

# Numerical investigation on rock fragmentation under decoupled charge blasting

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**Abstract:** Blasting using decoupled charge is extensively applied in rock excavation and rock fragmentation. In this study, the rock fragmentation induced by blasting using decoupled charge is investigated by combined finite element modelling and image-processing. After calibrating the numerical model developed in LS-DYNA against the fragment morphology and fragmentation size distribution (FSD) in three air-coupling blasts and three water-coupling blasts, a series of cubic single-hole models are constructed to simulate rock cracking induced by decoupled charge blasting with various decoupling ratios, distinct coupling mediums and different decoupled charge modes. The simulated fracture networks are obtained by blanking the damaged elements whose damage level is over the threshold of crack formation, and the resulting crack patterns are image-processed using ImageJ to identify fragment size. Then, the blast-created FSDs are characterized by a three-parameter generalized extreme value function, and the FSDs with decoupling ratios, coupling mediums and different decoupled charge modes are quantitatively analyzed and compared. The results show that rock fragmentation becomes finer and the FSD range gets narrower with the decrease in decoupling ratio. Meanwhile, smaller fragment sizes and narrower FSD spans are obtained when changing coupling material from air to water and altering radial decoupling to axial decoupling.

**Keywords:** Decoupled charge blasting, Rock fragmentation, coupling medium, Numerical simulation.

## 26 **1 Introduction**

27       Drilling and blasting is the most effective technique for rock excavation and rock  
28 fragmentation in mining, and the rock fragmentation caused by blasting is the first stage of the  
29 production in mining industry, which plays a significant role in delivering marketable products  
30 (An et al., 2017; Li et al., 2022; Tao et al., 2020; Wang et al., 2021a; Yi et al., 2017a, 2017b).  
31 In controlled blasting and some production blasting, the borehole is generally decoupled  
32 charged, and the rock fracturing in blasting is greatly influenced by decoupled charge mode  
33 (radial decoupling charge and axial decoupling charge), decoupling ratio (defined as the  
34 borehole diameter over charge diameter  $K_r$  in radial decoupling blasting and hole length  
35 without stemming over charge length  $K_a$  in axial decoupling blasting) and coupling medium.  
36 Therefore, it is necessary to investigate the behaviour of rock breakage under blasting using  
37 decoupled charge for improving the performance in rock excavation and rock fragmentation  
38 with controlled blasting and production blasting.

39       In conventional blasting, i.e. fully coupled charge blasting, the rock near the borehole is  
40 severely pulverized due to violent detonation pressure, and the overall development of rock  
41 fracture is extremely unstable because the bifurcation and coalescence of cracks successively  
42 occur with fine or small scales, resulting in that the rock disintegration in surrounding rock is  
43 often in excess of the requirement (Diehl et al., 2000; Han et al., 2020; Kutter and Fairhurst,  
44 1971). To respond to this situation, decoupled charge blasting is introduced and used in  
45 controlled blasting such as presplit blasting and smooth blasting to excavate rock in the desired  
46 manner and protect the reserved rock from severe damage (Langefors and Kihlström, 1978).  
47 In blasting using decoupled charge, including radially decoupled charge blast and axially  
48 decoupled charge blast, the coupling medium between the explosive and the borehole wall is  
49 strongly compressed by the high pressure generated by the expansion of detonation products  
50 so that the explosion shock/stress waves in coupling medium are rapidly decayed (Chen et al.,

51 2020). When the detonation-induced stress waves arrive at the borehole wall, they transmit and  
52 reflect at the interface between the coupling medium and rock several times until the blast-  
53 induced stress waves completely attenuate in the coupling medium. Hence, the peak pressure on  
54 borehole wall reduces and the duration of blast loading prolongs in decoupled charge blasting  
55 compared with those in blasting with fully coupled charge. With these mechanisms, as the gap  
56 between explosive and borehole wall becomes thicker, the amount of excessively shattering  
57 rock particles in the vicinity of borehole which are generated accompanying the rapidly  
58 forming and massively developed short cracks reduce. When the decoupled charge borehole is  
59 initiated with a large decoupling ratio, the rock fragmentation is mostly controlled by the  
60 propagation and interconnection of long cracks, and a radiation-shape fracture pattern is  
61 generated (Pál et al., 2014; Wittel et al., 2004), leading to the formation of large rock blocks.  
62 Consequently, the rock fragment size and its distribution range in decoupled charge blasting  
63 vary accordingly with the variation in decoupling ratio.

64 Moreover, the rock fragmentation induced by blasting is also influenced by the coupling  
65 medium. The air is the most commonly used coupling material in decoupled charge blasting.  
66 When air fills the gap between the explosive and hole-wall, the detonation products quickly  
67 expand after explosive initiation and fill the whole borehole because of the high compressibility  
68 of air such that a part of the detonation energy is consumed in air compression. Meanwhile,  
69 due to the air characteristic of low wave impedance, low transfer efficiency of explosion-  
70 induced stress from explosive to air and from air to rock is caused. With these mechanisms,  
71 decoupling with air can be employed to reduce extreme rock crushing and is usually applied to  
72 alleviate damage and vibration to the reserved rock (Liu et al., 2019; Singh et al., 2014; Tose,  
73 2006). Besides air, water is another frequently used coupling material in decoupled charge  
74 blasting, such as perimeter blasting of tunnelling, blasting for building demolition and blasting  
75 for permeability improvement in coal seam (Huang and Li, 2015; Yan and Xu, 2005; Yuan et

76 al., 2019). The water is generally characterized by incompressibility and low dissipation of  
77 explosion energy. During water-coupling blasting, the water in borehole works as an energy  
78 transfer layer and transmits much more energy into the rock mass than air owing to the low  
79 energy dissipation of explosion-induced stress waves in water, leading to the creation of smaller  
80 rock fragments (Cui et al., 2010; Jang et al., 2018). As a consequence, the fragmentation size  
81 distribution generated by decoupled charge blasting is distinctly governed by the filling  
82 medium on account of the significantly different mechanical properties of coupling materials.

83 Many investigations have been conducted on stress field evolution and fracture  
84 propagation under blasting using decoupled charge (Dehghani et al., 2020; Li et al., 2020;  
85 Liang et al., 2011; Wang et al., 2020; Xia et al., 2018). As early as 1981, the differences in  
86 explosion pressure and the fracture evolution between air-coupling blasting and water-coupling  
87 blasting were experimentally compared using plexiglass models by Fournery et al. (1981). The  
88 piezoelectric pressure transducers were applied to record pressure change during blasting and  
89 high-speed photography was used to view the dynamic crack evolution. It was found that there  
90 is an increase in both magnitude and duration of explosion pressure in water-coupling blasting  
91 compared to air-coupling one (blasting using a water-filled hole with one-fourth the amount of  
92 charge produces approximative pressure in rock and longer cracks, and the load duration is  
93 about 50% prolonged, compared with blasting using an air-filled hole), which appears to be  
94 very effective in initiating and propagating fractures. Using finite element modelling without  
95 element erosion or a similar algorithm in AUTODYN code, Zhu et al. (2007, 2008) compared  
96 the variations in rock fragmentation induced by blasting coupled with air, sand and water  
97 without considering the gas flow into "newly generated fractures", and it was pointed out that  
98 compared to the rock blasting with air-filled borehole, it is more efficient in rock breakage  
99 when filling the hole with sand or water, and the water coupling intensifies rock fragmentation  
100 most. Based on the model experiment, the effects of coupling mediums (air and plasticine) and

