plots above, filters can be applied using the filter_data method and keys_of_interest can be set.

```
In [ ]:
    filter_idxs = np.arange(len(LFB.time_array_cleaned)); title_suffix = ' - cleaned'
    # filter_idxs = LFB.filter_data(LFB.traffic_cleaned,prior_idxs=filter_idxs,zeros=Tru
    # filter_idxs = LFB.filter_data(LFB.anemo_cleaned['H_mean'],prior_idxs=filter_idxs,h
    # filter_idxs = LFB.filter_data(LFB.anemo_cleaned['Dir_mean'],prior_idxs=filter_idxs
    # filter_idxs = LFB.filter_data(LFB.anemo_cleaned['Dir_mean'],prior_idxs=filter_idxs
    # filter_idxs = LFB.filter_data(LFB.anemo_cleaned['Dir_mean'],prior_idxs=filter_idxs
    # filter_idxs = LFB.filter_data(LFB.anemo_cleaned['Dir_mean'],prior_idxs=filter_idxs
In [ ]:
    keys_of_interest = ['H_mean', 'H_max', 'W_mean', 'Vx_mean', 'Vy_mean', 'Dir_mean', 'H_turb
```

Anemometers

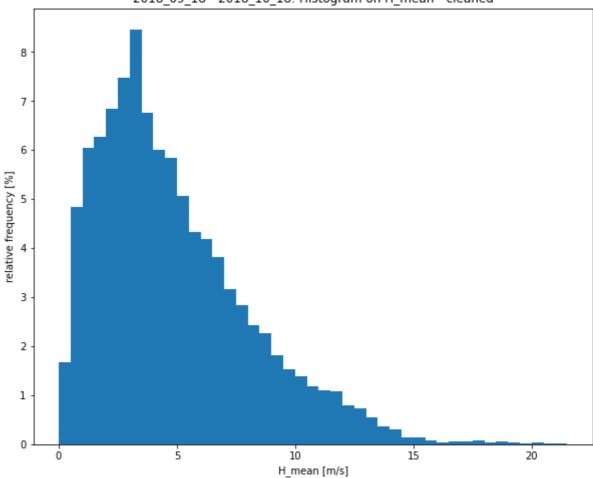
Below is an example of histograms on **anemometer** data. The structure of the batch-processing is similar to the time-series plots above.

Note how different bins are setup for the histograms of different types of measurements (*keys*) for the hist method.

Another usefull keyword is the split_sensors keyword, which when set to *True* creates a histogram for each *sensor* or combines them into a single histogram when set to *False*.

It is also possible to perform any kind of statistical analysis on the data using standard libraries like *numpy* or *scipy* or other 3rd-party libraries.

```
In [ ]:
         for key in LFB.anemo_cleaned.keys():
             if key in keys_of_interest:
                 if key.startswith('Dir_m'): # Adjust the bin width to 5° for directional dat
                     LFB.hist(LFB.anemo_cleaned[key].T[filter_idxs].T,xlabel=key,xunit=LFB.un
                 elif key.startswith('H_m'): # Adjust the bins for consistency.
                    LFB.hist(LFB.anemo_cleaned[key].T[filter_idxs].T,xlabel=key,xunit=LFB.un
                 elif key.endswith('_turb'): # Adjust the bins for consistency.
                     LFB.hist(LFB.anemo cleaned[key].T[filter idxs].T,xlabel=key,xunit=LFB.un
                 elif key.startswith('AOA_m'): # Adjust the bins for consistency.
                     LFB.hist(LFB.anemo_cleaned[key].T[filter_idxs].T,xlabel=key,xunit=LFB.un
                 else:
                     LFB.hist(LFB.anemo_cleaned[key].T[filter_idxs].T,xlabel=key,xunit=LFB.un
                 print('Statistics for', key, LFB.units[key], title_suffix)
                 print('----')
                 print('Mean:',np.round(np.mean(LFB.anemo_cleaned[key].T[filter_idxs].T),2))
                 print('Median:',np.round(np.median(LFB.anemo_cleaned[key].T[filter_idxs].T),
                 print('Percentile [10, 25, 75, 90]:',np.round(np.percentile(LFB.anemo_cleane
                 print('Minimum:',np.round(np.min(LFB.anemo_cleaned[key].T[filter_idxs].T),2)
                 print('Maximum:',np.round(np.max(LFB.anemo_cleaned[key].T[filter_idxs].T),2)
                 print('Variance:',np.round(np.var(LFB.anemo_cleaned[key].T[filter_idxs].T),2
                 print('Standard deviation:',np.round(np.std(LFB.anemo_cleaned[key].T[filter_
                 print('Skewness:',np.round(scipy.stats.skew(LFB.anemo_cleaned[key].T[filter_
                 print('Kurtosis:',np.round(scipy.stats.kurtosis(LFB.anemo cleaned[key].T[fil
```



Statistics for H_mean [m/s] - cleaned

Mann. 4 96

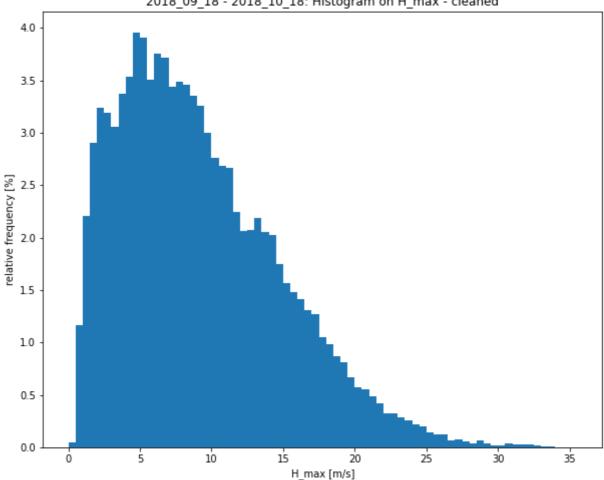
Mean: 4.86 Median: 4.13

Percentile [10, 25, 75, 90]: [1.29 2.45 6.64 9.46]

Minimum: 0.12 Maximum: 21.48 Variance: 10.52

Standard deviation: 3.24

Skewness: 1.07 Kurtosis: 1.19



Statistics for $H_max[m/s]$ - cleaned

_ . . .

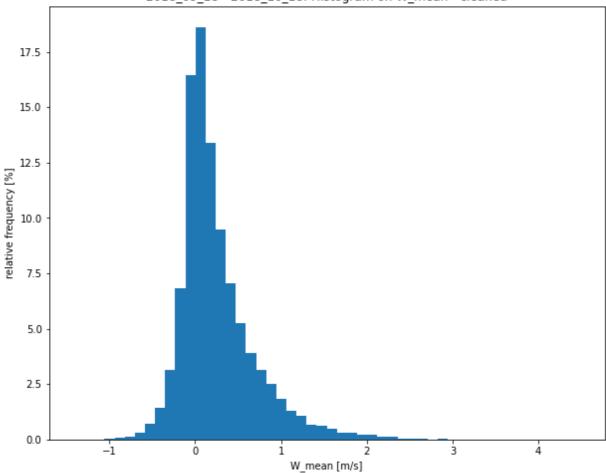
Mean: 9.17 Median: 8.2

Percentile [10, 25, 75, 90]: [2.55 4.78 12.74 17.07]

Minimum: 0.37 Maximum: 35.03 Variance: 31.59

Standard deviation: 5.62

Skewness: 0.79 Kurtosis: 0.33



Statistics for $W_mean [m/s]$ - cleaned

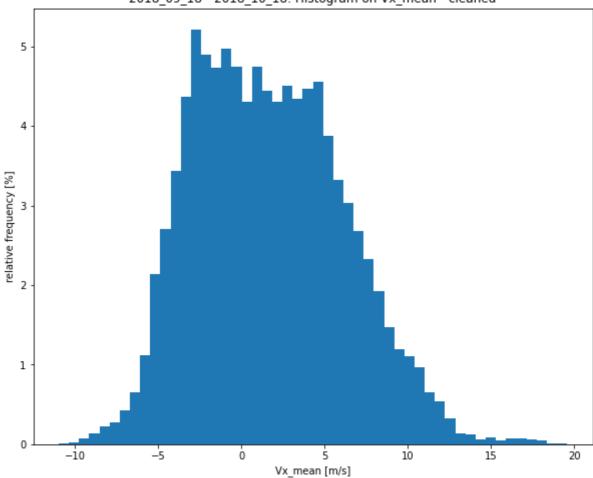
Mean: 0.25 Median: 0.14

Percentile [10, 25, 75, 90]: [-0.15 -0.02 0.43 0.83]

Minimum: -1.41 Maximum: 4.48 Variance: 0.2

Standard deviation: 0.44

Skewness: 1.59 Kurtosis: 4.23



Statistics for $Vx_mean [m/s] - cleaned$

Mean: 1.66

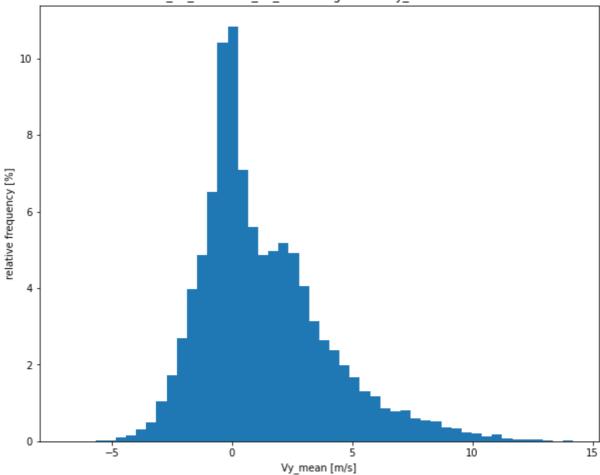
Median: 1.35

Percentile [10, 25, 75, 90]: [-3.84 -1.89 4.79 7.68]

Minimum: -10.97 Maximum: 19.58 Variance: 20.14

Standard deviation: 4.49

Skewness: 0.35 Kurtosis: -0.25



Statistics for Vy_mean [m/s] - cleaned

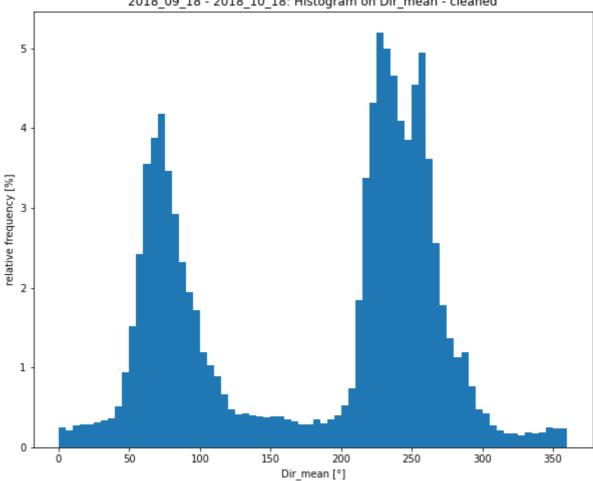
Mean: 1.3 Median: 0.65

Percentile [10, 25, 75, 90]: [-1.5 -0.47 2.71 4.9]

Minimum: -6.95 Maximum: 14.21 Variance: 7.09

Standard deviation: 2.66

Skewness: 1.03 Kurtosis: 1.31



Statistics for Dir_mean [°] - cleaned

Mana. 100.00

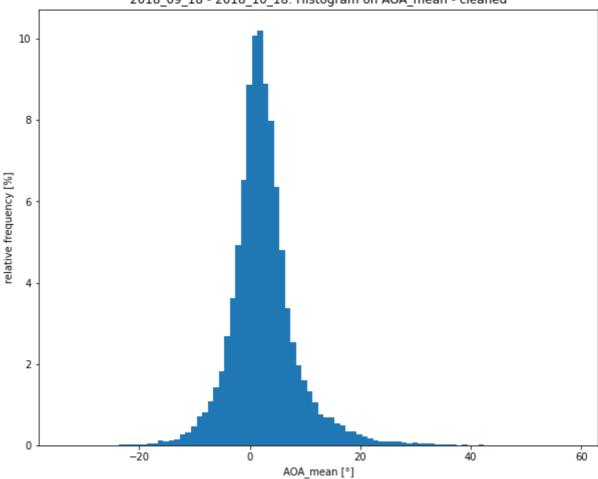
Mean: 180.89 Median: 222.57

Percentile [10, 25, 75, 90]: [63.3 83.71 250.04 268.52]

Minimum: 0.04 Maximum: 359.93 Variance: 7446.38

Standard deviation: 86.29

Skewness: -0.34 Kurtosis: -1.37



Statistics for AOA_mean [°] - cleaned

- . . .

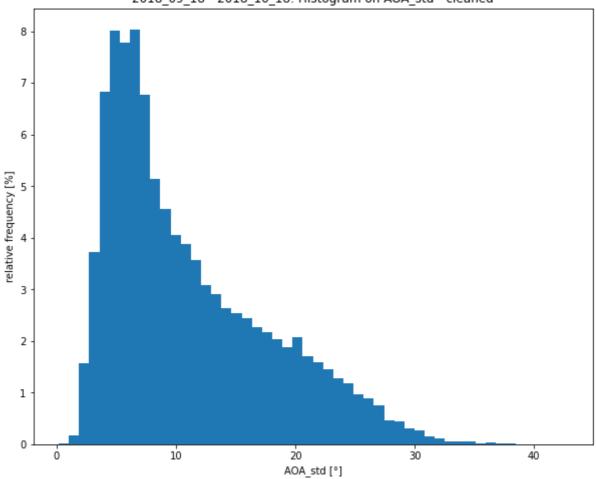
Mean: 2.44 Median: 1.91

Percentile [10, 25, 75, 90]: [-3.75 -0.69 4.89 9.06]

Minimum: -33.64 Maximum: 57.53 Variance: 36.94

Standard deviation: 6.08

Skewness: 1.03 Kurtosis: 5.42



Statistics for AOA_std [°] - cleaned

- . .

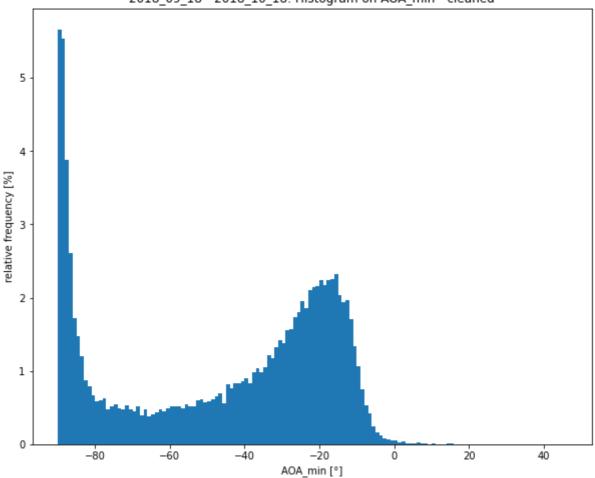
Mean: 11.13 Median: 9.04

Percentile [10, 25, 75, 90]: [4.17 5.78 15.41 21.51]

Minimum: 0.16 Maximum: 42.78 Variance: 45.8

Standard deviation: 6.77

Skewness: 0.94 Kurtosis: 0.14



Statistics for AOA_min [°] - cleaned

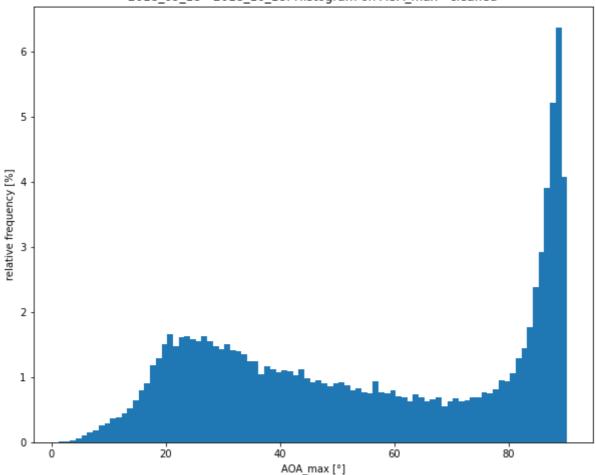
Mean: -45.97 Median: -36.54

Percentile [10, 25, 75, 90]: [-88.24 -79.03 -20.49 -13.66]

Minimum: -90.0 Maximum: 45.3 Variance: 832.33

Standard deviation: 28.85

Skewness: -0.35 Kurtosis: -1.42



Statistics for AOA_max [°] - cleaned

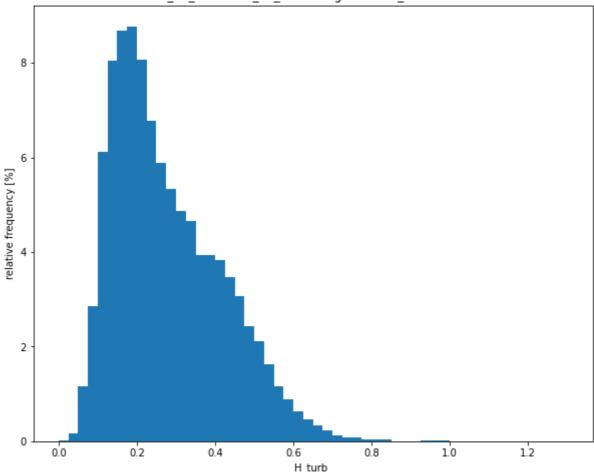
Mean: 55.15 Median: 53.57

Percentile [10, 25, 75, 90]: [20.8 30.44 84.21 88.36]

Minimum: 1.28 Maximum: 90.0 Variance: 695.77

Standard deviation: 26.38

Skewness: -0.05 Kurtosis: -1.5



Statistics for H_turb - cleaned

Mean: 0.28 Median: 0.25

Percentile [10, 25, 75, 90]: [0.12 0.17 0.37 0.48]

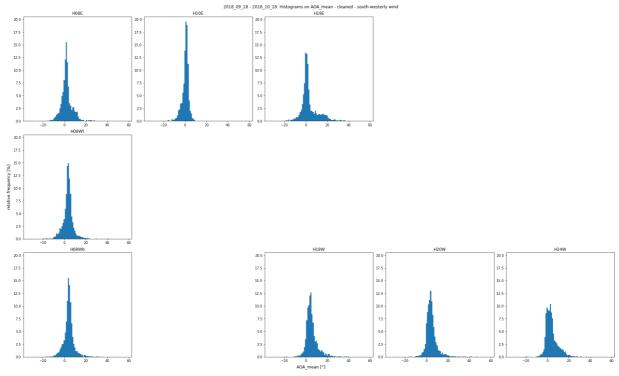
Minimum: 0.0 Maximum: 1.29 Variance: 0.02