101 decoupling coefficients on stress evolution in blasting were investigated with high-speed  
102 digital image correlation by Yang et al. (2019). The test results showed that plasticine-coupling  
103 increases the peak of explosion-induced stress compared with air-coupling, and with the  
104 decoupling ratio increasing, the peak of explosion-induced stress reduces initially fast and then  
105 decreases slowly. The same pressure attenuation tendency was reported in the physical tests  
106 and numerical simulations (Discrete element method with PFC<sup>2D</sup>) on water-coupling blasting  
107 by Yuan et al. (2019), and they also pointed out that the distribution of the fracture network is  
108 strongly correlated to the explosion-induced stress attenuation and there is an optimal  
109 decoupling coefficient for the best performance of rock fragmentation. Similarly, the effects of  
110 decoupling ratios and coupling materials (air and clay) on the extent of the fractured zone in  
111 rock-like material (polymethyl methacrylate) were experimentally studied by Ding et al. (2020)  
112 using a digital laser dynamic caustics experimental system. The test results demonstrated that  
113 when taking clay as the filling medium, more and longer cracks were formed and the  
114 fragmentation was significantly improved. Meanwhile, the dynamic energy release rate of the  
115 propagation of blast-induced main cracks increases first and then decreases with the increase  
116 of decoupling coefficient. Additionally, the blast-induced fractures inside rock sample and  
117 damage characteristics with various decoupling coefficients were experimentally investigated  
118 by Zuo et al. (2022) via X-ray computed tomography (CT, the spatial resolution of industrial  
119 CT scanning system is 0.5 mm × 0.35 mm × 1 mm) and three-dimensional (3D) rock fracture  
120 reconstruction. The experimental results were analyzed from a microscopic perspective that  
121 with a small decoupling ratio, the blast-induced crack surface was dominated by intracrystalline  
122 fractures while with a smaller charge diameter, the crack surface exhibited transgranular and  
123 intergranular coupled fracture modes, accompanying by decreasing rock damage. The above-  
124 mentioned studies have partly revealed the mechanisms of the pressure variation and fracture  
125 evolution in rock under decoupled charge blasting. However, the effect of decoupled charge

126 including decoupling ratio, coupling medium and decoupled charge mode on the blast-induced  
127 fragment size distribution (FSD) is still unclear.

128       Recently, the blast-induced rock fragmentation with different decoupling ratios and  
129 coupling mediums was experimentally investigated by Chi et al. (2022), and the results showed  
130 that blasting with a smaller decoupling ratio and the water-decoupled charge generates smaller  
131 fragments, while blasting with a larger decoupling ratio and the air-decoupled charge produces  
132 bigger fragments. Based on the laboratory tests conducted by Chi et al. (2022), in this study,  
133 rock fragmentation under decoupling charge blasting is studied using combined finite element  
134 modeling in LS-DYNA (LSTC, 2015) and image-processing using ImageJ (Durda et al., 2015).  
135 After reasonably determining the parameters for rock, explosive and coupling materials, the  
136 developed numerical model is carefully calibrated against the fragment morphology and FSD  
137 of three air-coupling blasts and three water-coupling blasts. Then, based on the verified  
138 numerical model, a series of cubic single-hole rock blasting models are built to simulate blast-  
139 induced rock fracturing with various decoupling ratios, distinct coupling mediums and different  
140 decoupled charge modes. The resulting crack patterns are image-processed to provide  
141 quantitative insights into the effects of decoupled charges on blast-induced rock fragmentation.  
142 Next, the FSDs obtained by the combined finite element modeling and image-processing are  
143 characterized by a three-parameter generalized extreme value function, and the FSDs in  
144 decoupled charge blasting with different charge modes, decoupling ratios and coupling  
145 mediums are quantitatively analyzed and compared. This study tries to provide novel insights  
146 into the formation and variation of rock fragmentation in decoupled charge blasting and  
147 supplies some guidance to improve the performances of rock excavation and rock  
148 fragmentation in controlled and production blasting.

## 149 **2. Numerical model and numerical calibration**

150 In the current simulation, finite element modelling with LS-DYNA code is adopted to  
151 simulate the rock fragmentation induced by decoupled charge blasting because a variety of  
152 constitutive models in LS-DYNA library can properly predict the pressure generated by  
153 explosive detonation and the dynamic damage behavior of rock which is extremely important  
154 for modelling rock blasting. To ensure the accuracy of numerical modelling, numerical  
155 verification is first performed against the results from laboratory-scale tests of three air-  
156 coupling blasts and three water-coupling blasts.

### 157 **2.1. Blasting tests**

158 In blasting tests, 240-mm-diameter and 300-mm-high cylindrical granite samples were  
159 used to investigate the rock fragmentation induced by decoupled charge blasting. The density  
160 of rock is  $2610 \text{ kg/m}^3$ ; Poisson's ratio is 0.23, Young's modulus is 43.5 GPa, the average P-  
161 wave velocity is 4400 m/s and the static uniaxial compressive strength is 86 MPa (Chi et al.,  
162 2022). In each sample, a central borehole with a diameter  $D$  of 10 mm, 14 mm or 20 mm was  
163 axially drilled with a length of 200 mm from the specimen top, and the PENT explosive with  
164 a diameter of about 6 mm and a height of about 120 mm was centrally placed at the bottom of  
165 borehole. Hence, the decoupling ratios in blasting tests are  $5/3$ ,  $7/3$  and  $10/3$ . Two plastic rings  
166 that have an external diameter equal to the blasthole diameter were used as the lining to fix the  
167 explosive column in hole centre, as depicted in Fig. 1. The density of PETN is approximately  
168  $900 \text{ kg/m}^3$ . The gap between PETN and hole-wall was filled with air or water, and the borehole  
169 was stemmed with fast-curing cement grout. In blasting, the explosive is ignited at the top of  
170 the charge column. After conducting the tests, the fragmentation size distributions induced by  
171 decoupled charge blasting were obtained by collecting, weighing and sieving the rock  
172 fragments.

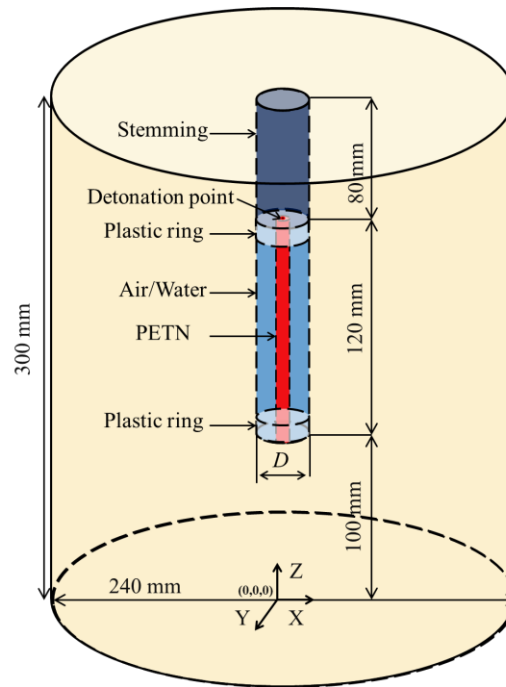


Fig. 1. Sketch of sample in blasting tests

173  
174

## 175 2.2. Numerical model

176 3D finite element model with the same configuration and size as the test specimen is built,  
 177 as shown in Fig. 2. The plastic rings that fix the PETN are constructed as air or water due to  
 178 their low density and strength. The elements at the interfaces between the explosive, air/water,  
 179 stemming and rock share common nodes, and the *Arbitrary-Lagrange-Euler (ALE)* algorithm  
 180 is applied for explosive and air/water to solve the problems of large deformation in rock  
 181 blasting while the *Lagrangian* formulation is adopted for stemming and rock. Moreover, the  
 182 *multi-material ALE* algorithm is employed to control the material mix between explosive and  
 183 air/water. With these algorithms, the ALE fluids are coupled with the Lagrangian structure, and  
 184 the robustness of ALE mesh motion and the accuracy of Lagrangian mesh motion within the  
 185 same framework can avoid problems such as negative volume typically encountered in blasting  
 186 modelling. In addition, the simulated explosion pressure at the target point (60, 0, 150/mm) is  
 187 recorded to investigate the pressure variation in the rock under decoupled charge blasting.



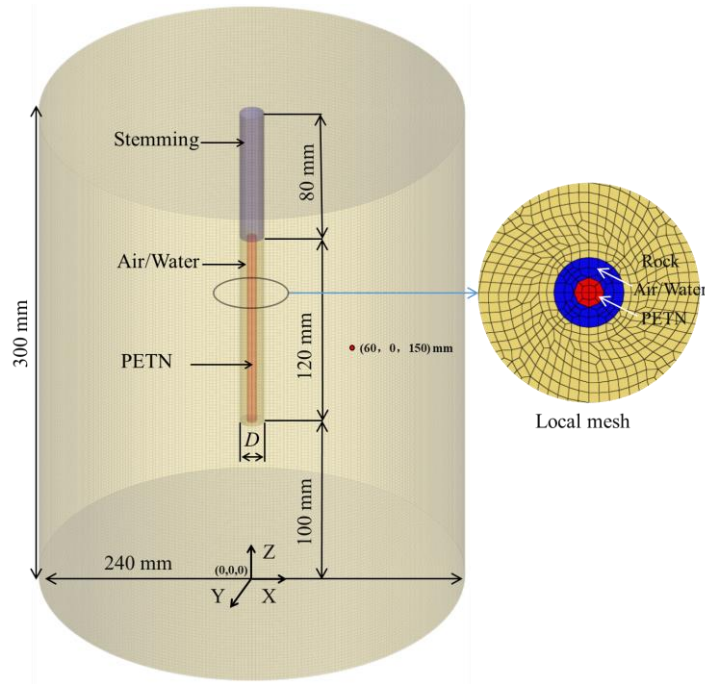


Fig. 2. Finite element model for blasting tests

### 2.2.1. Material model for rock

Granite is a typical anisotropic material because it consists of a variety of mineral particles and includes pre-existent microcracks, which are not possible to be constructed and simulated numerically because of the limitation of element size in finite element modelling. Hence, in the current numerical modelling, granite is assumed to be an isotropic material, and more symmetrical crack pattern and pressure pattern in granite may be induced due to this assumption of isotropy. There are several constitutive models such as Johnson\_Holmquist\_II (JH-2) model (Baranowski et al., 2020; Gharehdash et al., 2020; Pu et al., 2021; Wang et al., 2018), Holmquist\_Johnson\_Cook (HJC) model (Luo et al., 2021; Wang et al., 2021b) and Riedel\_Hiermaier\_Thoma (RHT) model (Hashemi and Katsabanis, 2021; Huo et al., 2020; Jang et al., 2018; Katsabanis, 2020; Leng et al., 2021; Liu et al., 2018a; Saadatmand Hashemi and Katsabanis, 2020; Zhang et al., 2022) extensively employed to simulate the blast-induced rock response. In the current modelling, the RHT model whose strength criteria are represented in terms of three stress limit surfaces, i.e., the initial elastic yield surface, the failure surface and the residual friction surface is chosen to model rock behavior under decoupled charge

205 blasting because of its advantages of considering the effects of confining pressure, high strain  
 206 rate, strain hardening and damage softening at the same time (Borrvall and Riedel, 2011). With  
 207 the use of this model, the behaviors of rock under dynamic loading such as crack initiation,  
 208 crack propagation and crack branching can be reasonably predicted. During the blasting  
 209 modelling, the loading scenario for rock element is that the material is elastic before its stress  
 210 hits the initial elastic yield surface and beyond this surface, it is in a linear strengthening phase  
 211 in which the rock element deforms plastically before the stress hits the failure surface. When  
 212 the hardening state reaches the ultimate strength on the failure surface, a parameterized damage  
 213 model governs the evolution of damage, and the material gradually shifts into the damage-  
 214 softening phase accompanied by plastic strain accumulation. At last, the material is fully  
 215 damaged with low residual strength when the stress reaches the residual friction surface.  
 216 Meanwhile, the pressure in the RHT model is expressed using the Mie–Greisen form with a  
 217 polynomial Hugoniot curve and a  $p$ - $\alpha$  compaction relationship.

218 In the RHT model, 38 parameters need to be input to LS-DYNA. The basic physical and  
 219 mechanical parameters such as Density  $\rho$  (2610 kg/m<sup>3</sup>) and static uniaxial compressive strength  
 220  $f_c$  (86 MPa) are obtained from laboratory experiments (Chi et al., 2022). The shear modulus  $G$   
 221 is calculated by  $G = E/(2 \times (1 + \gamma))$  in which  $E$  is Young's modulus,  $\gamma$  is Poisson's ratio, and  $G$   
 222 = 17.68 GPa. The uniaxial tensile strength  $f_t$  is empirically determined by  $f_t = f_c/10 = 8.6$  MPa  
 223 (Li, 2014). Then, part of the parameters for rock is obtained based on a series of theoretical  
 224 calculations as follows: the strain rate dependence in the RHT model is described as (Borrvall  
 225 and Riedel, 2011):

$$226 \quad F_r(\dot{\varepsilon}_p) = \begin{cases} (\dot{\varepsilon}_p / \dot{\varepsilon}_0^t)^{\beta_t} & (P \leq -f_t / 3) \\ \frac{P + f_t / 3}{f_c / 3 + f_t / 3} (\dot{\varepsilon}_p / \dot{\varepsilon}_0^c)^{\beta_c} - \frac{P - f_c / 3}{f_c / 3 + f_t / 3} (\dot{\varepsilon}_p / \dot{\varepsilon}_0^c)^{\beta_t} & (-f_t / 3 < P < f_t / 3) \\ (\dot{\varepsilon}_p / \dot{\varepsilon}_0^c)^{\beta_c} & (P \geq f_c / 3) \end{cases} \quad (1)$$