Standard deviation: 0.14

Skewness: 0.82 Kurtosis: 0.4

The code below showcases how direct statistical comparisons between anemometers can be implemented. In this example the mean angle of attack and turbulence intensity are compared between anemometers on the upwind- and downwind-side of the bridge for south-westerly and north-easterly winds.

```
LFB.hist(LFB.anemo_cleaned[key].T[filter_idxs].T,xlabel=key,xunit=LFB.un
       else:
           LFB.hist(LFB.anemo_cleaned[key].T[filter_idxs].T,xlabel=key,xunit=LFB.un
       for sensor_name in sensor_names_of_interest:
           if sensor name in LFB.anemo names[LFB.anemo ok sensor id[key]]:
               sensor id = np.where(LFB.anemo names[LFB.anemo ok sensor id[key]]==s
               print('Statistics for', sensor_name, key, LFB.units[key], title_suffix)
               print('----')
               print('Mean:',np.round(np.mean(LFB.anemo_cleaned[key].T[filter_idxs]
               print('Median:',np.round(np.median(LFB.anemo_cleaned[key].T[filter_i
               print('Percentile [10, 25, 75, 90]:',np.round(np.percentile(LFB.anem
               print('Minimum:',np.round(np.min(LFB.anemo_cleaned[key].T[filter_idx
               print('Maximum:',np.round(np.max(LFB.anemo_cleaned[key].T[filter_idx
               print('Variance:',np.round(np.var(LFB.anemo_cleaned[key].T[filter_id
               print('Standard deviation:',np.round(np.std(LFB.anemo_cleaned[key].T
               print('\n')
           else:
               raise KeyError(str(sensor_name)+' not in ok anemometers. Choose a va
#north-easterly wind
filter_idxs = np.arange(len(LFB.time_array_cleaned)); title_suffix = ' - cleaned'
filter_idxs = LFB.filter_data(LFB.anemo_cleaned['Dir_mean'],prior_idxs=filter_idxs,l
for key in LFB.anemo cleaned.keys():
   if key in keys_of_interest:
       if key.startswith('Dir_m'): # Adjust the bin width to 5° for directional dat
           LFB.hist(LFB.anemo_cleaned[key].T[filter_idxs].T,xlabel=key,xunit=LFB.un
       elif key.startswith('H_m'): # Adjust the bins for consistency.
           LFB.hist(LFB.anemo_cleaned[key].T[filter_idxs].T,xlabel=key,xunit=LFB.un
       elif key.endswith('_turb'): # Adjust the bins for consistency.
           LFB.hist(LFB.anemo_cleaned[key].T[filter_idxs].T,xlabel=key,xunit=LFB.un
       elif key.startswith('AOA m'): # Adjust the bins for consistency.
           LFB.hist(LFB.anemo_cleaned[key].T[filter_idxs].T,xlabel=key,xunit=LFB.un
       else:
           LFB.hist(LFB.anemo_cleaned[key].T[filter_idxs].T,xlabel=key,xunit=LFB.un
       for sensor_name in sensor_names_of_interest:
           if sensor_name in LFB.anemo_names[LFB.anemo_ok_sensor_id[key]]:
               sensor_id = np.where(LFB.anemo_names[LFB.anemo_ok_sensor_id[key]]==s
               print('Statistics for', sensor_name, key, LFB.units[key], title_suffix)
               print('----')
               print('Mean:',np.round(np.mean(LFB.anemo_cleaned[key].T[filter idxs]
               print('Median:',np.round(np.median(LFB.anemo_cleaned[key].T[filter_i
               print('Percentile [10, 25, 75, 90]:',np.round(np.percentile(LFB.anem)
               print('Minimum:',np.round(np.min(LFB.anemo cleaned[key].T[filter idx
               print('Maximum:',np.round(np.max(LFB.anemo_cleaned[key].T[filter_idx
               print('Variance:',np.round(np.var(LFB.anemo_cleaned[key].T[filter_id
               print('Standard deviation:',np.round(np.std(LFB.anemo_cleaned[key].T
               print('\n')
           else:
               raise KeyError(str(sensor name)+' not in ok anemometers. Choose a va
```



Statistics for H08Wb AOA_mean [°] - cleaned - south-westerly wind

Mean: 4.2 Median: 4.13

Percentile [10, 25, 75, 90]: [-1.29 2.15 6.08 8.93]

Minimum: -17.55 Maximum: 35.22 Variance: 23.56

Standard deviation: 4.85

Statistics for H08E AOA_mean [°] - cleaned - south-westerly wind

Mean: 2.18 Median: 1.75

Percentile [10, 25, 75, 90]: [-3.35 -0.39 4.02 8.75]

Minimum: -21.04 Maximum: 30.51 Variance: 26.74

Standard deviation: 5.17

Statistics for H18W AOA_mean [°] $\,$ - cleaned - south-westerly wind

Mean: 5.47 Median: 4.5

Percentile [10, 25, 75, 90]: [0.51 2.27 7.21 12.02]

Minimum: -17.74 Maximum: 39.49 Variance: 30.28

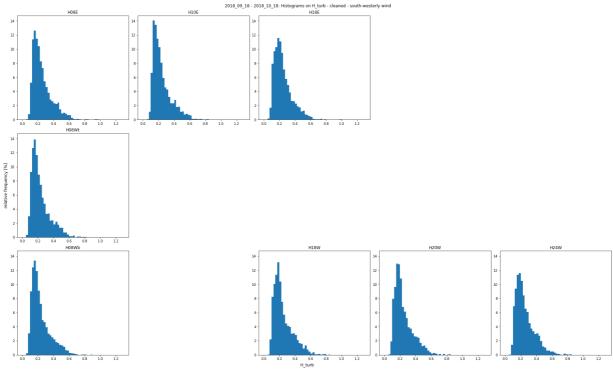
Standard deviation: 5.5

Statistics for H18E AOA_mean [°] - cleaned - south-westerly wind

Mean: 3.3 Median: 1.18

Percentile [10, 25, 75, 90]: [-3.54 -0.73 5.37 15.46]

Minimum: -21.9 Maximum: 53.22 Variance: 64.0 Standard deviation: 8.0



Statistics for H08Wb H_turb - cleaned - south-westerly wind

Mean: 0.24 Median: 0.2

Percentile [10, 25, 75, 90]: [0.12 0.15 0.3 0.42]

Minimum: 0.06 Maximum: 0.89 Variance: 0.01

Standard deviation: 0.12

Statistics for H08E H_turb - cleaned - south-westerly wind

Mean: 0.25 Median: 0.22

Percentile [10, 25, 75, 90]: [0.13 0.16 0.31 0.43]

Minimum: 0.07 Maximum: 0.95 Variance: 0.01

Standard deviation: 0.12

Statistics for H18W H_turb - cleaned - south-westerly wind

Mean: 0.25 Median: 0.21

Percentile [10, 25, 75, 90]: [0.12 0.16 0.31 0.42]

Minimum: 0.07 Maximum: 0.84 Variance: 0.01

Standard deviation: 0.12

Statistics for H18E H_turb - cleaned - south-westerly wind

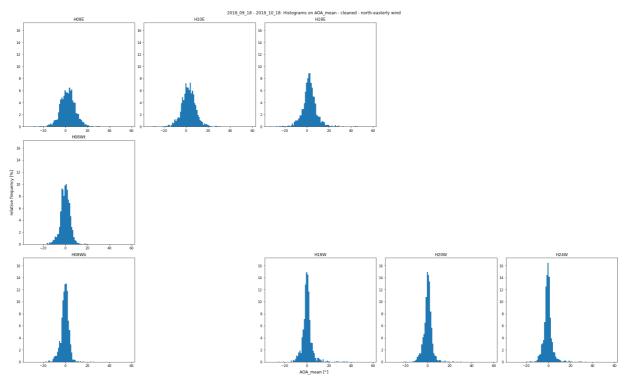
Mean: 0.25

Median: 0.23

Percentile [10, 25, 75, 90]: [0.13 0.16 0.3 0.41]

Minimum: 0.06
Maximum: 0.98
Variance: 0.01

Standard deviation: 0.11



Statistics for H08Wb AOA_mean [°] - cleaned - north-easterly wind

Mean: -0.42 Median: -0.09

Percentile [10, 25, 75, 90]: [-4.95 -2.32 1.73 3.62]

Minimum: -17.86 Maximum: 26.1 Variance: 13.94

Standard deviation: 3.73

```
Statistics for H08E AOA_mean [°] - cleaned - north-easterly wind
```

Mean: 2.41 Median: 2.36

Percentile [10, 25, 75, 90]: [-5.48 -2.15 6.54 10.84]

Minimum: -27.67 Maximum: 40.72 Variance: 47.37

Standard deviation: 6.88

Statistics for H18W AOA_mean [°] - cleaned - north-easterly wind

Mean: 0.39 Median: 0.22

Percentile [10, 25, 75, 90]: [-4.11 -1.63 2.04 4.6]

Minimum: -25.3 Maximum: 36.82 Variance: 22.95

Standard deviation: 4.79

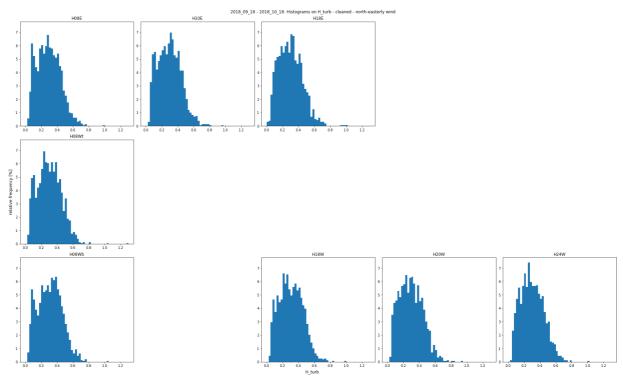
```
Statistics for H18E AOA_mean [°] - cleaned - north-easterly wind
```

Mean: 2.41 Median: 2.3

Percentile [10, 25, 75, 90]: [-5.12 -0.84 5.62 9.67]

Minimum: -33.11 Maximum: 45.93 Variance: 45.89

Standard deviation: 6.77



Statistics for H08Wb H_turb - cleaned - north-easterly wind

Mean: 0.31 Median: 0.31

Percentile [10, 25, 75, 90]: [0.11 0.2 0.42 0.51]

Minimum: 0.04 Maximum: 1.03 Variance: 0.02

Standard deviation: 0.15

Statistics for H08E H_turb - cleaned - north-easterly wind

Mean: 0.3

Median: 0.29

Percentile [10, 25, 75, 90]: [0.11 0.18 0.4 0.48]

Minimum: 0.04 Maximum: 0.98 Variance: 0.02

Standard deviation: 0.14

Statistics for H18W H_turb - cleaned - north-easterly wind

Mean: 0.31 Median: 0.3

Percentile [10, 25, 75, 90]: [0.11 0.2 0.41 0.5]

Minimum: 0.03 Maximum: 1.0 Variance: 0.02

Standard deviation: 0.15

Weatherstation

```
filter_idxs = np.arange(len(LFB.time_array_cleaned)); title_suffix = ' - cleaned'
# filter_idxs = LFB.filter_data(LFB.traffic_cleaned,prior_idxs=filter_idxs,zeros=Tru
# filter_idxs = LFB.filter_data(LFB.anemo_cleaned['H_mean'],prior_idxs=filter_idxs,h
# filter_idxs = LFB.filter_data(LFB.anemo_cleaned['Dir_mean'],prior_idxs=filter_idxs
# filter_idxs = LFB.filter_data(LFB.anemo_cleaned['Dir_mean'],prior_idxs=filter_idxs
```

Similarly, data **weather** data from the *weather station* at H10W can be analysed.

Accelerometers

Similarly, accelerometer data can be analysed.

Wind roses

Another usefull visualisation technique are **wind roses**, which can be created using the windrose method.

Note that it is possible to provide a specific colormap to the keyword cmap and even create your own colormap, for example by using the ListedColormap class from the *matplotlib*

library.

In this example the colormap from windfinder.com is recreated.

```
In [ ]:
    # Colormap for windroses based on windfinder.com colors
    Windfinder_wind_rose_cmap = ListedColormap(['darkblue', 'lightskyblue', 'limegreen',
```

The filters work the same way as above and will not be explained anymore further down.

```
filter_idxs = np.arange(len(LFB.time_array_cleaned)); title_suffix = ' - cleaned'
# filter_idxs = LFB.filter_data(LFB.anemo_cleaned['Dir_mean'][LFB.get_ok_sensor_ind(
# filter_idxs = LFB.filter_data(LFB.anemo_cleaned['AOA_mean'][LFB.get_ok_sensor_ind(
# filter_idxs = LFB.filter_data(LFB.traffic_cleaned,prior_idxs=filter_idxs,zeros=Tru
# filter_idxs = LFB.filter_data(LFB.anemo_cleaned['H_mean'],prior_idxs=filter_idxs,h
```

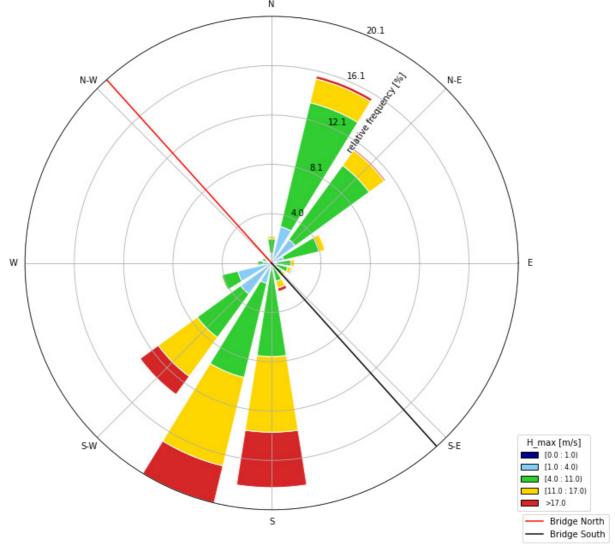
The wind roses can for example be created for 'H_max' or 'H_mean'. It is also again possible to split it up per sensor using the split_sensors keyword.

Note that for *multi-variat* analysis on measurements of different types it is necessary to find the common_ok_sensors and respective *sensor indices* first using the find_common_ok_sensors method.

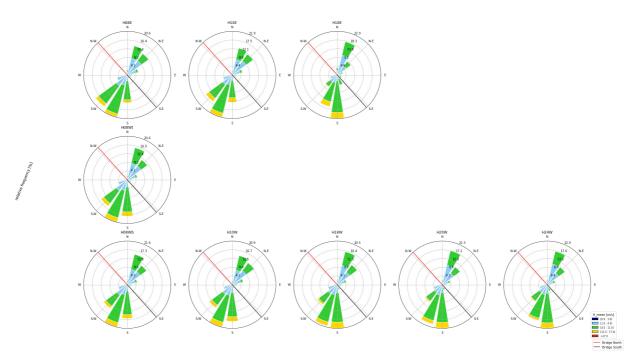
Also note how our custom Windfinder_wind_rose_cmap colormap is provided to the keyword cmap of the windrose method for this type of measurement and the respective bins are setup.

```
In [ ]:
    common_ok_sensors,s1_ind,s2_ind = LFB.find_common_ok_sensors(LFB.anemo_ok_sensor_id[
    LFB.windrose(LFB.anemo_cleaned['Dir_mean'][s1_ind].T[filter_idxs].T,LFB.anemo_cleane
```

2018_09_18 - 2018_10_18: Wind rose on H_max - cleaned $_{\rm N}$



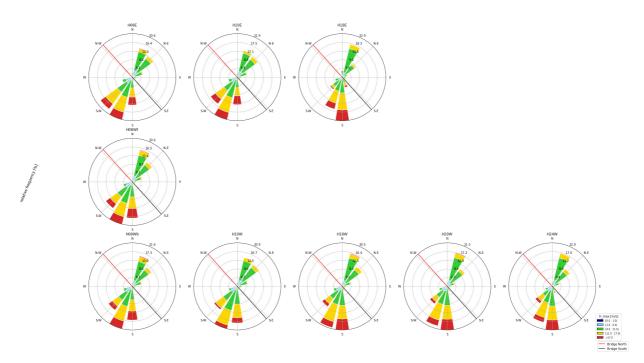
2018_09_18 - 2018_10_18: Wind roses on H_mean - cleaner



In []:

common_ok_sensors,s1_ind,s2_ind = LFB.find_common_ok_sensors(LFB.anemo_ok_sensor_id[
LFB.windrose(LFB.anemo_cleaned['Dir_mean'][s1_ind].T[filter_idxs].T,LFB.anemo_cleane

2018_09_18 - 2018_10_18: Wind roses on H_max - cleaned



AOA wind roses

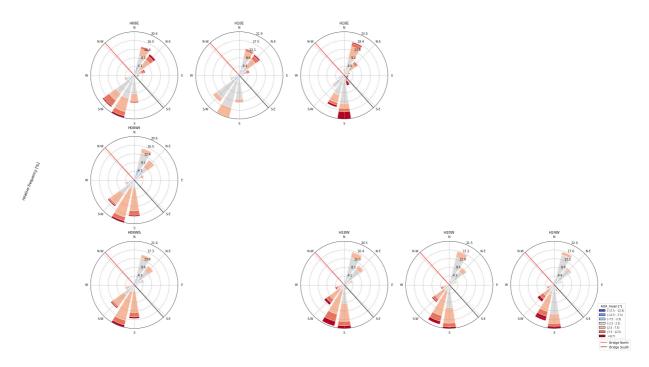
It is also possible to create wind roses on other *types of measurements*, such as the **angle of attack (AOA)**, by providing the respective *key* 'AOA_mean'.

Note how the 'coolwarm' *colormap* is provided to the keyword cmap of the windrose method for this type of measurement and the respective bins are setup.

```
filter_idxs = np.arange(len(LFB.time_array_cleaned)); title_suffix = ' - cleaned'
# filter_idxs = LFB.filter_data(LFB.anemo_cleaned['Dir_mean'][LFB.get_ok_sensor_ind(
# filter_idxs = LFB.filter_data(LFB.anemo_cleaned['AOA_mean'][LFB.get_ok_sensor_ind(
# filter_idxs = LFB.filter_data(LFB.traffic_cleaned,prior_idxs=filter_idxs,zeros=Tru
# filter_idxs = LFB.filter_data(LFB.anemo_cleaned['H_mean'],prior_idxs=filter_idxs,h
```

```
In [ ]:
    common_ok_sensors,s1_ind,s2_ind = LFB.find_common_ok_sensors(LFB.anemo_ok_sensor_id[
    LFB.windrose(LFB.anemo_cleaned['Dir_mean'][s1_ind].T[filter_idxs].T,LFB.anemo_cleane
```

2018_09_18 - 2018_10_18: Wind roses on AOA_mean - cleaned



Turbulence wind roses

Similarly, wind roses can be created for the horizontal turbulence intensity 'H_turb'

Polar scatterplots

Another visualisation technique for directional data is creating *polar scatterplots* using the polar_scatterplot method.