227 where  $F_r(\dot{\varepsilon}_p)$  is the strain strength factor,  $\dot{\varepsilon}_p$  is the strain rate,  $P$  is the pressure, in which  $P =$   
 228  $(\sigma_1 + \sigma_2 + \sigma_3)/3$ .  $\dot{\varepsilon}_0^c$  and  $\dot{\varepsilon}_0^t$  are the reference strain rate under compression and tension,  
 229 respectively, and  $\dot{\varepsilon}_0^c = 3.0 \times 10^{-8} \text{ s}^{-1}$ ,  $\dot{\varepsilon}_0^t = 3.0 \times 10^{-9} \text{ s}^{-1}$  (LSTC, 2015).  $\beta_c$  and  $\beta_t$  are the material  
 230 constants for compression and tension, respectively, which are given as (Borrvall and Riedel,  
 231 2011):

$$\beta_c = 4 / (20 + 3f_c), \beta_t = 2 / (20 + f_c) \quad (2)$$

233 So,  $\beta_c$  and  $\beta_t$  can be calculated as 0.014 and 0.019, respectively.

234 For a given stress state and rate of loading, the elastic-plastic yield surface in the RHT  
 235 model is given by (Borrvall and Riedel, 2011):

$$\sigma_y(P^*, \dot{\varepsilon}_p, \varepsilon_p^*) = f_c \sigma_y^*(P^*, F_r(\dot{\varepsilon}_p), \varepsilon_p^*) R_3(\theta, P^*) \quad (3)$$

237 where  $\sigma_y^*$  is the normalized yield function,  $R_3$  denotes the Willam-Warnke function,  $\theta$  is the  
 238 lode angle,  $P^*$  is the normalized pressure and  $P^* = P/f_c$ . Moreover, the failure surface is  
 239 expressed as (Borrvall and Riedel, 2011):

$$\sigma_f^*(P^*, F_r) = \begin{cases} A(P^* - F_r/3 + (A/F_r)^{-1/N})^N & (3P^* \geq F_r) \\ F_r f_s^* / Q_1 + 3P^*(1 - f_s^* / Q_1) & (F_r \geq 3P^* \geq 0) \end{cases} \quad (4)$$

241 where  $Q_1 = R_3(\pi/6, 0)$ ,  $\sigma_f^*(F_r)$  is the normalized strength with  $\sigma_f^* = \sigma_f / f_c$ , in which  $\sigma_f = (0.5((\sigma_1$   
 242  $-\sigma_2)^2 + (\sigma_2 - \sigma_3)^2 + (\sigma_1 - \sigma_3)^2))^{0.5} \cdot f_s^*$  and  $f_t^*$  are parameters of relative shear strength and relative  
 243 tensile strength, respectively.  $f_t^* = f_t / f_c = 0.10$  and  $f_s^* = \tau / f_c$  in which  $\tau = A' f_c ((\sigma_n - f_t) / f_c)^{B'}$ .  
 244 Pan et al. (2022) gave the values for intact granite, and  $A' = 1.32$  and  $B' = 0.57$ . Thus  $f_s^* = 0.32$ .  
 245  $A$  and  $N$  are parameters of the failure surface. When rock is under a quasi-static state, i.e.  $\dot{\varepsilon}_p =$   
 246  $3.0 \times 10^{-8} \text{ s}^{-1}$  and  $F_r = 1$ ,  $A$  and  $N$  can be calculated through taking the triaxial compressive  
 247 strengths of rock under various confining pressures obtained by the Hoek-Brown criterion into  
 248 Eq. (4). For intact granite in the current study, the Hoek-Brown criterion can be written as:

249 
$$\sigma_1 = \sigma_3 + f_c \left( 24 \frac{\sigma_3}{f_c} + 1 \right)^{1/2} \quad (5)$$

250 where  $\sigma_1$  and  $\sigma_3$  are the maximum and minimum effective stresses at failure. Next, the  
 251 mechanical parameters of rock under various confining pressures can be calculated and are  
 252 listed in Table 1. Taking the values of  $P^*$  and  $\sigma_f^*$  under confining stresses of 10 and 100 MPa  
 253 into Eq. (4),  $A = 2.50$  and  $N = 0.72$  are obtained.

254 **Table 1**  
 255 Mechanical parameters of rock under various lateral pressures

$\sigma_2 = \sigma_3/\text{MPa}$	$\sigma_1/\text{MPa}$	$P/\text{MPa}$	$\sigma_f/\text{MPa}$	$P^*$	$\sigma_f^*$
0.00	-8.60	-2.86	8.60	-0.033	0.10
0.00	86.00	28.67	86.00	0.33	1.00
10.00	177.44	65.81	167.44	0.77	1.95
50.00	382.56	160.85	332.56	1.87	3.87
100.00	562.38	254.13	462.38	2.95	5.38
200.00	848.23	416.08	648.23	4.84	7.54

256 Driven by blast loading, the maximum reduction in strength of RHT model is given as a  
 257 function of relative pressure (Borrvall and Riedel, 2011):

258 
$$Q(P^*) = Q_0 + BP^* \quad (6)$$

259 where  $Q_0$  is the ratio between the radii of the tensile and compressive meridians,  $B$  is the lode  
 260 angle dependence factor.  $Q_0 = 0.68$  and  $B = 0.05$  are determined based on the curve regression  
 261 results reported by Yu (1998). Furthermore, the damage value  $D$  in the RHT model is calculated  
 262 according to (LSTC, 2015):

263 
$$D = \sum(\Delta\varepsilon_p/\varepsilon_f) \quad (7)$$

264 where  $\Delta\varepsilon_p$  is the accumulated plastic strain,  $\varepsilon_f$  is the failure strain expressed as (LSTC, 2015):

265 
$$\varepsilon_f = D_1 - (P^* - (1 - D) P_t^*)^{D_2} \quad (8)$$

266 where  $P_t^*$  is the failure cut-off pressure,  $D_1$  and  $D_2$  are damage constants, and  $D_1 = 0.04$  and  $D_2$   
 267  $= 1.00$  are determined from Reference (Brannon and Leelavanichkul, 2009). After running the  
 268 simulation,  $D = 0$  represents the rock element undamaged whereas  $D = 1$  means that rock  
 269 element is fully damaged.