Again a custom *colormap* Windfinder_cmap is set up for wind speed data ('H_m...') using the ListedColormap class from the *matplotlib* library to match the colormap from

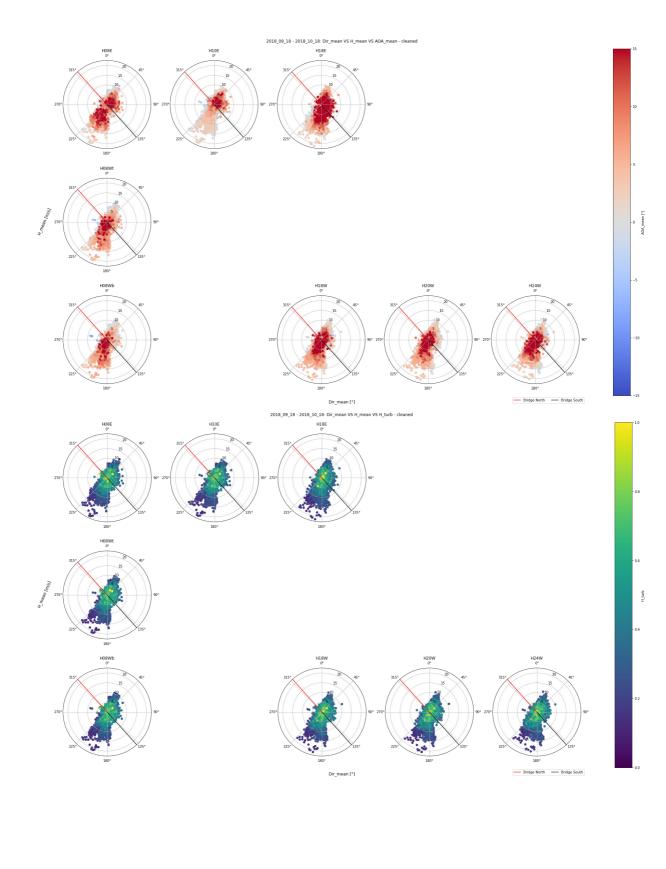
```
In []: # Colormap for scatterplots based on windfinder.com colors
Windfinder_cmap_list = []
for windspeed in range(36):
    if windspeed <= 1:
        Windfinder_cmap_list.append('darkblue')
    elif windspeed <= 4:
        Windfinder_cmap_list.append('lightskyblue')
    elif windspeed <= 11:
        Windfinder_cmap_list.append('limegreen')
    elif windspeed <= 17:
        Windfinder_cmap_list.append('gold')
    else:
        Windfinder_cmap_list.append('tab:red')
Windfinder_cmap = ListedColormap(Windfinder_cmap_list)</pre>
```

```
filter_idxs = np.arange(len(LFB.time_array_cleaned)); title_suffix = ' - cleaned'
# filter_idxs = LFB.filter_data(LFB.anemo_cleaned['Dir_mean'][LFB.get_ok_sensor_ind(
# filter_idxs = LFB.filter_data(LFB.anemo_cleaned['AOA_mean'][LFB.get_ok_sensor_ind(
# filter_idxs = LFB.filter_data(LFB.traffic_cleaned,prior_idxs=filter_idxs,zeros=Tru
# filter_idxs = LFB.filter_data(LFB.anemo_cleaned['H_mean'],prior_idxs=filter_idxs,h
# filter_idxs = LFB.filter_data(LFB.anemo_cleaned['AOA_mean'],prior_idxs=filter_idxs
```

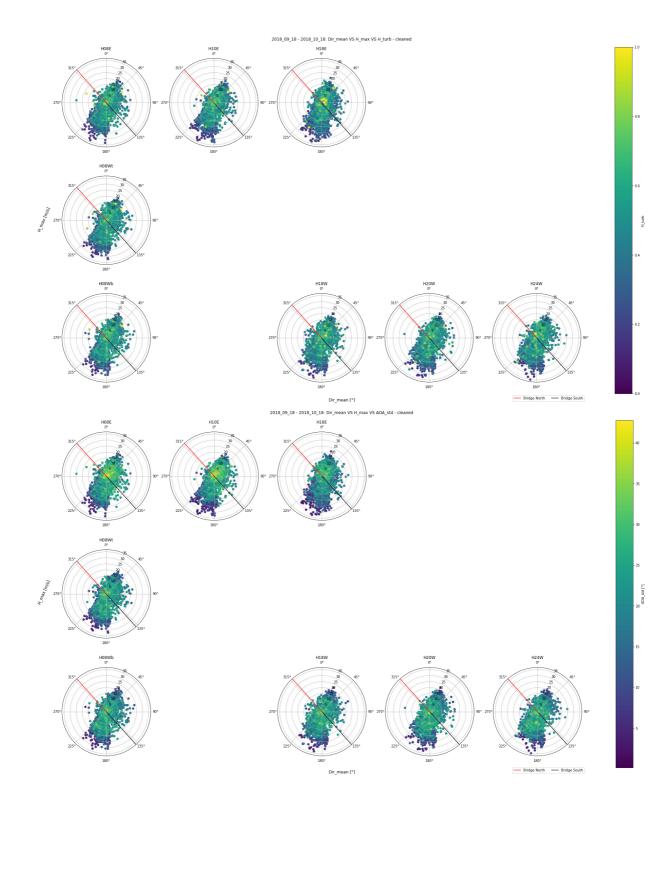
A similar method of *batch-processing* as showcased in the time-series plots is utilised, looping over the key2s_of_interest for the *radial axis* and key3s_of_interest for the *color-axis*

Note how different *colormaps* (cmap) and *limits* (vmin and vmax) are assigned to different *types of measurement* on the *color-axis* (key3)

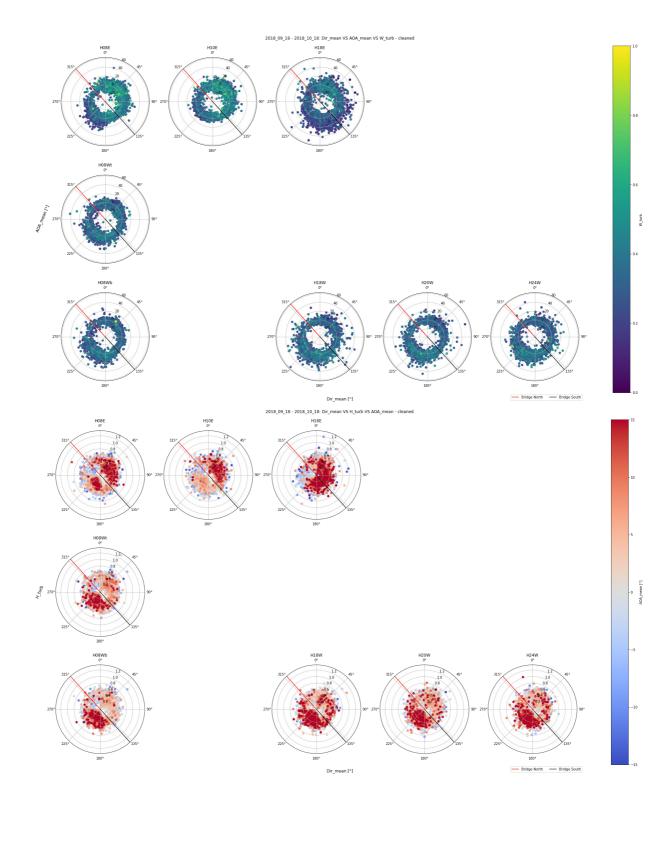
```
In [ ]:
         key1 = 'Dir mean'
         key2s_of_interest =['H_mean','H_max','AOA_mean','H_turb']
         key3s_of_interest = ['AOA_mean','H_mean','H_turb','AOA_std','AOA_min','AOA_max','W_t
         for key2 in key2s_of_interest:
             for key3 in key3s_of_interest:
                  if key2 != key3:
                      if key3.startswith('AOA_m'):
                          cmap = 'coolwarm'
                          vmin = -15
                          vmax = 15
                     elif key3.startswith('H m'):
                          cmap = Windfinder_cmap
                          vmin = 0
                          vmax = 35
                     elif key3.endswith('_turb'):
                          cmap = 'viridis'
                          vmin = 0
                          vmax = 1
                      else:
                          cmap = 'viridis'
                          vmin = None
                          vmax = None
                      common_ok_sensors,s1_ind,s2_ind = LFB.find_common_ok_sensors(LFB.anemo_o
                      common_ok_sensors,stemp_ind,s3_ind = LFB.find_common_ok_sensors(common_ok_sensors)
                      s1_ind = list(np.array(s1_ind)[stemp_ind])
                      s2_ind = list(np.array(s2_ind)[stemp_ind])
                      LFB.polar_scatterplot(LFB.anemo_cleaned[key1][s1_ind].T[filter_idxs].T,L
```

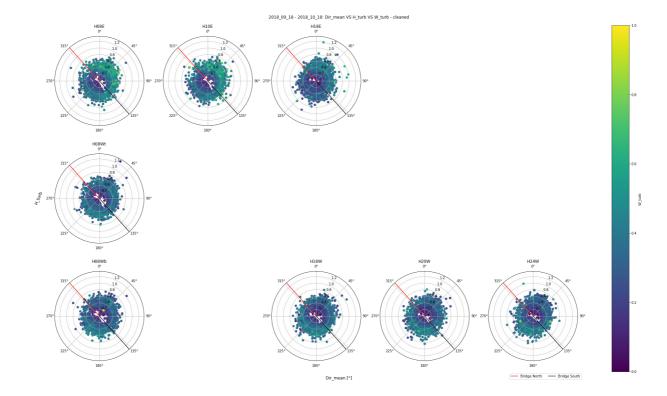


9 18 - 2018 10 18: Dir m



- 2018 10 18: Dir m





Boxplots

Aside from *splitting the sensors* in the different types of visualisations it is also possible to create *boxplots* to compare data from different sensors using the boxplot method.

```
filter_idxs = np.arange(len(LFB.time_array_cleaned)); title_suffix = ' - cleaned'
# filter_idxs = LFB.filter_data(LFB.traffic_cleaned,prior_idxs=filter_idxs,zeros=Tru
# filter_idxs = LFB.filter_data(LFB.anemo_cleaned['H_mean'],prior_idxs=filter_idxs,h
```

As the boxplot method is based on the function with the same name from the *matplotlib* library, using help(plt.boxplot) to refer to the documentation can help to understand this visualisation

```
In [ ]: help(plt.boxplot)
```

Help on function boxplot in module matplotlib.pyplot:

boxplot(x, notch=None, sym=None, vert=None, whis=None, positions=None, widths=None, patch_artist=None, bootstrap=None, usermedians=None, conf_intervals=None, meanline=N one, showmeans=None, showcaps=None, showbox=None, showfliers=None, boxprops=None, la bels=None, flierprops=None, medianprops=None, meanprops=None, capprops=None, whisker props=None, manage_ticks=True, autorange=False, zorder=None, *, data=None)

Draw a box and whisker plot.

The box extends from the first quartile (Q1) to the third quartile (Q3) of the data, with a line at the median. The whiskers extend from the box by 1.5x the inter-quartile range (IQR). Flier points are those past the end of the whiskers. See https://en.wikipedia.org/wiki/Box_plot for reference.

```
.. code-block:: none
```

<----> IQR

Parameters

x : Array or a sequence of vectors.

The input data. If a 2D array, a boxplot is drawn for each column in *x*. If a sequence of 1D arrays, a boxplot is drawn for each array in *x*.

notch : bool, default: False

Whether to draw a notched boxplot (`True`), or a rectangular boxplot (`False`). The notches represent the confidence interval (CI) around the median. The documentation for *bootstrap* describes how the locations of the notches are computed by default, but their locations may also be overridden by setting the *conf_intervals* parameter.

.. note::

In cases where the values of the CI are less than the lower quartile or greater than the upper quartile, the notches will extend beyond the box, giving it a distinctive "flipped" appearance. This is expected behavior and consistent with other statistical visualization packages.

sym : str, optional

The default symbol for flier points. An empty string ('') hides the fliers. If `None`, then the fliers default to 'b+'. More control is provided by the *flierprops* parameter.

vert : bool, default: True

If `True`, draws vertical boxes.

If `False`, draw horizontal boxes.

whis : float or (float, float), default: 1.5
The position of the whiskers.

If a float, the lower whisker is at the lowest datum above ``Q1 - whis*(Q3-Q1)``, and the upper whisker at the highest datum below ``Q3 + whis*(Q3-Q1)``, where Q1 and Q3 are the first and third quartiles. The default value of ``whis = 1.5`` corresponds to Tukey's original definition of boxplots.

If a pair of floats, they indicate the percentiles at which to draw the whiskers (e.g., (5, 95)). In particular, setting this to (0, 100) results in whiskers covering the whole range of the data.

In the edge case where ``Q1 == Q3``, *whis* is automatically set to (0, 100) (cover the whole range of the data) if *autorange* is True.

Beyond the whiskers, data are considered outliers and are plotted as individual points.

bootstrap : int, optional

Specifies whether to bootstrap the confidence intervals around the median for notched boxplots. If *bootstrap* is None, no bootstrapping is performed, and notches are calculated using a Gaussian-based asymptotic approximation (see McGill, R., Tukey, J.W., and Larsen, W.A., 1978, and Kendall and Stuart, 1967). Otherwise, bootstrap specifies

the number of times to bootstrap the median to determine its 95% confidence intervals. Values between 1000 and 10000 are recommended.

usermedians : 1D array-like, optional

A 1D array-like of length ``len(x)``. Each entry that is not `None` forces the value of the median for the corresponding dataset. For entries that are `None`, the medians are computed by Matplotlib as normal.

conf_intervals : array-like, optional

A 2D array-like of shape ``(len(x), 2)``. Each entry that is not None forces the location of the corresponding notch (which is only drawn if *notch* is `True`). For entries that are `None`, the notches are computed by the method specified by the other parameters (e.g., *bootstrap*).

positions : array-like, optional

The positions of the boxes. The ticks and limits are automatically set to match the positions. Defaults to `range(1, N+1)` where N is the number of boxes to be drawn.

widths : float or array-like

The widths of the boxes. The default is 0.5, or ``0.15*(distance between extreme positions)``, if that is smaller.

patch_artist : bool, default: False

If `False` produces boxes with the Line2D artist. Otherwise, boxes are drawn with Patch artists.

labels : sequence, optional

Labels for each dataset (one per dataset).

manage_ticks : bool, default: True

If True, the tick locations and labels will be adjusted to match the boxplot positions.

autorange : bool, default: False

When `True` and the data are distributed such that the 25th and 75th percentiles are equal, *whis* is set to (0, 100) such that the whisker ends are at the minimum and maximum of the data.

meanline : bool, default: False

If `True` (and *showmeans* is `True`), will try to render the mean as a line spanning the full width of the box according to *meanprops* (see below). Not recommended if *shownotches* is also True. Otherwise, means will be shown as points.

zorder : float, default: ``Line2D.zorder = 2``
The zorder of the boxplot.

Returns

dict

A dictionary mapping each component of the boxplot to a list of the `.Line2D` instances created. That dictionary has the following keys (assuming vertical boxplots):

- 'boxes': the main body of the boxplot showing the quartiles and the median's confidence intervals if enabled.
- ``medians``: horizontal lines at the median of each box.

```
- ``whiskers``: the vertical lines extending to the most
extreme, non-outlier data points.
```

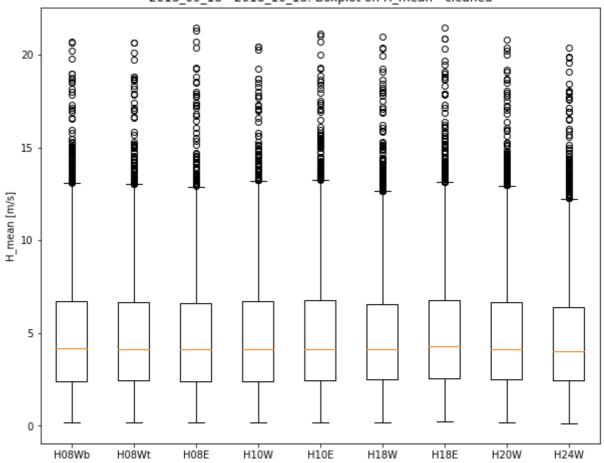
```
- ``caps``: the horizontal lines at the ends of the whiskers.
```

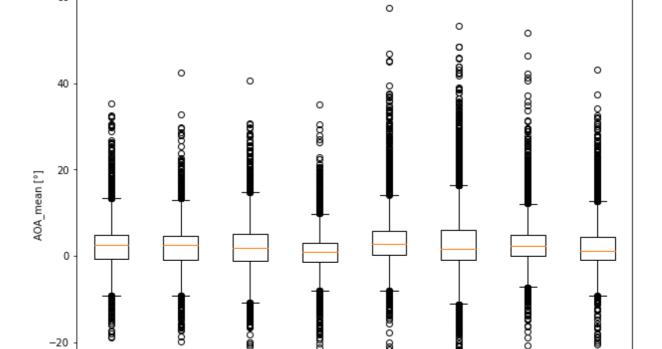
- ``fliers``: points representing data that extend beyond the whiskers (fliers).
- ``means``: points or lines representing the means.

```
Other Parameters
______
showcaps : bool, default: True
   Show the caps on the ends of whiskers.
showbox : bool, default: True
   Show the central box.
showfliers : bool, default: True
   Show the outliers beyond the caps.
showmeans : bool, default: False
   Show the arithmetic means.
capprops : dict, default: None
   The style of the caps.
boxprops : dict, default: None
   The style of the box.
whiskerprops : dict, default: None
   The style of the whiskers.
flierprops : dict, default: None
   The style of the fliers.
medianprops : dict, default: None
   The style of the median.
meanprops : dict, default: None
   The style of the mean.
data : indexable object, optional
   If given, all parameters also accept a string ``s``, which is
    interpreted as ``data[s]`` (unless this raises an exception).
See Also
_____
violinplot : Draw an estimate of the probability density function.
```

Below are some examples for this type of visualisation, using the same batch-processing technique as before.

```
keys_of_interest =['H_mean','AOA_mean','AOA_std','AOA_min','AOA_max','H_turb']
for key in keys_of_interest:
    LFB.boxplot(LFB.anemo_cleaned[key].T[filter_idxs].T,labels=LFB.anemo_names[LFB.a
```





H10E

H18W

H18E

H20W

H24W

0

H08Wt

0

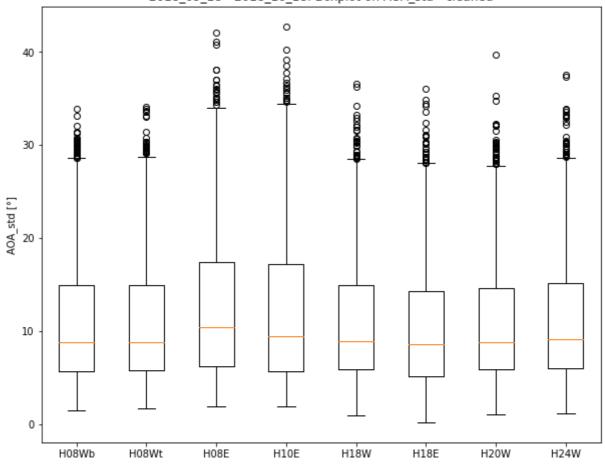
новиь

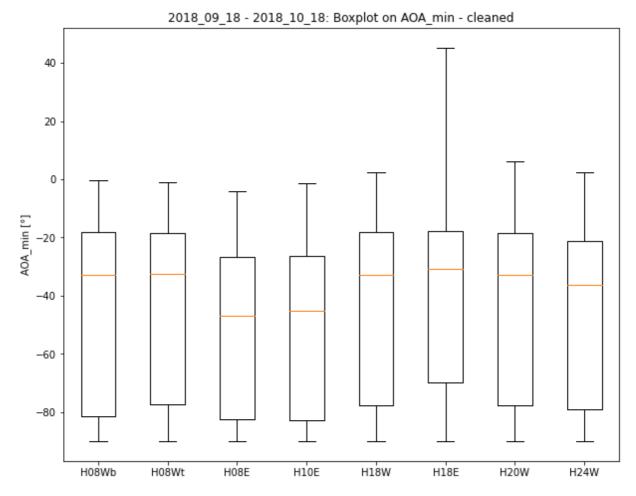
8

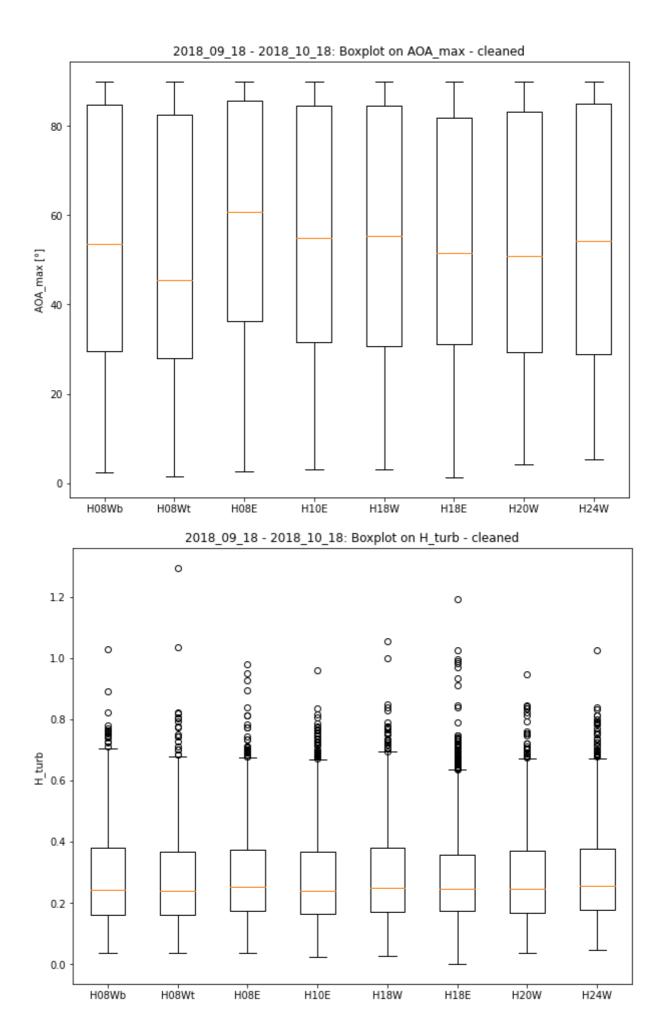
HO8E

2018_09_18 - 2018_10_18: Boxplot on AOA_mean - cleaned

60







Scatterplots

Scatterplots can be used to visualize bi-variat data or even tri-variat data using colored scatterplots. These can be created using the scatterplot method and setting the keyword color to True.

Alot of the functionallity of this method is shared with the previously described methods and will not be explained further. For more details refer to the documentation using help(BridgeData.scatterplot).

```
In [ ]: help(BridgeData.scatterplot)
```

Help on function scatterplot in module __main__:

scatterplot(self, data1, data2, data3, label1='data1', label2='data2', label3='data 3', units=['[]', '[]', '[]'], title_suffix='', color=True, plot_in_order_of_color=True, cmap='viridis', vmin=None, vmax=None, curve_fit=False, func='quadratic', upper_1 im=inf, lower_lim=-inf, bounds=([-inf, -inf, -inf], [inf, inf, inf]), res=1000, pred =1.5, curve_fit_return=False, split_sensors=False, sensors=[], ncol=4, bridge_model=False, Hanger_num=[], West=[], Top=[], save=False)

```
Method to create scatterplots on bridge data in a consistent manner.
   Parameters:
   data1 : array_like
       Data for x-axis.
   data2 : array_like
       Data for y-axis.
   data3 : array_like
       Data for color-axis.
   label1 : str, default 'data1'
       Label for x-axis.
   label2 : str, default 'data2'
       Label for y-axis.
   label3 : str, default 'data3'
       Label for colorbar.
    units: list of str, default ['[]','[]','[]']
       Units for x-,y- and color-axis.
    title_suffix : str, optional
       Add a suffix to the title.
    color : bool, default True
       The scatterplot is colored based on data3.
    plot in order of color : bool, default True
       Plot the datapoints of higher color ontop of datapoints of lower color.
    cmap : colormap or str, default 'viridis'
       Colormap to use for the scatterplot.
   vmin : float, optional
       Lower limit for the color-axis.
    vmax : float, optional
       Upper limit for the color-axis.
    curve_fit : bool, default False
       Fit a curve to the scatterplot. Note: Only works for single scatterplot, not
multiple.
    func : {'quadratic', 'linear'}
       Function for curve fitting.
    upper_lim : float, default np.inf
       Upper limit for data3 values.
    lower lim : float, default -np.inf
       Lower limit for data3 values.
   bounds : tuple, default ([-np.inf,-np.inf,,-np.inf],[np.inf,np.inf,np.inf])
       Bounds for curve fitting parameters.
    res : int, default 1000
       Number of points for the curve fitting.
```

```
pred : float, default 1.5
       Value for prediction of curve fitting.
    curve_fit_return : bool, default False
        Return the parameters of the curve fit.
    split sensors : bool, default False
        Split the scatterplot into the different sensors.
    sensors : list of str, optional
       List of sensor labels to place above seperate scatterplots if `split_sensors
`is used.
    ncol : int, default 4
       Number of columns defining the grid to place the scatterplots on if `split_s
ensors` is used and `bridge_model` is False.
    bridge model : bool, default False
       Whether to place the scatterplots on a gird based on their location at the b
ridge if `split_sensors` is used. Uses `Hanger_num`, `West` and `Top`.
    Hanger_num : list of int, optional
       List of the hanger numbers at which each sensor is located.
   West, Top : list of bool, optional
       List of booleans defining whether each sensor is located on the West side, o
r is a top-row sensor respectively.
    save : bool, default False
        Save the scatterplot in ../images/. Note: Requires the prior existence of th
at folder.
   Returns:
    popt1, popt2, pcov1, pcov2 : array_like, optional
        If `curve_fit_return` is True, returns the parameters of the curve fit.
   See Also
    -----
    `polar_scatterplot`
```

Note that it is also possible to analyse data of different *measurement types* from **anemometers** in relation to data of different *measurement types* from **anccelerometers** in different ways to examine the **wind response** of the bridge.

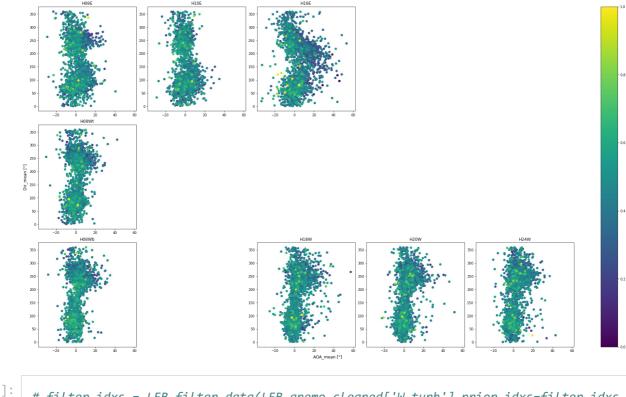
filter_idxs = np.arange(len(LFB.time_array_cleaned)); title_suffix = ' - cleaned'

Anemo VS Anemo VS Anemo - Wind characteristics

In []:

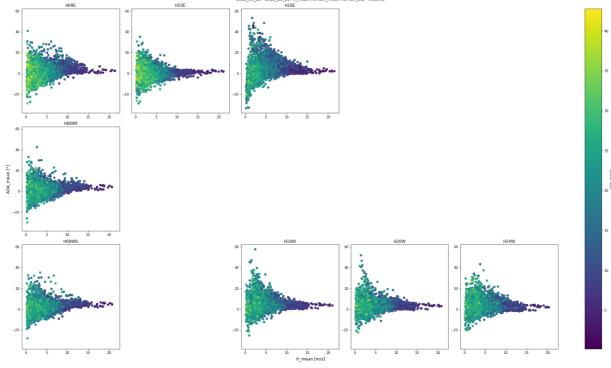
```
# filter idxs = LFB.filter data(LFB.traffic cleaned,prior idxs=filter idxs,zeros=Tru
         # filter idxs = LFB.filter data(LFB.anemo cleaned['H mean'],prior idxs=filter idxs,h
         # filter idxs = LFB.filter data(LFB.anemo cleaned['Dir mean'],prior idxs=filter idxs
         # filter_idxs = LFB.filter_data(LFB.anemo_cleaned['Dir_mean'],prior_idxs=filter_idxs
In [ ]:
         key1 = 'AOA mean'
         key2 = 'Dir_mean'
         key3 = 'H_mean'
         common ok sensors,s1 ind,s2 ind = LFB.find common ok sensors(LFB.anemo ok sensor id
         common_ok_sensors,stemp_ind,s3_ind = LFB.find_common_ok_sensors(common_ok_sensors,LF
         s1_ind = list(np.array(s1_ind)[stemp_ind])
         s2_ind = list(np.array(s2_ind)[stemp_ind])
         if key3.startswith('AOA_m'):
             cmap = 'coolwarm'
             vmin = -15
             vmax = 15
         elif key3.startswith('H m'):
             cmap = Windfinder cmap
             vmin = 0
             vmax = 35
```

```
elif key3.endswith('_turb'):
             cmap = 'viridis'
             vmin = 0
             vmax = 1
         else:
             cmap = 'viridis'
             vmin = None
             vmax = None
         LFB.scatterplot(LFB.anemo_cleaned[key1][s1_ind].T[filter_idxs].T,LFB.anemo_cleaned[k
In [ ]:
         key1 = 'AOA_mean'
         key2 = 'Dir_mean'
         key3 = 'H_turb'
         common_ok_sensors,s1_ind,s2_ind = LFB.find_common_ok_sensors(LFB.anemo_ok_sensor_id[
         common_ok_sensors,stemp_ind,s3_ind = LFB.find_common_ok_sensors(common_ok_sensors,LF
         s1_ind = list(np.array(s1_ind)[stemp_ind])
         s2_ind = list(np.array(s2_ind)[stemp_ind])
         if key3.startswith('AOA m'):
             cmap = 'coolwarm'
             vmin = -15
             vmax = 15
         elif key3.startswith('H_m'):
             cmap = Windfinder cmap
             vmin = 0
             vmax = 35
         elif key3.endswith('_turb'):
             cmap = 'viridis'
             vmin = 0
             vmax = 1
         else:
             cmap = 'viridis'
             vmin = None
             vmax = None
         LFB.scatterplot(LFB.anemo_cleaned[key1][s1_ind].T[filter_idxs].T,LFB.anemo_cleaned[k
```

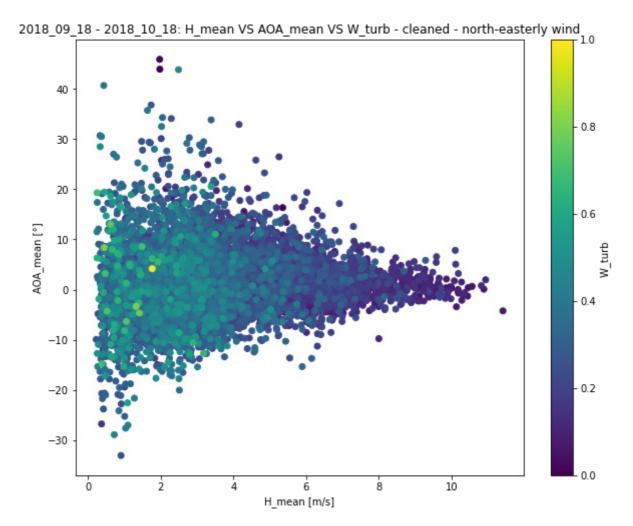


```
In [ ]:
         # filter_idxs = LFB.filter_data(LFB.anemo_cleaned['W_turb'],prior_idxs=filter_idxs,l
         key1 = 'AOA_mean'
         key2 = 'Dir_mean'
         key3 = 'W_turb'
         common_ok_sensors,s1_ind,s2_ind = LFB.find_common_ok_sensors(LFB.anemo_ok_sensor_id[
         common_ok_sensors,stemp_ind,s3_ind = LFB.find_common_ok_sensors(common_ok_sensors,LF
         s1_ind = list(np.array(s1_ind)[stemp_ind])
         s2_ind = list(np.array(s2_ind)[stemp_ind])
         if key3.startswith('AOA_m'):
             cmap = 'coolwarm'
             vmin = -15
             vmax = 15
         elif key3.startswith('H_m'):
             cmap = Windfinder_cmap
             vmin = 0
             vmax = 35
         elif key3.endswith('_turb'):
             cmap = 'viridis'
             vmin = 0
             vmax = 1
         else:
             cmap = 'viridis'
             vmin = None
             vmax = None
         LFB.scatterplot(LFB.anemo_cleaned[key1][s1_ind].T[filter_idxs].T,LFB.anemo_cleaned[k
```

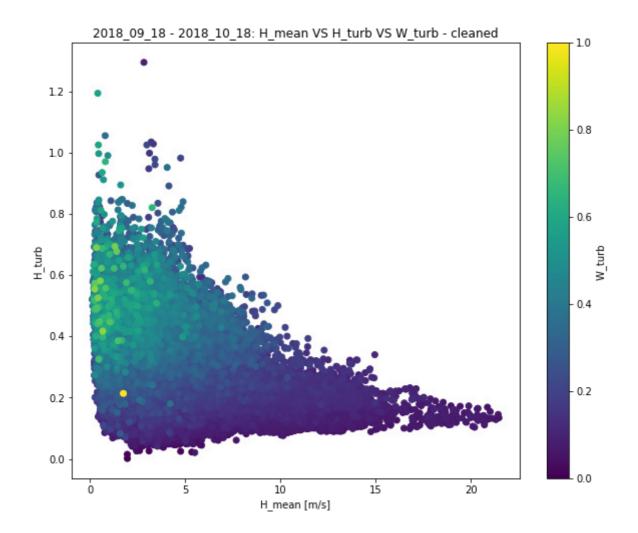
LFB.scatterplot(LFB.anemo_cleaned[key1][s1_ind].T[filter_idxs].T,LFB.anemo_cleaned[k



```
In [ ]:
         filter_idxs = np.arange(len(LFB.time_array_cleaned)); title_suffix = ' - cleaned'
         # filter_idxs = LFB.filter_data(LFB.anemo_cleaned['Dir_mean'],prior_idxs=filter_idxs
         filter_idxs = LFB.filter_data(LFB.anemo_cleaned['Dir_mean'],prior_idxs=filter_idxs,1
         # filter_idxs = LFB.filter_data(LFB.anemo_cleaned['W_turb'],prior_idxs=filter_idxs,l
         key1 = 'H_mean'
key2 = 'AOA_mean'
         key3 = 'W_turb'
         common_ok_sensors,s1_ind,s2_ind = LFB.find_common_ok_sensors(LFB.anemo_ok_sensor_id[
         common_ok_sensors,stemp_ind,s3_ind = LFB.find_common_ok_sensors(common_ok_sensors,LF
         s1_ind = list(np.array(s1_ind)[stemp_ind])
         s2_ind = list(np.array(s2_ind)[stemp_ind])
         if key3.startswith('AOA_m'):
              cmap = 'coolwarm'
             vmin = -15
              vmax = 15
         elif key3.startswith('H_m'):
              cmap = Windfinder cmap
              vmin = 0
              vmax = 35
         elif key3.endswith(' turb'):
              cmap = 'viridis'
              vmin = 0
              vmax = 1
         else:
              cmap = 'viridis'
              vmin = None
              vmax = None
         LFB.scatterplot(LFB.anemo_cleaned[key1][s1_ind].T[filter_idxs].T,LFB.anemo_cleaned[k
```



```
In [ ]:
         filter_idxs = np.arange(len(LFB.time_array_cleaned)); title_suffix = ' - cleaned'
         # filter_idxs = LFB.filter_data(LFB.anemo_cleaned['W_turb'],prior_idxs=filter_idxs,l
         key1 = 'H_mean'
         key2 = 'H_turb'
key3 = 'W_turb'
         common_ok_sensors,s1_ind,s2_ind = LFB.find_common_ok_sensors(LFB.anemo_ok_sensor_id[
         common_ok_sensors,stemp_ind,s3_ind = LFB.find_common_ok_sensors(common_ok_sensors,LF
         s1_ind = list(np.array(s1_ind)[stemp_ind])
         s2_ind = list(np.array(s2_ind)[stemp_ind])
         if key3.startswith('AOA_m'):
             cmap = 'coolwarm'
             vmin = -15
             vmax = 15
         elif key3.startswith('H_m'):
             cmap = Windfinder cmap
             vmin = 0
             vmax = 35
         elif key3.endswith('_turb'):
             cmap = 'viridis'
             vmin = 0
             vmax = 1
         else:
             cmap = 'viridis'
             vmin = None
             vmax = None
         LFB.scatterplot(LFB.anemo_cleaned[key1][s1_ind].T[filter_idxs].T,LFB.anemo_cleaned[k
```



Anemo VS Acc VS Anemo - Wind response

Note that in the following scatterplots the data is filtered such that traffic dominated responses are ignored.

```
filter_idxs = np.arange(len(LFB.time_array_cleaned)); title_suffix = ' - cleaned'
filter_idxs = LFB.filter_data(LFB.traffic_cleaned,prior_idxs=filter_idxs,zeros=True,
# filter_idxs = LFB.filter_data(LFB.anemo_cleaned['H_mean'],prior_idxs=filter_idxs,h
```

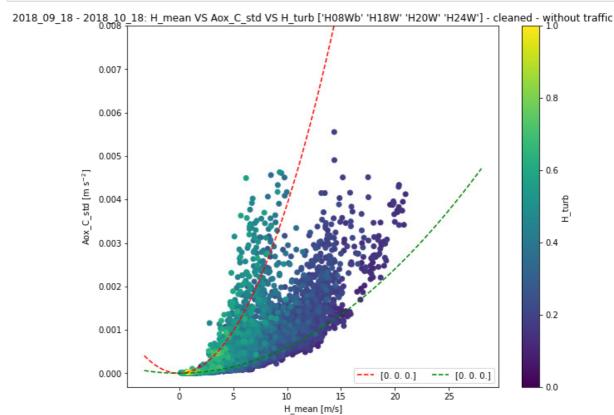
Through *batch-processing* the same plots are generated for the lateral bridge response 'Aox_C_std', vertical bridge response 'Aoz_C_std' and torsional bridge response 'theta_std'

The scatterplots below show the bridge response at different mean horizontal wind velocities 'H_mean' . The color-axis displays the horizontal turbulence intensity 'H_turb' .