270 Besides, the equation of state (EOS) of the RHT model is described as (Borrvall and  
 271 Riedel, 2011):

$$272 \quad P_{EOS} = \frac{1}{\alpha} ((B_0 + B_1\mu)\alpha_0\rho_0e + A_1\mu + A_2\mu^2 + A_3\mu^3) \quad \mu > 0 \quad (9)$$

273 where  $\rho_0$  is the initial density of rock,  $e$  is the internal energy per unit mass,  $\mu$  is the volumetric  
 274 strain,  $B_0$  and  $B_1$  are constants for polynomial EOS, and  $B_0 = B_1 \approx 2s - 1$  in which  $s$  is the  
 275 material constant.  $\alpha$  and  $\alpha_0$  are the current and initial porosity, respectively.  $B_0 = B_1 = 1.22$ ,  $\alpha_0$   
 276  $= 1.00$  are set according to Reference (Xie et al., 2017).  $A_1$ ,  $A_2$  and  $A_3$  are the Hugoniot  
 277 polynomial coefficients which can be calculated by the derived formulation of Xie et al. (2017)  
 278 as follows:

$$279 \quad A_1 = \alpha_0\rho_0c^2 \quad (10a)$$

$$280 \quad A_2 = \alpha_0\rho_0c^2(2s - 1) \quad (10b)$$

$$281 \quad A_3 = \alpha_0\rho_0c^2[(3s - 1)(s - 1)] \quad (10c)$$

282 where  $c$  is the P-wave velocity in rock. So,  $A_1 = 50.8$  GPa,  $A_2 = 61.98$  GPa and  $A_3 = 13.02$  GPa  
 283 can be obtained. Besides, the elastic limit pressure, i.e. the pore crush pressure, is taken as 2/3  
 284 of the uniaxial compressive strength according to Riedel et al. (2009), which is 57.33 MPa.  
 285 The remaining parameters are set as defaults (Borrvall and Riedel, 2011), and the parameters  
 286 used in RHT model for rock are listed in Table 2. In addition, the fast-curing cement grout for  
 287 stemming is also modelled using the RHT model and the default parameters are used. More  
 288 details about the RHT model can be found in References (Borrvall and Riedel, 2011; LSTC,  
 289 2015; Xie et al., 2017).

290 **Table 2**  
 291 **Parameters for rock**

Parameter	Type	Value	Parameter	Type	Value
Mass density $\rho$ (kg/m <sup>3</sup> )	<i>E</i>	2610	Compressive strain rate dependence exponent $\beta_c$	<i>E</i>	0.014
Elastic shear modulus $G$ (GPa)	<i>E</i>	17.68	Tensile strain rate dependence exponent $\beta_t$	<i>E</i>	0.019
Eroding plastic strain $EPSF$	<i>L</i>	2.0	Volumetric plastic strain fraction in tension $PTF$	<i>L</i>	0.001
Parameter for polynomial EOS $B_0$	<i>L</i>	1.22	Compressive yield surface parameter	<i>L</i>	0.53

			<i>GC*</i>		
Parameter for polynomial EOS $B_1$	<i>L</i>	1.22	Tensile yield surface parameter $GT^*$	<i>L</i>	0.70
Parameter for polynomial EOS $T_1$ (GPa)	<i>E</i>	50.80	Shear modulus reduction factor $XI$	<i>L</i>	0.50
Parameter for polynomial EOS $T_2$ (GPa)	<i>L</i>	0.0	Damage parameter $D_1$	<i>L</i>	0.04
Failure surface parameter $A$	<i>E</i>	2.50	Damage parameter $D_2$	<i>L</i>	1.0
Failure surface parameter $N$	<i>E</i>	0.72	Minimum damaged residual strain $EPM$	<i>L</i>	0.01
Compressive strength $f_c$ (MPa)	<i>E</i>	86	Residual surface parameter $AF$	<i>L</i>	1.60
Crush pressure $PEL$ (MPa)	<i>E</i>	57.33	Residual surface parameter $NF$	<i>L</i>	0.61
Relative shear strength $f_s^*$	<i>E</i>	0.32	Gruneisen gamma $GAMMA$	<i>L</i>	0.0
Relative tensile strength $f_t^*$	<i>E</i>	0.10	Hugoniot polynomial coefficient $A_1$ (GPa)	<i>E</i>	50.80
Lode angle dependence factor $Q_0$	<i>L</i>	0.68	Hugoniot polynomial coefficient $A_2$ (GPa)	<i>E</i>	61.98
Lode angle dependence factor $B$	<i>L</i>	0.05	Hugoniot polynomial coefficient $A_3$ (GPa)	<i>E</i>	13.02
Reference compressive strain rate $EOC$ ( $S^{-1}$ )	<i>L</i>	$3.0E^{-8}$	Compaction pressure $PCO$ (GPa)	<i>L</i>	6.0
Reference tensile strain rate $ETC$ ( $s^{-1}$ )	<i>L</i>	$3.0E^{-9}$	Porosity exponent $NP$	<i>L</i>	3.0
Break compressive strain rate $EC$ ( $s^{-1}$ )	<i>L</i>	$3.0E^{+22}$	Initial porosity $\omega_0$	<i>L</i>	1.00
Break tensile strain rate $ET$ ( $s^{-1}$ )	<i>L</i>	$3.0E^{+22}$			

292 Type “E” denotes parameters obtained based on experiment; Type “L” denotes parameters determined based on  
293 literature

### 294 2.2.2. Jones-Wilkins-Lee EOS for PETN

295 The combination of the material type of Mat\_High\_Explosive\_Burn and the EOS of  
296 Jones-Wilkins-Lee (JWL) is widely used in LS-DYNA to simulate the pressure generated by  
297 the expansion of detonation products (Liu et al., 2018b, 2019; Wei et al., 2009). The JWL EOS  
298 precisely defines the detonation pressure  $P$  as (Lee et al., 1968):

$$299 \quad P = A \left( 1 - \frac{\omega}{R_1 V} \right) e^{-R_1 V} + B \left( 1 - \frac{\omega}{R_2 V} \right) e^{-R_2 V} + \frac{\omega E}{V} \quad (11)$$

300 where  $V$  is the volume relative to the undetonated state,  $E$  is the detonation energy per unit  
301 "initial" volume with an initial value of  $E_0$ , and  $A$ ,  $B$ ,  $R_1$ ,  $R_2$  and  $\omega$  are explosive constants. The  
302 detonation velocity ( $VOD$ ) and Chapman-Jouguet pressure ( $PCJ$ ) of PETN are calculated using  
303 the regression equations based on the published data on detonation pressure measurements on  
304 PETN (Green and Lee, 2006), and  $VOD = (\rho_0 + 0.499)/0.272$  and  $PCJ = 18.05 \rho_0^2 + 17.39 \rho_0$   
305  $+ 7.45$  ( $\rho_0$  in  $g/cm^3$ ,  $VOD$  in km/s and  $PCJ$  in GPa). The remaining parameters for explosive are  
306 determined with the regression equations reported by Banadaki based on JWL data for PETN  
307 at different densities (Banadaki, 2010), and the parameters for PETN are listed in Table 3.

308 **Table 3**

309 Parameters for explosive

$\rho_0$ (kg/m <sup>3</sup> )	VOD (km/s)	$E_0$ (GPa)	$P_{CJ}$	$A$ (GPa)	$B$ (GPa)	$R_1$	$R_2$	$\omega$
900	5.144	5.00	6.42	441.4	11.60	6.96	1.99	0.24

310 2.2.3. Linear\_Polynomial EOS for air

311 The material type of Mat\_Null together with a specific Linear\_Polynomial EOS is  
 312 extensively employed to model air in LS-DYNA, and this EOS describes the pressure  $P$  in the  
 313 air as (LSTC, 2015):

$$314 \quad P = C_0 + C_1\mu + C_2\mu_2 + C_3\mu_3 + (C_4 + C_5 + C_6\mu_2)E \quad (12)$$

315 where  $E$  is the internal energy per volume,  $\mu$  defines the compression of air by  $\mu=(\rho/\rho_0)-1$  with  
 316  $\rho$  and  $\rho_0$  being the current and initial density of air, respectively.  $C_0, C_1, C_2, C_3, C_4, C_5$  and  $C_6$   
 317 are material constants of air, and  $C_4$  and  $C_5$  can be calculated by  $C_4 = C_5 = \gamma - 1$  with  $\gamma$  being  
 318 the ratio of specific heats. The parameters for air are well documented with previous  
 319 experimental calibrations and are listed in Table 4.