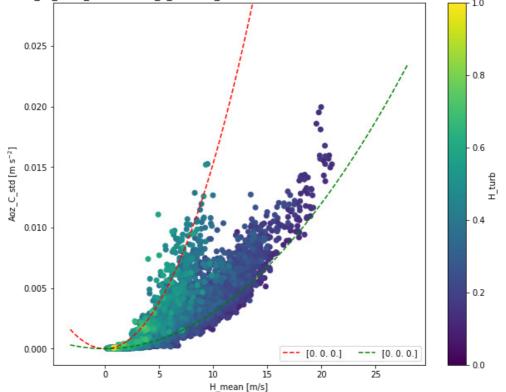
A red and green parabola are fitted to the data, limited to datapoints with turbulence intensities above 0.6 and below 0.1 respectively.

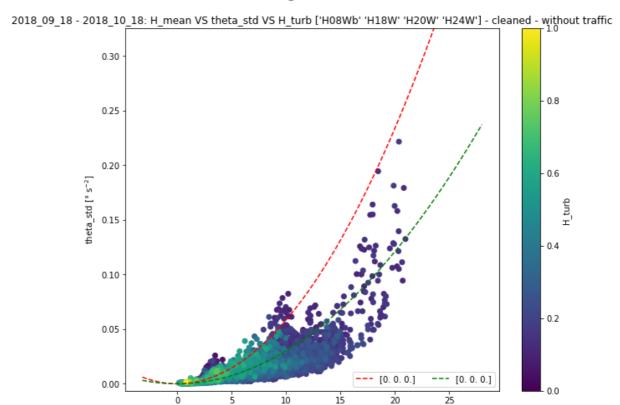
```
key1 = 'H_mean'
key2s_of_interest = ['Aox_C_std','Aoz_C_std','theta_std']
key3 = 'H_turb'
for key2 in key2s_of_interest:
    selected_sensors_key1=['H08Wb','H18W','H20W','H24W']
    selected_sensors_key2=['H09','H18','H24','H30']
    selected_sensors_key3=['H08Wb','H18W','H20W','H24W']
    s1_ind = LFB.get_ok_sensor_ind(sensor_names=selected_sensors_key1,sensor_type='a
    s2_ind = LFB.get_ok_sensor_ind(sensor_names=selected_sensors_key2,sensor_type='a
```

```
s3_ind = LFB.get_ok_sensor_ind(sensor_names=selected_sensors_key3,sensor_type='a
diff = np.abs(len(s1_ind)-len(s2_ind))
if key3.startswith('AOA_m'):
    cmap = 'coolwarm'
    vmin = -15
    vmax = 15
elif key3.startswith('H_m'):
   cmap = Windfinder_cmap
   vmin = 0
    vmax = 35
elif key3.endswith('_turb'):
    cmap = 'viridis'
   vmin = 0
    vmax = 1
else:
    cmap = 'viridis'
   vmin = None
   vmax = None
LFB.scatterplot(LFB.anemo_cleaned[key1][s1_ind].T[filter_idxs].T,LFB.acc_cleaned
```



2018_09_18 - 2018_10_18: H_mean VS Aoz_C_std VS H_turb ['H08Wb' 'H18W' 'H20W' 'H24W'] - cleaned - without traffic



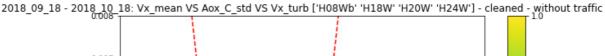


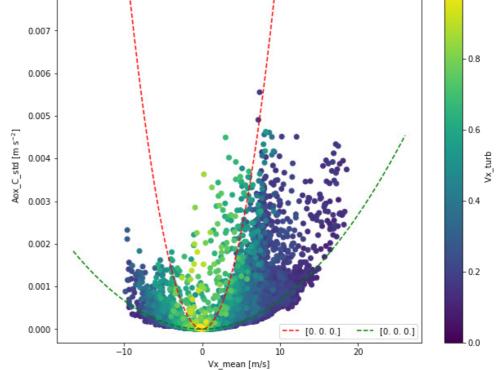
The scatterplots below only take the mean velocity 'Vx_mean' and turbulence intensity 'Vx_turb' in x-direction, which is perpendicular to the bridge, instead of the full horizontal component. Note that also splits the data in westerly and easterly wind directions, as the x-component is signed.

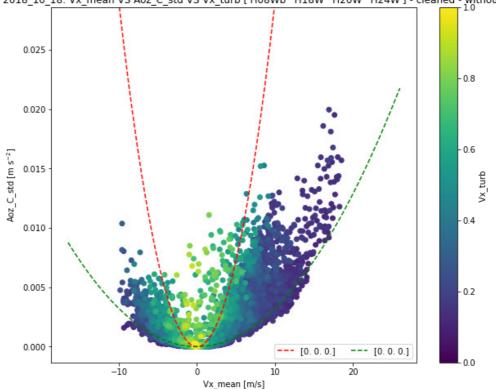
H_mean [m/s]

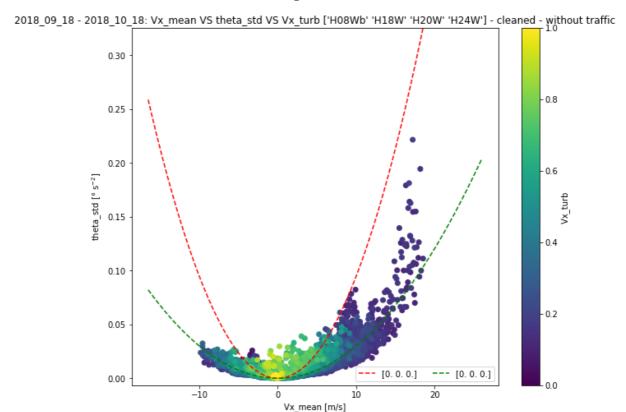
```
key1 = 'Vx_mean'
key2s_of_interest = ['Aox_C_std','Aoz_C_std','theta_std']
key3 = 'Vx_turb'
for key2 in key2s_of_interest:
    selected_sensors_key1=['H08Wb','H18W','H20W','H24W']
```

```
selected_sensors_key2=['H09','H18','H24','H30']
selected_sensors_key3=['H08Wb','H18W','H20W','H24W']
s1_ind = LFB.get_ok_sensor_ind(sensor_names=selected_sensors_key1,sensor_type='a
s2_ind = LFB.get_ok_sensor_ind(sensor_names=selected_sensors_key2,sensor_type='a
s3_ind = LFB.get_ok_sensor_ind(sensor_names=selected_sensors_key3,sensor_type='a
diff = np.abs(len(s1_ind)-len(s2_ind))
if key3.startswith('AOA_m'):
    cmap = 'coolwarm'
   vmin = -15
   vmax = 15
elif key3.startswith('H_m'):
   cmap = Windfinder_cmap
   vmin = 0
   vmax = 35
elif key3.endswith('_turb'):
    cmap = 'viridis'
    vmin = 0
   vmax = 1
else:
   cmap = 'viridis'
   vmin = None
    vmax = None
LFB.scatterplot(LFB.anemo_cleaned[key1][s1_ind].T[filter_idxs].T,LFB.acc_cleaned
```









In the scatterplots below the bridge response divided by the turbulence intensity 'Vx_turb' at different mean wind speeds in x-direction 'Vx_mean', measured at midspan from the downwind anemometer 'H18W' or 'H18E', depending on the filtered wind direction. The color-axis is displays 'Vx_turb'. The scatterplots are split across the accelerometer pairs 'H09', 'H18', 'H24' and 'H30'.

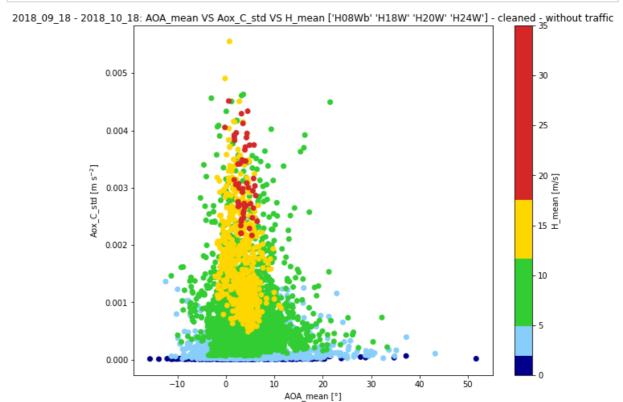
```
filter_idxs = LFB.filter_data(LFB.traffic_cleaned,prior_idxs=None,zeros=True,mode='a
    filter_idxs = LFB.filter_data(LFB.anemo_cleaned['Dir_mean'],prior_idxs=filter_idxs,h
    key1 = 'Vx_mean'
    key2s_of_interest = ['Aox_C_std','Aoz_C_std','theta_std']
    key3 = 'Vx_turb'
```

```
for key2 in key2s_of_interest:
               selected_sensors_key1=['H18W']
               selected_sensors_key2=['H09','H18','H24','H30']
               selected_sensors_key1
               s1_ind = LFB.get_ok_sensor_ind(sensor_names=selected_sensors_key1,sensor_type='a
               s2_ind = LFB.get_ok_sensor_ind(sensor_names=selected_sensors_key2,sensor_type='a
               s3_ind = LFB.get_ok_sensor_ind(sensor_names=selected_sensors_key3,sensor_type='a
               diff = np.abs(len(s1_ind)-len(s2_ind))
               if key3.startswith('AOA_m'):
                   cmap = 'coolwarm'
                   vmin = -15
                   vmax = 15
               elif key3.startswith('H_m'):
                   cmap = Windfinder cmap
                   vmin = 0
                   vmax = 35
               elif key3.endswith('_turb'):
                   cmap = 'viridis'
                   vmin = 0
                   vmax = 1
               else:
                   cmap = 'viridis'
                   vmin = None
                   vmax = None
               LFB.scatterplot(np.repeat(LFB.anemo_cleaned[key1][s1_ind].T[filter_idxs].T,diff+
                               0.035
         Aox C std / Vx turb [m s-2]
           0.025
           0.020
           0.015
           0.010
                                                                                    5.0
           0.12
         Aoz C std / Vx turb [m s<sup>-2</sup>]
           0.08
                                                                                           12.5 15.0 17.5
                                                      Vx_mean [m/s]
                               2018_09_18 - 2018_10_18: Vx_mean V5 theta_std / Vx_turb V5 Vx_turb ['H18W'] - cleaned - without traffic - south-westerly wind
         theta std /Vx turb [° s-2]
In [ ]:
          filter_idxs = LFB.filter_data(LFB.traffic_cleaned,prior_idxs=None,zeros=True,mode='a
          filter idxs = LFB.filter data(LFB.anemo cleaned['Dir mean'],prior idxs=filter idxs,l
          key1 = 'Vx_mean'
          key2s_of_interest = ['Aox_C_std','Aoz_C_std','theta_std']
          key3 = 'Vx_turb'
          for key2 in key2s_of_interest:
               selected_sensors_key1=['H18E']
```

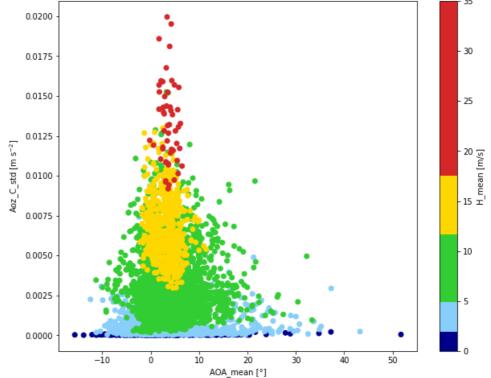
```
selected_sensors_key2=['H09','H18','H24','H30']
                                                             selected_sensors_key3=selected_sensors_key1
                                                             s1_ind = LFB.get_ok_sensor_ind(sensor_names=selected_sensors_key1,sensor_type='a
                                                             s2_ind = LFB.get_ok_sensor_ind(sensor_names=selected_sensors_key2,sensor_type='a
                                                             s3_ind = LFB.get_ok_sensor_ind(sensor_names=selected_sensors_key3,sensor_type='a
                                                             diff = np.abs(len(s1_ind)-len(s2_ind))
                                                             if key3.startswith('AOA_m'):
                                                                               cmap = 'coolwarm'
                                                                               vmin = -15
                                                                               vmax = 15
                                                             elif key3.startswith('H_m'):
                                                                               cmap = Windfinder_cmap
                                                                               vmin = 0
                                                                               vmax = 35
                                                            elif key3.endswith('_turb'):
                                                                               cmap = 'viridis'
                                                                               vmin = 0
                                                                               vmax = 1
                                                             else:
                                                                               cmap = 'viridis'
                                                                               vmin = None
                                                                               vmax = None
                                                             LFB.scatterplot(np.repeat(LFB.anemo_cleaned[key1][s1_ind].T[filter_idxs].T,diff+
                                                                                                                               2018\_09\_18 - 2018\_10\_18 : Vx\_mean \ VS \ Aox\_C\_std \ / \ Vx\_turb \ VS \ Vx\_turb \ ['H18E'] - cleaned - without \ traffic - north-easterly \ window of the control of the 
                                     Vx_turb [m s<sup>-2</sup>]
                                     Aox C std /
                                                                                                                               2018\_09\_18 - 2018\_10\_18 : Vx\_mean\ VS\ Aoz\_C\_std\ /\ Vx\_turb\ VS\ Vx\_turb\ ['H18E'] - cleaned\ -\ without\ traffice and the property of the 
                                     Aoz C std / Vx turb [m s<sup>-2</sup>]
                                                                                                                                    0.02
                                            0.015
                                                                                                                                    0.01
                                                                                                                                                                                                                           Vx_mean [m/s]
                                                                                                                               2018_09_18 - 2018_10_18: Vx_mean VS theta_std / Vx_turb VS Vx_turb ['H18E'] - cleaned - without traffic - north-easterly wind H18
                                     theta_std /Vx_turb [° s-2]
                                            0.20
                                            0.15
In [ ]:
                                          filter_idxs = np.arange(len(LFB.time_array_cleaned)); title_suffix = ' - cleaned'
                                          filter_idxs = LFB.filter_data(LFB.traffic_cleaned,prior_idxs=filter_idxs,zeros=True,
                                          # filter_idxs = LFB.filter_data(LFB.anemo_cleaned['H_mean'],prior_idxs=filter_idxs,h
In [ ]:
                                          key1 = 'AOA_mean'
                                          key2s_of_interest = ['Aox_C_std','Aoz_C_std','theta_std']
                                          key3 = 'H_mean'
```

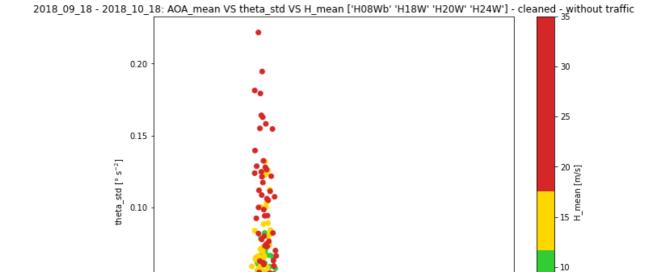
for key2 in key2s of interest:

```
selected_sensors_key1=['H08Wb','H18W','H20W','H24W']
selected_sensors_key2=['H09','H18','H24','H30']
selected_sensors_key3=['H08Wb','H18W','H20W','H24W']
s1_ind = LFB.get_ok_sensor_ind(sensor_names=selected_sensors_key1,sensor_type='a
s2_ind = LFB.get_ok_sensor_ind(sensor_names=selected_sensors_key2,sensor_type='a
s3_ind = LFB.get_ok_sensor_ind(sensor_names=selected_sensors_key3,sensor_type='a
if key3.startswith('AOA_m'):
    cmap = 'coolwarm'
   vmin = -15
    vmax = 15
elif key3.startswith('H_m'):
    cmap = Windfinder_cmap
   vmin = 0
   vmax = 35
elif key3.endswith('_turb'):
    cmap = 'viridis'
    vmin = 0
    vmax = 1
else:
   cmap = 'viridis'
   vmin = None
    vmax = None
LFB.scatterplot(LFB.anemo_cleaned[key1][s1_ind].T[filter_idxs].T,LFB.acc_cleaned
```









20

AOA_mean [°]

30

```
key1 = 'AOA_mean'
key2s_of_interest = ['Aox_C_std','Aoz_C_std','theta_std']
key3 = 'H_turb'
for key2 in key2s_of_interest:
    selected_sensors_key1=['H08Wb','H18W','H20W','H24W']
    selected_sensors_key2=['H09','H18','H24','H30']
    selected_sensors_key3=['H08Wb','H18W','H20W','H24W']
    s1_ind = LFB.get_ok_sensor_ind(sensor_names=selected_sensors_key1,sensor_type='a
    s2_ind = LFB.get_ok_sensor_ind(sensor_names=selected_sensors_key2,sensor_type='a
    s3_ind = LFB.get_ok_sensor_ind(sensor_names=selected_sensors_key3,sensor_type='a
    if key3.startswith('AOA_m'):
        cmap = 'coolwarm'
        vmin = -15
```

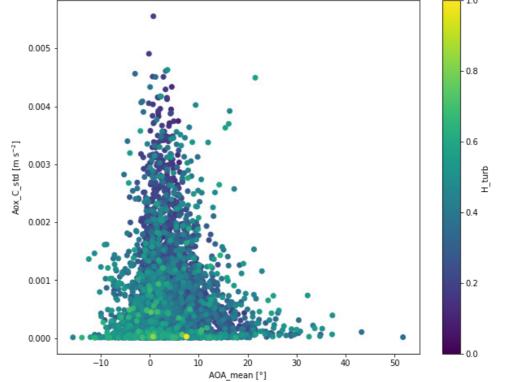
0.05

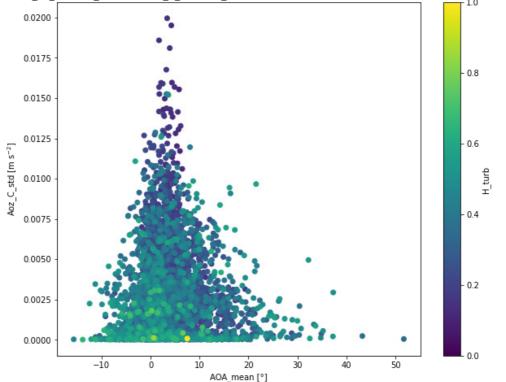
0.00

-io

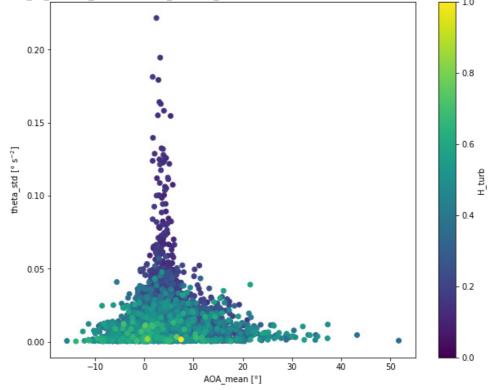
```
vmax = 15
elif key3.startswith('H_m'):
    cmap = Windfinder_cmap
    vmin = 0
    vmax = 35
elif key3.endswith('_turb'):
    cmap = 'viridis'
    vmin = 0
    vmax = 1
else:
    cmap = 'viridis'
    vmin = None
    vmax = None
    LFB.scatterplot(LFB.anemo_cleaned[key1][s1_ind].T[filter_idxs].T,LFB.acc_cleaned
```

2018_09_18 - 2018_10_18: AOA_mean VS Aox_C_std VS H_turb ['H08Wb' 'H18W' 'H20W' 'H24W'] - cleaned - without traffic







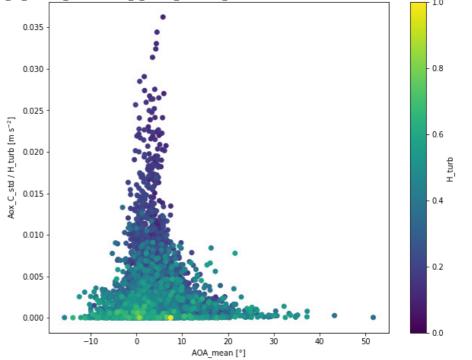


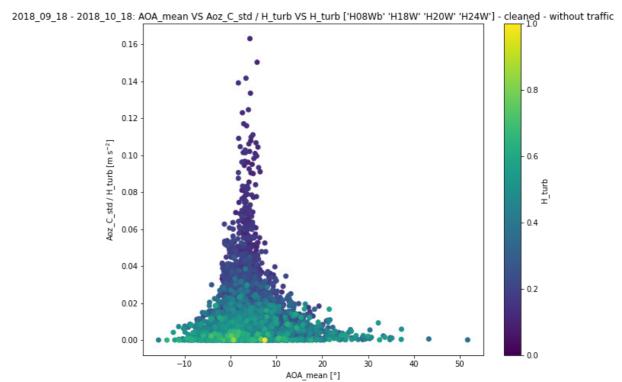
```
key1 = 'AOA_mean'
key2s_of_interest = ['Aox_C_std','Aoz_C_std','theta_std']
key3 = 'H_turb'
for key2 in key2s_of_interest:
    selected_sensors_key1=['H08Wb','H18W','H20W','H24W']
    selected_sensors_key2=['H09','H18','H24','H30']
    selected_sensors_key3=['H08Wb','H18W','H20W','H24W']
    s1_ind = LFB.get_ok_sensor_ind(sensor_names=selected_sensors_key1,sensor_type='a
    s2_ind = LFB.get_ok_sensor_ind(sensor_names=selected_sensors_key2,sensor_type='a
    s3_ind = LFB.get_ok_sensor_ind(sensor_names=selected_sensors_key3,sensor_type='a
    if key3.startswith('AOA_m'):
        cmap = 'coolwarm'
```

```
vmin = -15
vmax = 15
elif key3.startswith('H_m'):
    cmap = Windfinder_cmap
    vmin = 0
    vmax = 35
elif key3.endswith('_turb'):
    cmap = 'viridis'
    vmin = 0
    vmax = 1
else:
    cmap = 'viridis'
    vmin = None
    vmax = None

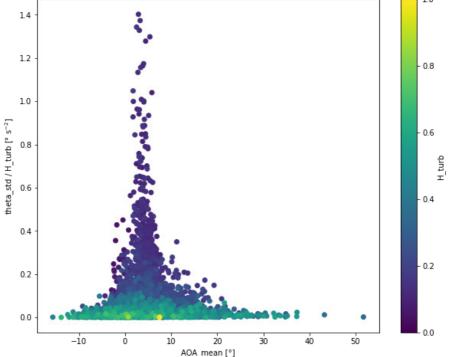
LFB.scatterplot(LFB.anemo_cleaned[key1][s1_ind].T[filter_idxs].T,LFB.acc_cleaned
```

2018_09_18 - 2018_10_18: AOA_mean VS Aox_C_std / H_turb VS H_turb ['H08Wb' 'H18W' 'H20W' 'H24W'] - cleaned - without traffic







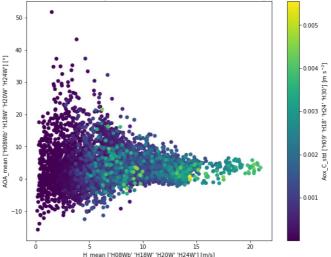


Below are more examples for different combinations of measurements in a scatterplot.

Anemo VS Anemo VS Acc - Wind response

Lateral

```
In [ ]:
         key1 = 'H mean'
         key2 = 'AOA_mean'
         key3 = 'Aox_C_std'
         print('ok anemometers for ',key1,':',LFB.anemo_names[LFB.anemo_ok_sensor_id[key1]])
         print('ok anemometers for ',key2,':',LFB.anemo_names[LFB.anemo_ok_sensor_id[key2]])
         print('ok accelerometers for ',key3,':',LFB.acc_names[LFB.acc_ok_sensor_id[key3]])
         selected_sensors_key1=['H08Wb','H18W','H20W','H24W']
         selected_sensors_key2=['H08Wb','H18W','H20W','H24W']
         selected_sensors_key3=['H09','H18','H24','H30']
         s1_ind = LFB.get_ok_sensor_ind(sensor_names=selected_sensors_key1,sensor_type='anemo
         s2_ind = LFB.get_ok_sensor_ind(sensor_names=selected_sensors_key2,sensor_type='anemo
         s3 ind = LFB.get ok sensor ind(sensor names=selected sensors key3, sensor type='acc',
         LFB.scatterplot(LFB.anemo_cleaned[key1][s1_ind].T[filter_idxs].T,LFB.anemo_cleaned[k
        ok anemometers for H mean : ['H08Wb' 'H08Wt' 'H08E' 'H10W' 'H10E' 'H18W' 'H18E' 'H2
        0W' 'H24W']
        ok anemometers for AOA_mean : ['H08Wb' 'H08Wt' 'H08E' 'H10E' 'H18W' 'H18E' 'H20W'
        ok accelerometers for Aox_C_std : ['H09' 'H18' 'H24' 'H30']
```



```
In [ ]:
          key1 = 'H_mean'
          key2 = 'H_turb'
          key3 = 'Aox_C_std'
          print('ok anemometers for ',key1,':',LFB.anemo_names[LFB.anemo_ok_sensor_id[key1]])
          print('ok anemometers for ',key2,':',LFB.anemo_names[LFB.anemo_ok_sensor_id[key2]])
          print('ok accelerometers for ',key3,':',LFB.acc_names[LFB.acc_ok_sensor_id[key3]])
          selected_sensors_key1=['H08Wb','H18W','H20W','H24W']
          selected_sensors_key2=['H08Wb','H18W','H20W','H24W']
          selected_sensors_key3=['H09','H18','H24','H30']
          s1_ind = LFB.get_ok_sensor_ind(sensor_names=selected_sensors_key1,sensor_type='anemo
          s2_ind = LFB.get_ok_sensor_ind(sensor_names=selected_sensors_key2,sensor_type='anemo
          s3_ind = LFB.get_ok_sensor_ind(sensor_names=selected_sensors_key3,sensor_type='acc',
          LFB.scatterplot(LFB.anemo_cleaned[key1][s1_ind].T[filter_idxs].T,LFB.anemo_cleaned[k
         ok anemometers for H_mean : ['H08Wb' 'H08Wt' 'H08E' 'H10W' 'H10E' 'H18W' 'H18E' 'H2
         0W' 'H24W']
         ok anemometers for H_{turb} : ['H08Wb' 'H08Wt' 'H08E' 'H10E' 'H18W' 'H18E' 'H20W' 'H2
         ok accelerometers for Aox_C_std : ['H09' 'H18' 'H24' 'H30']
         2018_09_18 - 2018_10_18: H_mean ['H08Wb' 'H18W' 'H20W' 'H24W'] VS H_turb ['H08Wb' 'H18W' 'H20W' 'H24W'] VS Aox_C_std ['H09' 'H18' 'H24' 'H30'] - cleaned - without traffic
                                  1.0
                                                                                 0.005
                                  0.8
                                                                                 0.004
                                 'H18W' 'H20W' 'H24W']
                                  0.2
                                                                                 0.001
```

Vertical

```
In [ ]:
    key1 = 'H_mean'
    key2 = 'AOA_mean'
    key3 = 'Aoz_C_std'
    print('ok anemometers for ',key1,':',LFB.anemo_names[LFB.anemo_ok_sensor_id[key1]])
```

H_mean ['H08Wb' 'H18W' 'H20W' 'H24W'] [m/s]

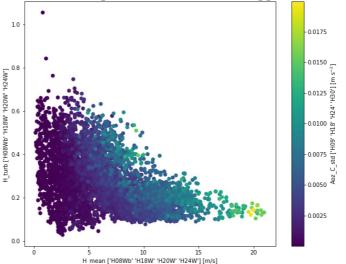
20

```
print('ok anemometers for ',key2,':',LFB.anemo_names[LFB.anemo_ok_sensor_id[key2]])
 print('ok accelerometers for ',key3,':',LFB.acc_names[LFB.acc_ok_sensor_id[key3]])
 selected_sensors_key1=['H08Wb','H18W','H20W','H24W']
 selected_sensors_key2=['H08Wb','H18W','H20W','H24W']
 selected_sensors_key3=['H09','H18','H24','H30']
 s1_ind = LFB.get_ok_sensor_ind(sensor_names=selected_sensors_key1,sensor_type='anemo'
 s2_ind = LFB.get_ok_sensor_ind(sensor_names=selected_sensors_key2,sensor_type='anemo'
 s3_ind = LFB.get_ok_sensor_ind(sensor_names=selected_sensors_key3,sensor_type='acc',
LFB.scatterplot(LFB.anemo_cleaned[key1][s1_ind].T[filter_idxs].T,LFB.anemo_cleaned[k
ok anemometers for H mean : ['H08Wb' 'H08Wt' 'H08E' 'H10W' 'H10E' 'H18W' 'H18E' 'H2
0W' 'H24W']
ok anemometers for AOA_mean : ['H08Wb' 'H08Wt' 'H08E' 'H10E' 'H18W' 'H18E' 'H20W'
'H24W']
ok accelerometers for Aoz_C_std : ['H09' 'H18' 'H24' 'H30']
2018_09_18 - 2018_10_18: H_mean ['H08Wb' 'H18W' 'H20W' 'H24W'] VS AOA_mean ['H08Wb' 'H18W' 'H20W' 'H24W'] VS Aoz_C_std ['H09' 'H18' 'H24' 'H30'] - cleaned - without traffic
                                                                       0.0175
                                                                       0.0150
                        'H24W'] [°]
                                                                       0.0125 P
                        WOCH.
                        'H18W'
                                                                       0.0100
                        ['H08Wb'
                                                                       0.0075
                        AOA
                                                                       0.0050
                                                                       0.0025
                                     H_mean ['H08Wb' 'H18W' 'H20W' 'H24W'] [m/s]
 key1 = 'H mean'
 key2 = 'H_turb'
 key3 = 'Aoz_C_std'
 print('ok anemometers for ',key1,':',LFB.anemo_names[LFB.anemo_ok_sensor_id[key1]])
 print('ok anemometers for ',key2,':',LFB.anemo_names[LFB.anemo_ok_sensor_id[key2]])
 print('ok accelerometers for ',key3,':',LFB.acc_names[LFB.acc_ok_sensor_id[key3]])
 selected_sensors_key1=['H08Wb','H18W','H20W','H24W']
 selected_sensors_key2=['H08Wb','H18W','H20W','H24W']
 selected_sensors_key3=['H09','H18','H24','H30']
 s1_ind = LFB.get_ok_sensor_ind(sensor_names=selected_sensors_key1,sensor_type='anemo
```

In []:

```
LFB.scatterplot(LFB.anemo_cleaned[key1][s1_ind].T[filter_idxs].T,LFB.anemo_cleaned[k
ok anemometers for H_mean : ['H08Wb' 'H08Wt' 'H08E' 'H10W' 'H10E' 'H18W' 'H18E' 'H2
0W' 'H24W']
ok anemometers for H_turb : ['H08Wb' 'H08Wt' 'H08E' 'H10E' 'H18W' 'H18E' 'H20W' 'H2
4W']
ok accelerometers for Aoz_C_std : ['H09' 'H18' 'H24' 'H30']
```

s2_ind = LFB.get_ok_sensor_ind(sensor_names=selected_sensors_key2, sensor_type='anemo
s3 ind = LFB.get ok sensor ind(sensor names=selected sensors key3, sensor type='acc',



Torsional

```
In [ ]:
          key1 = 'H_mean'
          key2 = 'AOA_mean'
          key3 = 'theta_std'
          print('ok anemometers for ',key1,':',LFB.anemo_names[LFB.anemo_ok_sensor_id[key1]])
          print('ok anemometers for ',key2,':',LFB.anemo_names[LFB.anemo_ok_sensor_id[key2]])
          print('ok accelerometers for ',key3,':',LFB.acc_names[LFB.acc_ok_sensor_id[key3]])
          selected_sensors_key1=['H08Wb','H18W','H20W','H24W']
          selected_sensors_key2=['H08Wb','H18W','H20W','H24W']
          selected_sensors_key3=['H09','H18','H24','H30']
          s1_ind = LFB.get_ok_sensor_ind(sensor_names=selected_sensors_key1,sensor_type='anemo'
          s2_ind = LFB.get_ok_sensor_ind(sensor_names=selected_sensors_key2,sensor_type='anemo'
          s3_ind = LFB.get_ok_sensor_ind(sensor_names=selected_sensors_key3,sensor_type='acc',
          LFB.scatterplot(LFB.anemo_cleaned[key1][s1_ind].T[filter_idxs].T,LFB.anemo_cleaned[k
         ok anemometers for H_mean : ['H08Wb' 'H08Wt' 'H08E' 'H10W' 'H10E' 'H18W' 'H18E' 'H2
         0W' 'H24W']
         ok anemometers for AOA_mean : ['H08Wb' 'H08Wt' 'H08E' 'H10E' 'H18W' 'H18E' 'H20W'
         'H24W']
         ok accelerometers for theta std : ['H09' 'H18' 'H24' 'H30']
         2018_09_18 - 2018_10_18: H_mean ['H08Wb' 'H18W' 'H20W' 'H24W'] VS AOA_mean ['H08Wb' 'H18W' 'H20W' 'H24W'] VS theta_std ['H09' 'H18' 'H24' 'H30'] - cleaned - without traffic
                                                                                  0.200
                                  "H18W" "H20W" "H24W"] [°]
                                                                                  0.150
                                                                                  0.125
                                  mean ['H08Wb'
                                    10
                                                                                  0.050
                                                                                  0.025
```

```
key1 = 'H_mean'
key2 = 'H_turb'
key3 = 'theta_std'
print('ok anemometers for ',key1,':',LFB.anemo_names[LFB.anemo_ok_sensor_id[key1]])
```

H mean ['H08Wb' 'H18W' 'H20W' 'H24W'] [m/s]

```
print('ok anemometers for ',key2,':',LFB.anemo_names[LFB.anemo_ok_sensor_id[key2]])
 print('ok accelerometers for ',key3,':',LFB.acc_names[LFB.acc_ok_sensor_id[key3]])
 selected_sensors_key1=['H08Wb','H18W','H20W','H24W']
 selected_sensors_key2=['H08Wb','H18W','H20W','H24W']
 selected_sensors_key3=['H09','H18','H24','H30']
 s1_ind = LFB.get_ok_sensor_ind(sensor_names=selected_sensors_key1,sensor_type='anemo'
 s2_ind = LFB.get_ok_sensor_ind(sensor_names=selected_sensors_key2,sensor_type='anemo'
 s3_ind = LFB.get_ok_sensor_ind(sensor_names=selected_sensors_key3,sensor_type='acc',
LFB.scatterplot(LFB.anemo_cleaned[key1][s1_ind].T[filter_idxs].T,LFB.anemo_cleaned[k
ok anemometers for H_mean : ['H08Wb' 'H08Wt' 'H08E' 'H10W' 'H10E' 'H18W' 'H18E' 'H2
0W' 'H24W']
ok anemometers for H_turb : ['H08Wb' 'H08Wt' 'H08E' 'H10E' 'H18W' 'H18E' 'H20W' 'H2
4W']
ok accelerometers for theta_std : ['H09' 'H18' 'H24' 'H30']
2018_09_18 - 2018_10_18: H_mean ['H08Wb' 'H18W' 'H20W' 'H24W'] V5 H_turb ['H08Wb' 'H18W' 'H20W' 'H24W'] V5 theta_std ['H09' 'H18' 'H24' 'H30'] - cleaned - without traffic
                          1.0
                                                                           0.200
                                                                           0.175
                         'H24W']
                                                                           0.150
                         "H20W"
                                                                           0.125
                          0.6
                         ['H08Wb' 'H18W'
                                                                           0.075
                                                                           0.050
                          0.2
                                                                           0.025
                          0.0
                                      H_mean ['H08Wb' 'H18W' 'H20W' 'H24W'] [m/s]
```