320 **Table 4**  
 321 Parameters for air

$\rho_0$ (kg/m <sup>3</sup> )	$E_0$ (J/m <sup>3</sup> )	$\gamma$	$C_0$	$C_1$	$C_2$	$C_3$	$C_4$	$C_5$	$C_6$
1.29	$2.5 \times 10^5$	1.4	0	0	0	0	0.4	0.4	0

322 2.2.4. Gruneisen EOS for water

323 The water is modeled by the material type of Mat\_Null combined with the Gruneisen EOS,  
 324 and this EOS defines pressure  $P$  for compressed water as (LSTC, 2015):

$$325 \quad P = \frac{\rho_0 C^2 \mu \left[ 1 + \left( 1 - \frac{\gamma_0}{2} \right) \mu - \frac{\alpha}{2} \mu^2 \right]}{\left[ 1 - (S_1 - 1) \mu - S_2 \frac{\mu^2}{\mu + 1} - S_3 \frac{\mu^3}{(\mu + 1)^2} \right]^2} + (\gamma_0 + \alpha \mu) E \quad (13)$$

326 where  $\gamma_0$  is the Gruneisen gamma,  $\alpha$  is the first order volume correction to  $\gamma_0$ ,  $\mu$  is defined as  
 327  $\rho/\rho_0-1$  with  $\rho$  and  $\rho_0$  being the current and initial density of water, respectively.  $C$  is the intercept  
 328 of  $v_s-v_p$  curve,  $E$  is the internal energy per unit "initial" volume with an initial value of  $E_0$ , and  
 329  $S_1, S_2$  and  $S_3$  are the coefficients of the slope of the  $v_s-v_p$  curve. This combination in LS-DYNA  
 330 is widely used for simulating water-filled blasting and underwater explosion (Zhang et al., 2012;

331 Zhang et al., 2014), and the parameters of water are also well documented with previous  
 332 experimental verifications. Thus, the calibrated parameters in previous study for water are  
 333 employed in the current simulation and no parametric study on the compressibility of water for  
 334 the water-coupling blasts is conducted. This may lead to a little difference in stress transfer  
 335 from explosive transmitting water to rock between simulation and real blasting. However,  
 336 compared to the extremely high pressure in blasting, this tiny difference can be neglected. The  
 337 parameters for water are listed in Table 5.

338 **Table 5**  
 339 Parameters for water

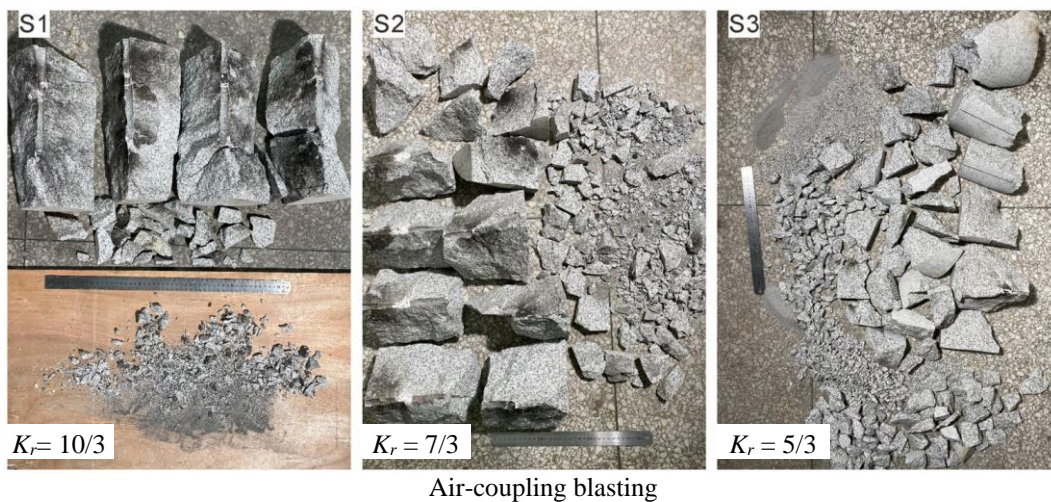
$\rho_0$ (kg/m <sup>3</sup> )	$C$ (m/s)	$E_0$ (J/m <sup>3</sup> )	$S_1$	$S_2$	$S_3$	$\gamma_0$	$\alpha$	$V_0$
1000	1480	$1.89 \times 10^6$	2.56	-1.986	1.2268	0.35	0	1.0

### 340 2.3. Numerical calibration

341 The results of rock fragmentation in tests of decoupled charge blasting are presented in  
 342 Fig. 3. As can be seen, after running the physical tests, the sample S1 (air-coupling, hole  
 343 diameter of 20 mm,  $K_r = 3.33$ ) was mainly fragmented into several large blocks, and each of  
 344 large fragment is almost a quarter cylinder; sample S2 (air-coupling, hole diameter of 14 mm,  
 345  $K_r = 2.33$ ) was primarily disintegrated into eight fragments being almost half of a quarter  
 346 cylinder and several smaller fragments; sample S3 (air-coupling, hole diameter of 10 mm,  $K_r$   
 347 = 1.67) was broken into many small fragments. The samples S4, S5 and S6 have borehole  
 348 diameters of 20 mm, 14 mm and 10 mm and decoupling ratios  $K_r$  of 3.33, 2.33 and 1.67 in the  
 349 sequence and were water-filled. Similar to air-coupling blasting, the fragment sizes of samples  
 350 S4–S6 show a decreasing tendency with the decrease of hole diameter, without fragments larger  
 351 than 180 mm. In comparison, the variation in rock fragmentation under water-coupling blasting  
 352 of samples S4-S6 is not obvious as that under air-coupling blasting of samples S1-S3.

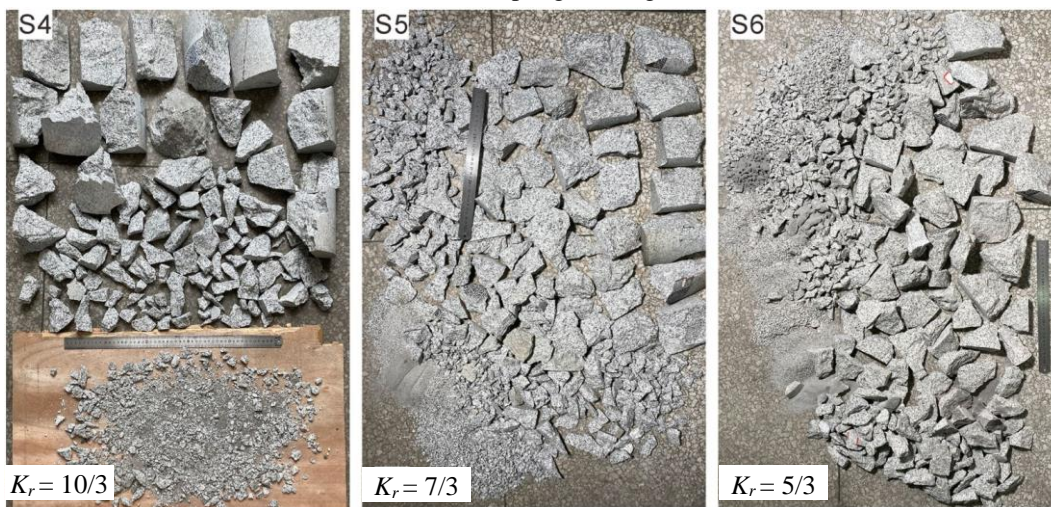


353



Air-coupling blasting

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Water-coupling blasting

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Fig. 3 rock fragmentation after blast testing