Anemo VS Acc VS Acc - Wind response

```
In [ ]:
         key1 = 'H mean'
         key2 = 'Aoz_C_std'
         key3 = 'Aoz_C_max_by_std'
         print('ok anemometers for ',key1,':',LFB.anemo_names[LFB.anemo_ok_sensor_id[key1]])
         print('ok accelerometers for ',key2,':',LFB.acc_names[LFB.acc_ok_sensor_id[key2]])
         print('ok accelerometers for ',key3,':',LFB.acc_names[LFB.acc_ok_sensor_id[key3]])
selected_sensors_key1=['H08Wb','H18W','H20W','H24W']
         selected_sensors_key2=['H09','H18','H24','H30']
         selected sensors key3=['H09','H18','H24','H30']
         s1 ind = LFB.get ok sensor ind(sensor names=selected sensors key1, sensor type='anemo
         s2_ind = LFB.get_ok_sensor_ind(sensor_names=selected_sensors_key2,sensor_type='acc',
         s3_ind = LFB.get_ok_sensor_ind(sensor_names=selected_sensors_key3,sensor_type='acc',
         LFB.scatterplot(LFB.anemo_cleaned[key1][s1_ind].T[filter_idxs].T,LFB.acc_cleaned[key
         ok anemometers for H_mean : ['H08Wb' 'H08Wt' 'H08E' 'H10W' 'H10E' 'H18W' 'H18E' 'H2
         0W' 'H24W']
         ok accelerometers for Aoz C std : ['H09' 'H18' 'H24' 'H30']
         ok accelerometers for Aoz C max by std : ['H09' 'H18' 'H24' 'H30']
```

Acc VS Anemo VS Acc - Wind response

```
In [ ]:
          key1 = 'Aoz_C_std'
          key2 = 'H turb'
          key3 = 'Aoz_C_max_by_std'
          print('ok anemometers for ',key1,':',LFB.acc_names[LFB.acc_ok_sensor_id[key1]])
          print('ok anemometers for ',key2,':',LFB.anemo_names[LFB.anemo_ok_sensor_id[key2]])
          print('ok accelerometers for ',key3,':',LFB.acc_names[LFB.acc_ok_sensor_id[key3]])
          selected_sensors_key1=['H09','H18','H24','H30']
          selected_sensors_key2=['H08Wb','H18W','H20W','H24W']
          selected_sensors_key3=['H09','H18','H24','H30']
          s1_ind = LFB.get_ok_sensor_ind(sensor_names=selected_sensors_key1,sensor_type='acc',
          s2_ind = LFB.get_ok_sensor_ind(sensor_names=selected_sensors_key2,sensor_type='anemo'
          s3_ind = LFB.get_ok_sensor_ind(sensor_names=selected_sensors_key3,sensor_type='acc',
          LFB.scatterplot(LFB.acc_cleaned[key1][s1_ind].T[filter_idxs].T,LFB.anemo_cleaned[key
         ok anemometers for Aoz_C_std : ['H09' 'H18' 'H24' 'H30']
         ok anemometers for H turb : ['H08Wb' 'H08Wt' 'H08E' 'H10E' 'H18W' 'H18E' 'H20W' 'H2
         ok accelerometers for Aoz_C_max_by_std : ['H09' 'H18' 'H24' 'H30']
         2018_09_18 - 2018_10_18: Aoz_C_std ['H09' 'H18' 'H24' 'H30'] VS H_turb ['H08Wb' 'H18W' 'H20W' 'H24W'] VS Aoz_C_max_by_std ['H09' 'H18' 'H24' 'H30'] - cleaned - without traffic
                                    1.0
                                                                                   4oz_C_max_by_std ['H09' 'H18' 'H24' 'H30']
                                  'H24W'
                                    0.6
                                    0.2
                                                    0.0075 0.0100
                                                            0.0125 0.0150
                                                                      0.0175 0.0200
```

Acc VS Acc VS Anemo - Wind response

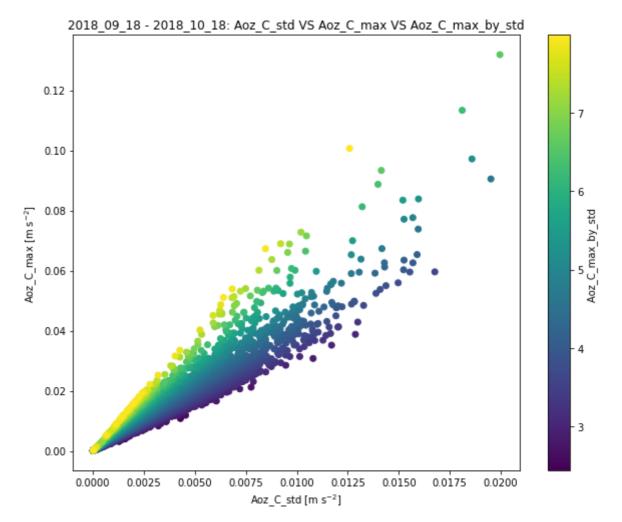
```
key1 = 'Aoz_C_std'
key2 = 'Aoz_C_max'
key3 = 'H_mean'
print('ok anemometers for ',key1,':',LFB.acc_names[LFB.acc_ok_sensor_id[key1]])
print('ok anemometers for ',key2,':',LFB.acc_names[LFB.acc_ok_sensor_id[key2]])
print('ok accelerometers for ',key3,':',LFB.anemo_names[LFB.anemo_ok_sensor_id[key3]])
selected_sensors_key1=['H09','H18','H24','H30']
```

Aoz C std ['H09' 'H18' 'H24' 'H30'] [m s-2]

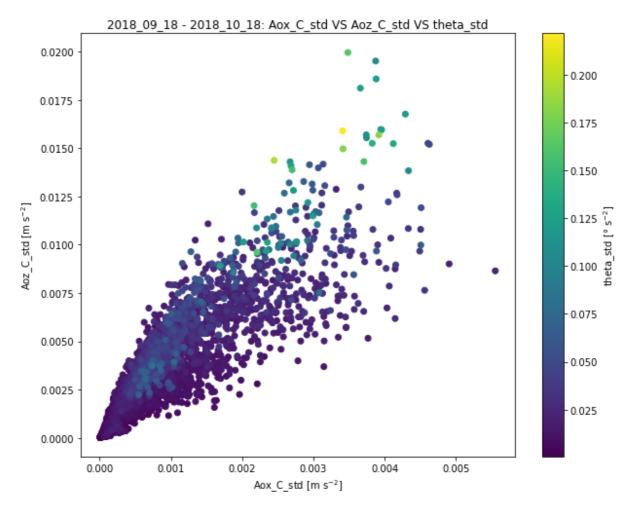
```
selected_sensors_key3=['H08Wb','H18W','H20W','H24W']
 s1_ind = LFB.get_ok_sensor_ind(sensor_names=selected_sensors_key1,sensor_type='acc',
 s2_ind = LFB.get_ok_sensor_ind(sensor_names=selected_sensors_key2,sensor_type='acc',
 s3_ind = LFB.get_ok_sensor_ind(sensor_names=selected_sensors_key3,sensor_type='anemo
 if key3.startswith('AOA m'):
      cmap = 'coolwarm'
      vmin = -15
      vmax = 15
 elif key3.startswith('H_m'):
      cmap = Windfinder_cmap
      vmin = 0
      vmax = 35
 elif key3.endswith('_turb'):
      cmap = 'viridis'
      vmin = 0
      vmax = 1
 else:
      cmap = 'viridis'
      vmin = None
      vmax = None
 LFB.scatterplot(LFB.acc_cleaned[key1][s1_ind].T[filter_idxs].T,LFB.acc_cleaned[key2]
ok anemometers for Aoz_C_std : ['H09' 'H18' 'H24' 'H30']
ok anemometers for Aoz_C_max : ['H09' 'H18' 'H24' 'H30']
ok accelerometers for H_mean : ['H08Wb' 'H08Wt' 'H08E' 'H10W' 'H10E' 'H18W' 'H18E'
'H20W' 'H24W']
2018_09_18 - 2018_10_18: Aoz_C_std ['H09' 'H18' 'H24' 'H30'] VS Aoz_C_max ['H09' 'H18' 'H24' 'H30'] VS H_mean ['H08Wb' 'H18W' 'H22W' 'H24W'] - cleaned - without traffic
                          0.150
                                                                                72 TS W.1 Lm/s1
                        4oz C max ['H09' 'H18' 'H24' 'H30'] [m s<sup>-2</sup>]
                          0.100
                                                                                 'H18W'
                                                                                10 g
                          0.050
                          0.025
                          0.000
                                                         [ 4.36 -0. ]
                                                                 --- [ 4.36 -0. 1
                                                           0.020
                                       0.005
                                             0.010
                                                    0.015
                                                                  0.025
```

Acc VS Acc vs Acc - Acceleration characteristics

```
key1 = 'Aoz_C_std'
key2 = 'Aoz_C_max'
key3 = 'Aoz_C_max_by_std'
common_ok_sensors,s1_ind,s2_ind = LFB.find_common_ok_sensors(LFB.acc_ok_sensor_id[ke
common_ok_sensors,stemp_ind,s3_ind = LFB.find_common_ok_sensors(common_ok_sensors,LF
s1_ind = list(np.array(s1_ind)[stemp_ind])
s2_ind = list(np.array(s2_ind)[stemp_ind])
LFB.scatterplot(LFB.acc_cleaned[key1][s1_ind].T[filter_idxs].T,LFB.acc_cleaned[key2]
```

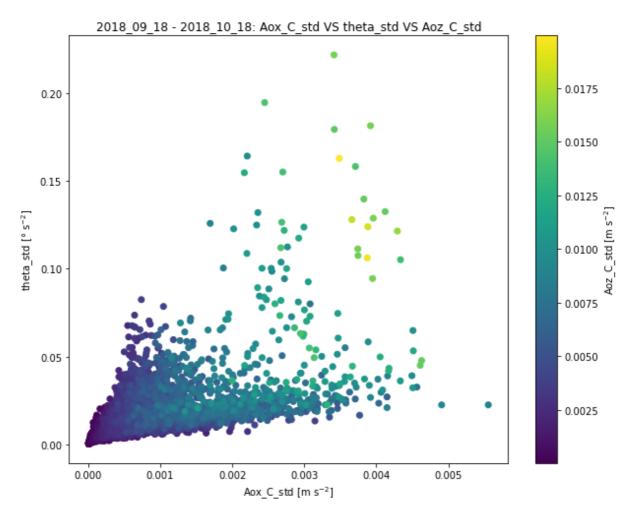


```
key1 = 'Aox_C_std'
key2 = 'Aoz_C_std'
key3 = 'theta_std'
common_ok_sensors,s1_ind,s2_ind = LFB.find_common_ok_sensors(LFB.acc_ok_sensor_id[ke
common_ok_sensors,stemp_ind,s3_ind = LFB.find_common_ok_sensors(common_ok_sensors,LF
s1_ind = list(np.array(s1_ind)[stemp_ind])
s2_ind = list(np.array(s2_ind)[stemp_ind])
LFB.scatterplot(LFB.acc_cleaned[key1][s1_ind].T[filter_idxs].T,LFB.acc_cleaned[key2]
```



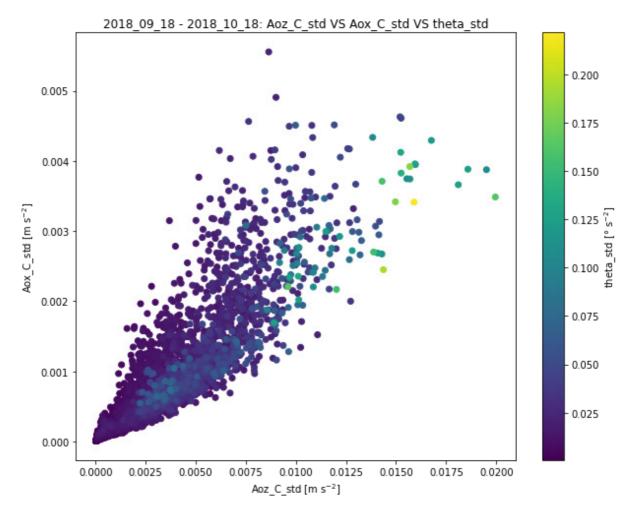
```
In []:
    key1 = 'Aox_C_std'
    key2 = 'theta_std'
    key3 = 'Aoz_C_std'
    common_ok_sensors,s1_ind,s2_ind = LFB.find_common_ok_sensors(LFB.acc_ok_sensor_id[ke common_ok_sensors,stemp_ind,s3_ind = LFB.find_common_ok_sensors(common_ok_sensors,LF s1_ind = list(np.array(s1_ind)[stemp_ind])
    s2_ind = list(np.array(s2_ind)[stemp_ind])

LFB.scatterplot(LFB.acc_cleaned[key1][s1_ind].T[filter_idxs].T,LFB.acc_cleaned[key2]
```



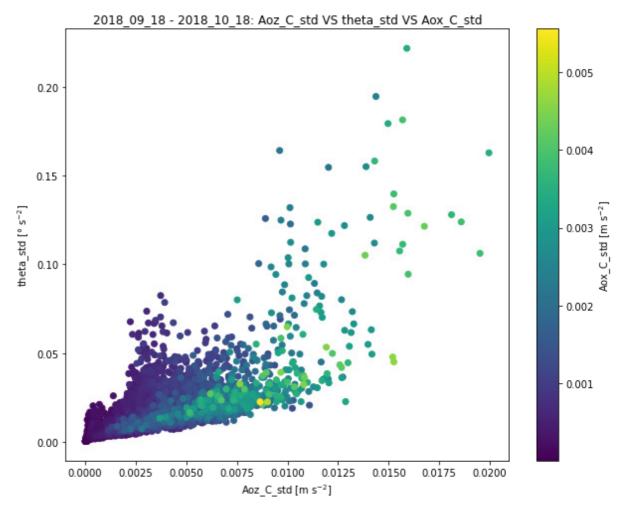
```
In []:
    key1 = 'Aoz_C_std'
    key2 = 'Aox_C_std'
    key3 = 'theta_std'
    common_ok_sensors,s1_ind,s2_ind = LFB.find_common_ok_sensors(LFB.acc_ok_sensor_id[ke common_ok_sensors,stemp_ind,s3_ind = LFB.find_common_ok_sensors(common_ok_sensors,LF s1_ind = list(np.array(s1_ind)[stemp_ind])
    s2_ind = list(np.array(s2_ind)[stemp_ind])

LFB.scatterplot(LFB.acc_cleaned[key1][s1_ind].T[filter_idxs].T,LFB.acc_cleaned[key2]
```



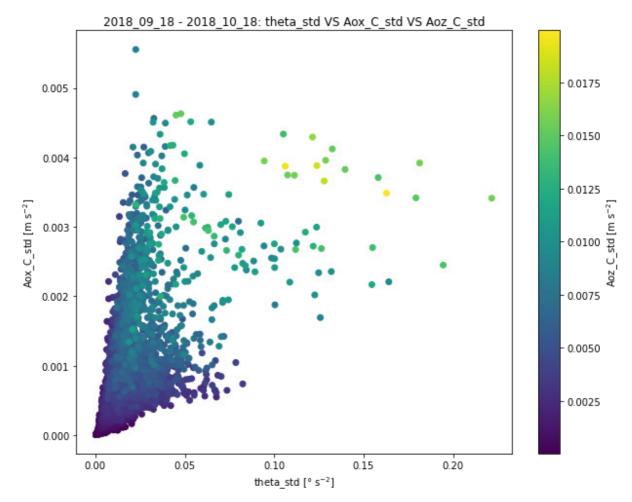
```
In []:
    key1 = 'Aoz_C_std'
    key2 = 'theta_std'
    key3 = 'Aox_C_std'
    common_ok_sensors,s1_ind,s2_ind = LFB.find_common_ok_sensors(LFB.acc_ok_sensor_id[ke common_ok_sensors,stemp_ind,s3_ind = LFB.find_common_ok_sensors(common_ok_sensors,LF s1_ind = list(np.array(s1_ind)[stemp_ind])
    s2_ind = list(np.array(s2_ind)[stemp_ind])

LFB.scatterplot(LFB.acc_cleaned[key1][s1_ind].T[filter_idxs].T,LFB.acc_cleaned[key2]
```

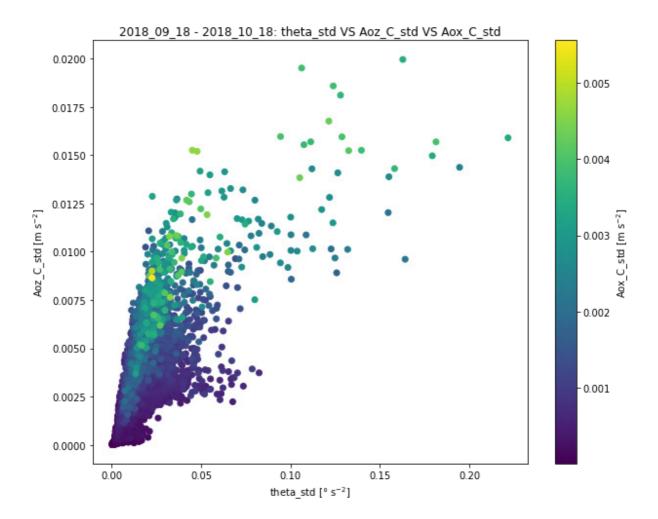


```
In []:
    key1 = 'theta_std'
    key2 = 'Aox_C_std'
    key3 = 'Aoz_C_std'
    common_ok_sensors,s1_ind,s2_ind = LFB.find_common_ok_sensors(LFB.acc_ok_sensor_id[ke common_ok_sensors,stemp_ind,s3_ind = LFB.find_common_ok_sensors(common_ok_sensors,LF s1_ind = list(np.array(s1_ind)[stemp_ind])
    s2_ind = list(np.array(s2_ind)[stemp_ind])

LFB.scatterplot(LFB.acc_cleaned[key1][s1_ind].T[filter_idxs].T,LFB.acc_cleaned[key2]
```



```
key1 = 'theta_std'
key2 = 'Aoz_C_std'
key3 = 'Aox_C_std'
common_ok_sensors,s1_ind,s2_ind = LFB.find_common_ok_sensors(LFB.acc_ok_sensor_id[ke common_ok_sensors,stemp_ind,s3_ind = LFB.find_common_ok_sensors(common_ok_sensors,LF s1_ind = list(np.array(s1_ind)[stemp_ind])
s2_ind = list(np.array(s2_ind)[stemp_ind])
LFB.scatterplot(LFB.acc_cleaned[key1][s1_ind].T[filter_idxs].T,LFB.acc_cleaned[key2]
```



Correlation matrices

Below are some correlation matrices for relevant measurements, selected using keys_of_interst .

```
In [ ]:
# keys_of_interest = ['H_mean','H_turb','W_mean','W_turb','Vx_mean','Vx_turb','Vy_me
keys_of_interest = ['H_mean','H_turb','AOA_mean','Aox_C_std','Aoz_C_std','theta_std'
```

Anemo & Anemo - Wind characteristics

```
filter_idxs = np.arange(len(LFB.time_array_cleaned)); title_suffix = ' - cleaned'
# filter_idxs = LFB.filter_data(LFB.traffic_cleaned,prior_idxs=filter_idxs,zeros=Tru
```

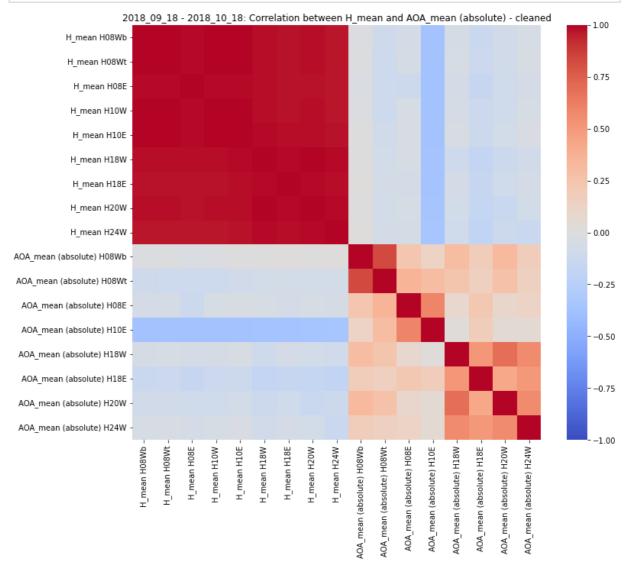
Batch-processing using two nested *for-loops* over key1 and key2 is used. *if-statements* are used to selectively process *keys* from keys_of_interest and process each key pairing only once. Another *if-statement* is used to apply the absolute opperation np.abs to data of keys starting with 'AOA_m' only.

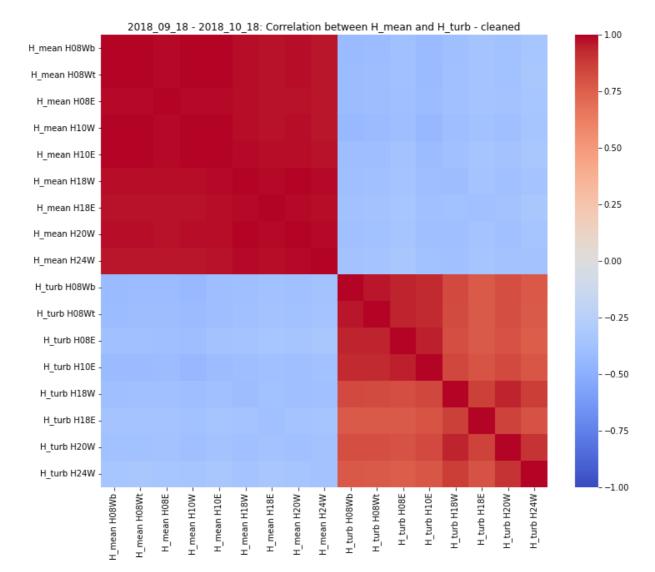
```
data1 = LFB.anemo_cleaned[key1].T[filter_idxs].T
    title1_suffix = ''

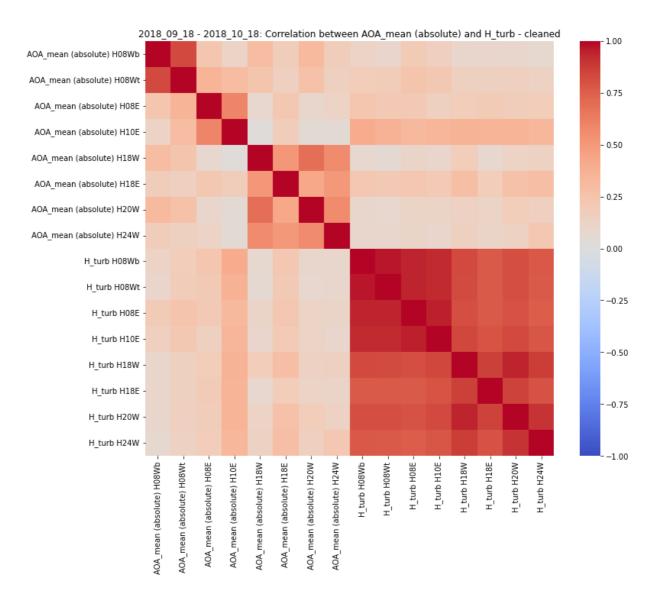
if key2.startswith('AOA_m'):
    data2 = np.abs(LFB.anemo_cleaned[key2].T[filter_idxs].T)
    title2_suffix = ' (absolute)'

else:
    data2 = LFB.anemo_cleaned[key2].T[filter_idxs].T
    title2_suffix = ''

LFB.correlation_matrix(data1,data2,title1=key1+title1_suffix,tit)
```



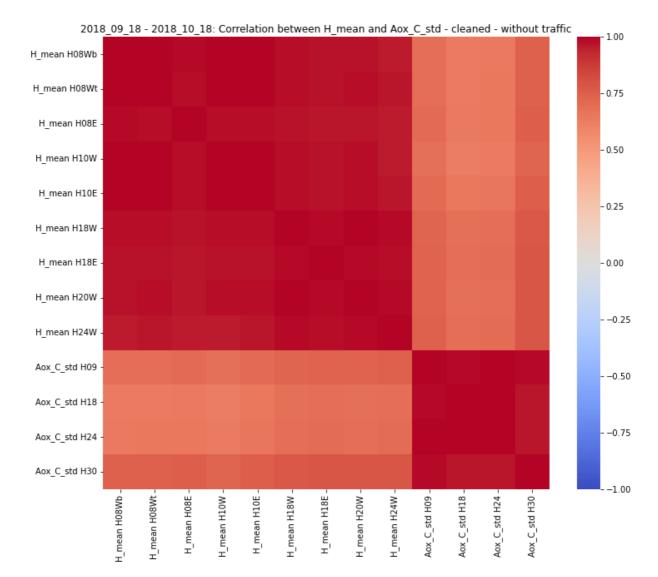


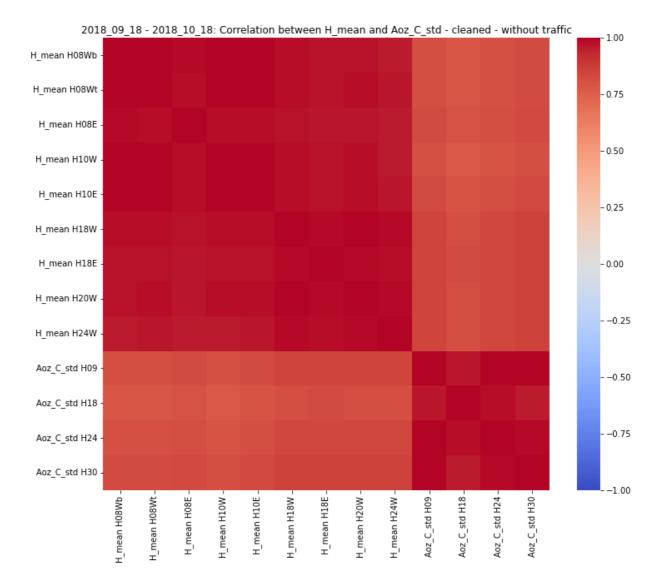


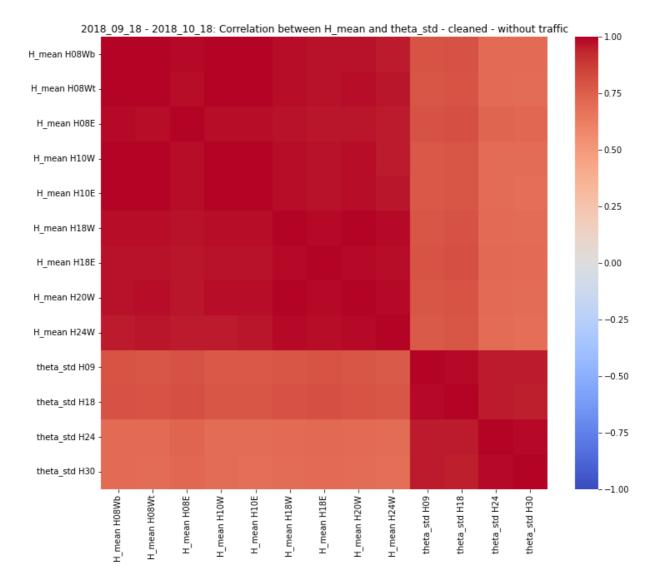
Anemo & Acc - Wind response

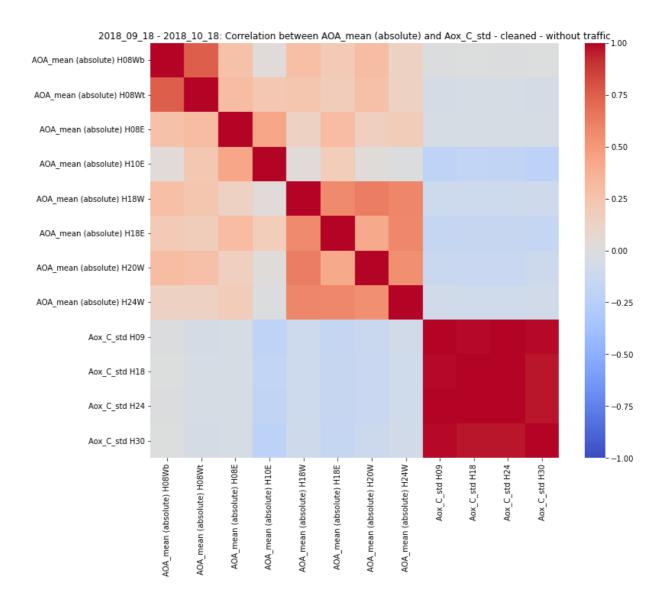
For correlations with accelerometer data the data is filtered for traffic, as only the wind response is of interest.

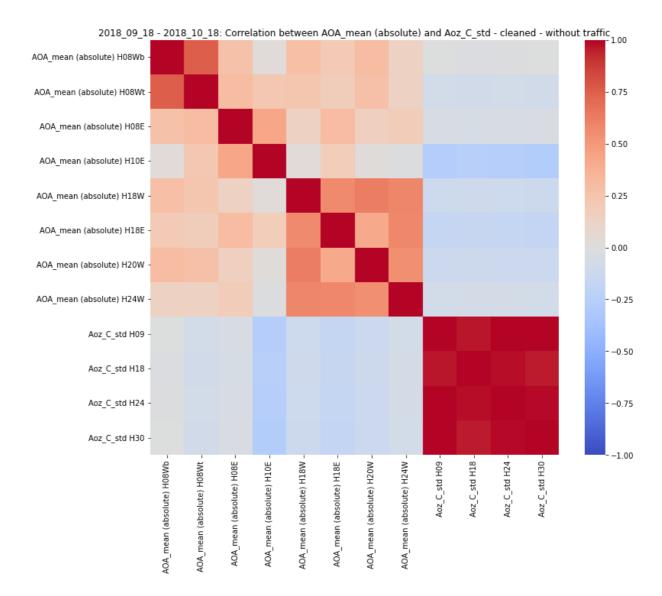
```
In [ ]:
         filter_idxs = np.arange(len(LFB.time_array_cleaned)); title_suffix = ' - cleaned'
         filter_idxs = LFB.filter_data(LFB.traffic_cleaned,prior_idxs=filter_idxs,zeros=True,
In [ ]:
         for key1_num, key1 in enumerate(LFB.anemo_cleaned.keys()):
             if key1 in keys_of_interest:
                 for key2_num, key2 in enumerate(LFB.acc_cleaned.keys()):
                     if key2 in keys of interest:
                         if key1.startswith('AOA m'):
                             data1 = np.abs(LFB.anemo_cleaned[key1].T[filter_idxs].T)
                             title1_suffix = ' (absolute)'
                         else:
                             data1 = LFB.anemo_cleaned[key1].T[filter_idxs].T
                             title1_suffix = ''
                         data2 = LFB.acc_cleaned[key2].T[filter_idxs].T
                         title2 suffix = ''
                         LFB.correlation matrix(data1,data2,title1=key1+title1 suffix,title2=
```

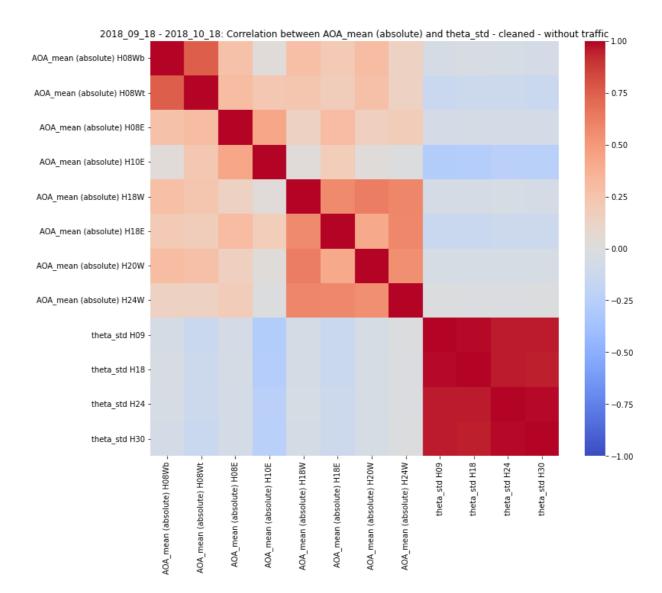


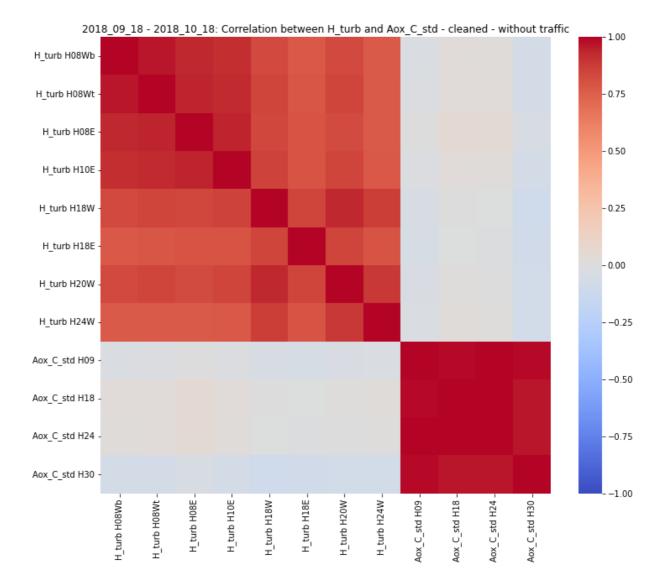


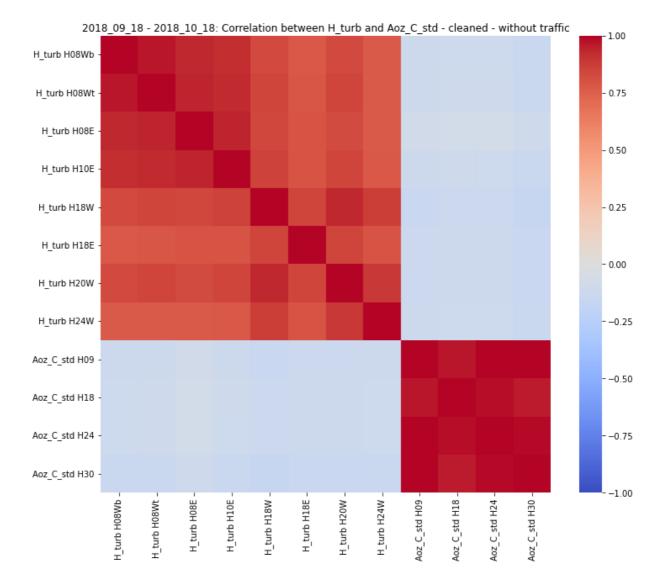


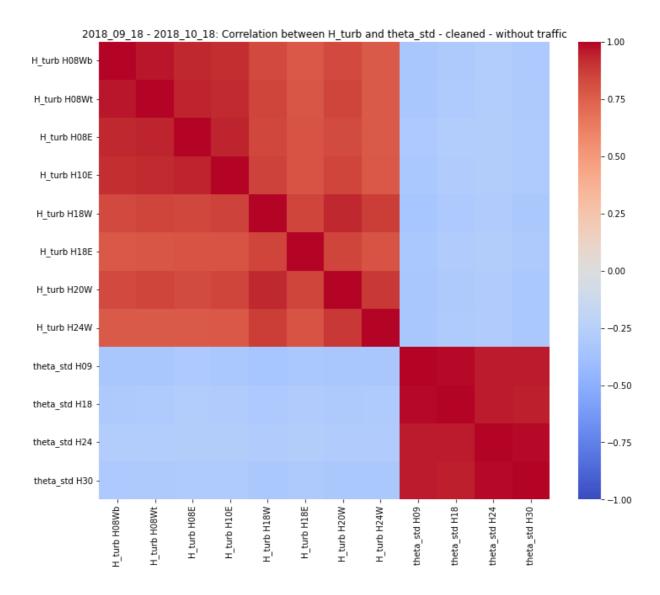












Acc & Acc - Acceleration characteristics