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These results of rock breakage in specimens of S1-S3 under air-coupling blasting and specimens of S4-S6 under water-coupling blasting are simulated using the developed numerical model with the above-introduced material models and EOSs in LS-DYNA. Before the modelling of the blasting tests, mesh size convergence test is conducted with different element sizes, and the simulation results of air-coupling blasting for Sample S2 are presented as examples in Fig. 4. The numerical results in the mesh size convergence test show that the damage patterns are almost the same while smaller mesh size gives more small cracks and takes much longer computational time. In the mesh size convergence test, the explicit time integration scheme with one-point quadrature, which is a typical integration scheme of hexahedral element in LS-DYNA for saving computing memory and reducing computational

366 time, is invoked and the time step  $\Delta t$  is shorter than the time that blast stress wave propagates  
367 crossing the minimum side length of any element  $l_{\min}$ , i.e.

368 
$$\Delta t < l_{\min}/C \tag{14}$$

369 where  $C$  is the propagation velocity of the explosion-induced stress wave. Besides, the value  
370 of minimum  $\Delta t$  /average  $\Delta t$  is larger than 0.95 when the mesh size is larger than 2 mm×2 mm  
371 ×2 mm, indicating that the numerical model developed in the current study runs stably and is  
372 reasonable. Finally, to balance the simulation reliability and computational time, the mesh size  
373 of 2 mm×2 mm ×2 mm is adopted, and this model is discretized with 1 744 200 hexahedral  
374 elements.

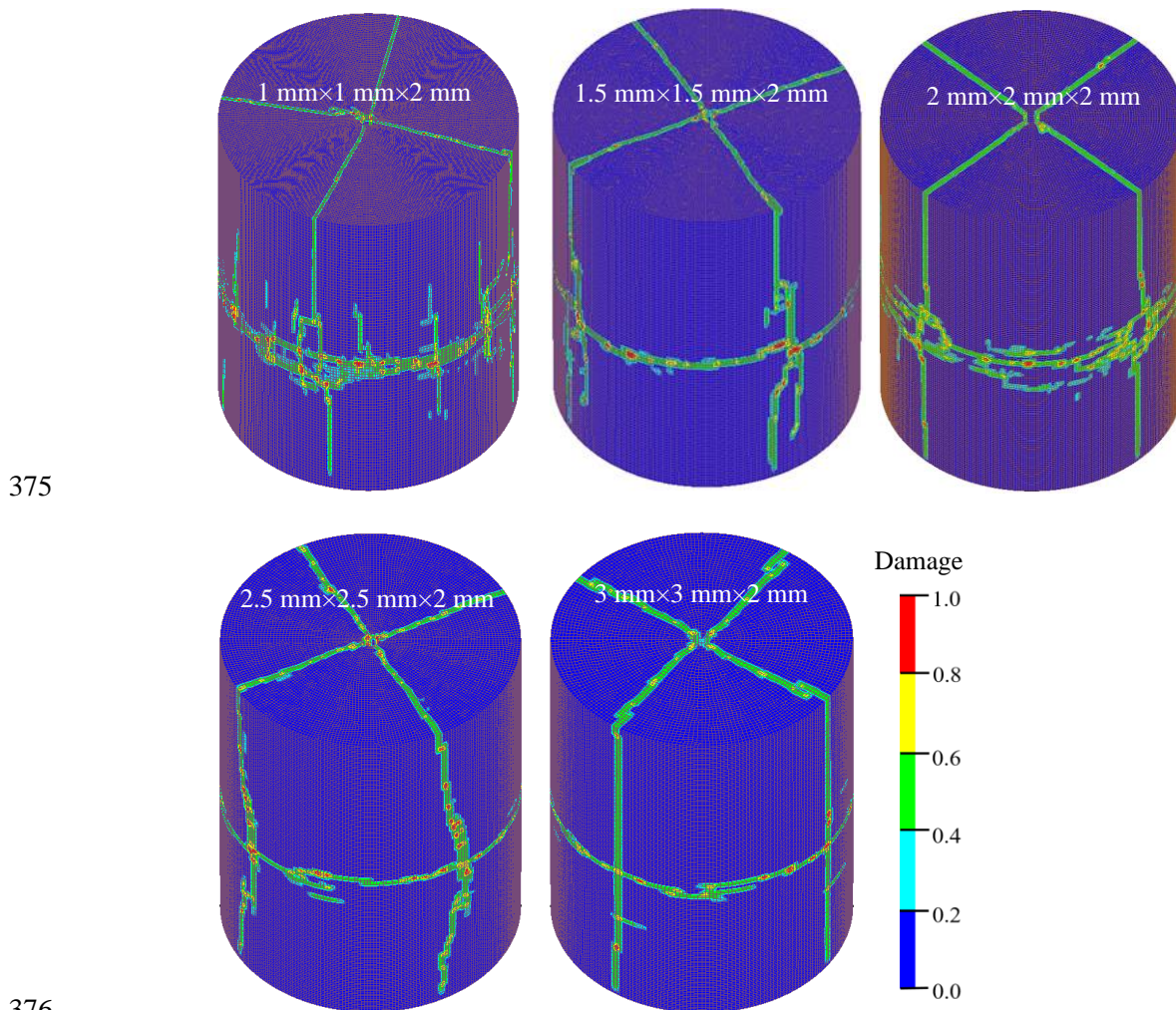
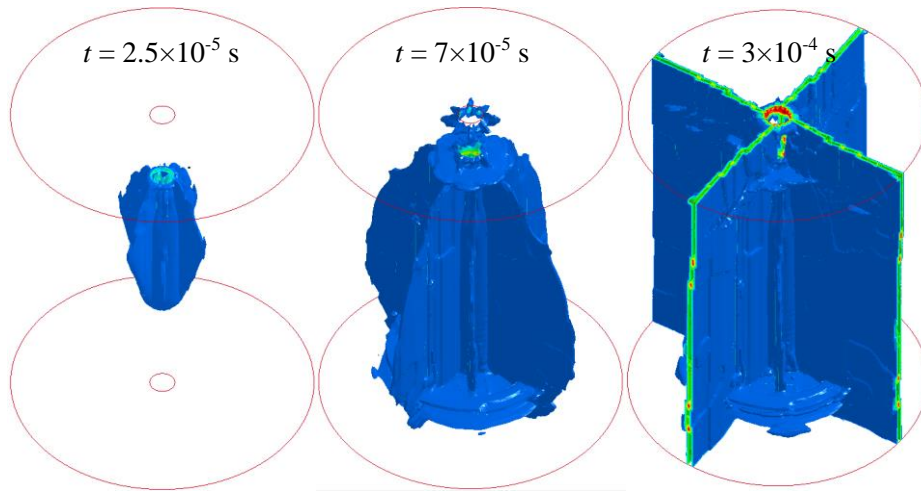


Fig. 4 Damage patterns under air-coupling blasting (S2) with various mesh sizes

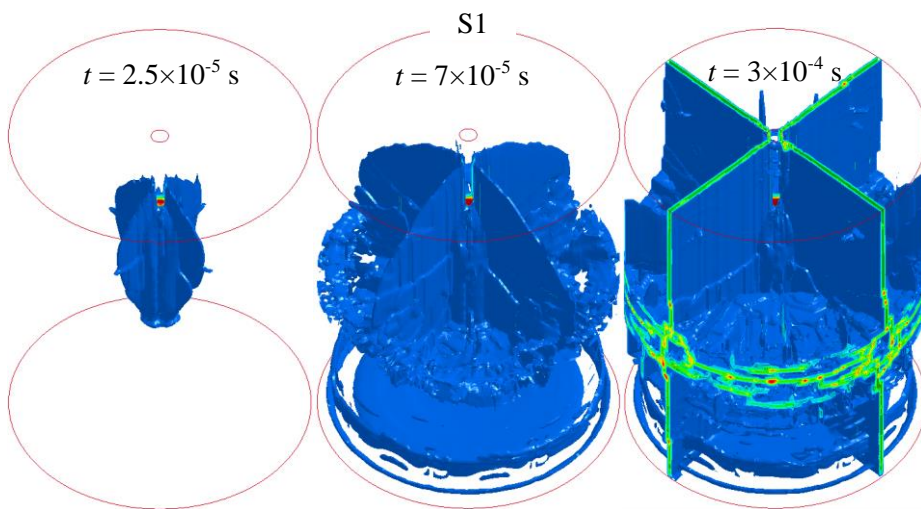


378 Using the mesh size of 2 mm×2 mm×2 mm, three air-coupling blasts and three water-  
379 coupling blasts are simulated, and the corresponding damage evolution processes and time-  
380 history curves of explosion-induced pressure at target point are presented in Figs. 5(a) and 5(b),  
381 respectively. In the current numerical modelling, the overall crack pattern is homogeneous in  
382 the radial direction of the model, but some heterogeneous small cracks are generated due to the  
383 use of RHT model. With the using of this model, the behaviours of rock under dynamic loading  
384 such as crack initiation, crack propagation and crack branching can be reasonably predicted so  
385 that the phenomenon of heterogeneous rock fracturing which is generally observed in actual  
386 blast is also modelled.

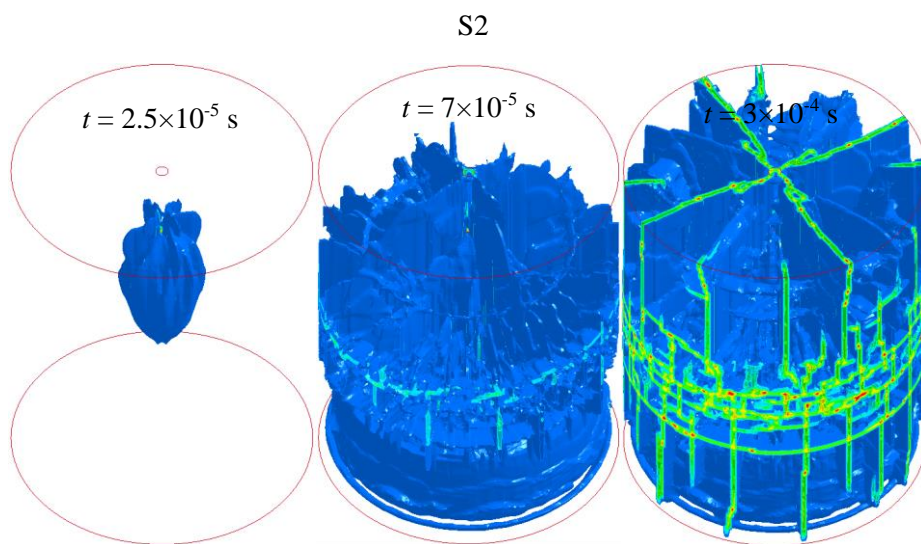
387 After detonation, a damage zone near the detonation point is immediately created due to  
388 high detonation pressure created by the burning of explosive column ( $t = 2.5 \times 10^{-5}$  s). Then, the  
389 blast-induced cracks extend downward and outward. At this stage, the rock sample is gradually  
390 fragmented with the development of radial cracks and tensile damage in the vicinity of sample  
391 surface, which is mainly induced by the tensile component and the reflection of explosion-  
392 induced stress waves ( $2.5 \times 10^{-5}$  s  $\leq t \leq 7 \times 10^{-5}$  s). After that, the blast-created fractures propagate  
393 upward until reaching the top surface of sample, which is also resulted by the tensile stress and  
394 reflected stress waves. As can be seen in Fig. 5(a), with the same charge diameter, more  
395 extensive cracks are formed under blasting with smaller borehole size, while more blast-induced  
396 fractures are generated after the detonation of decoupled charged borehole using water-  
397 coupling. This is because a narrower gap between charge and borehole wall and water-coupling  
398 produces a higher explosion pressure in rock, as can be observed in Fig. 5(b). In the current  
399 numerical modelling, the calculation is terminated when no new crack forms and crack  
400 extension arrests, and the computational duration is  $3 \times 10^{-4}$  ms.



401



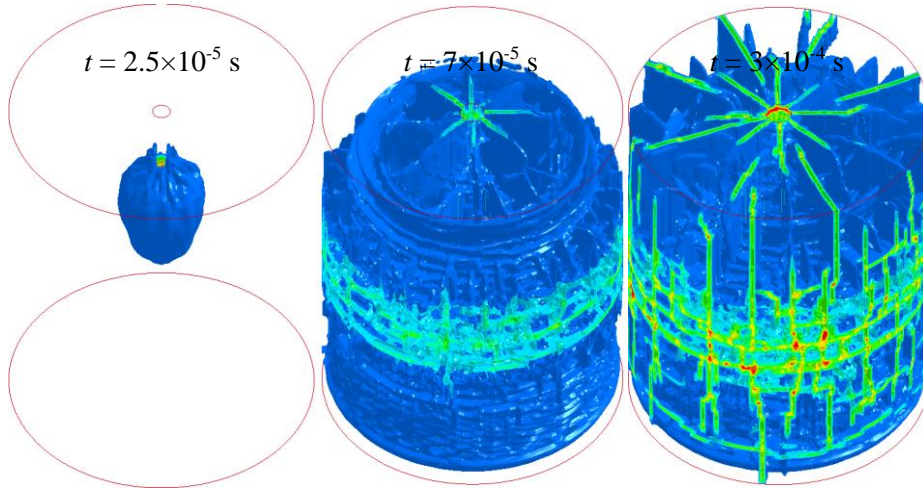
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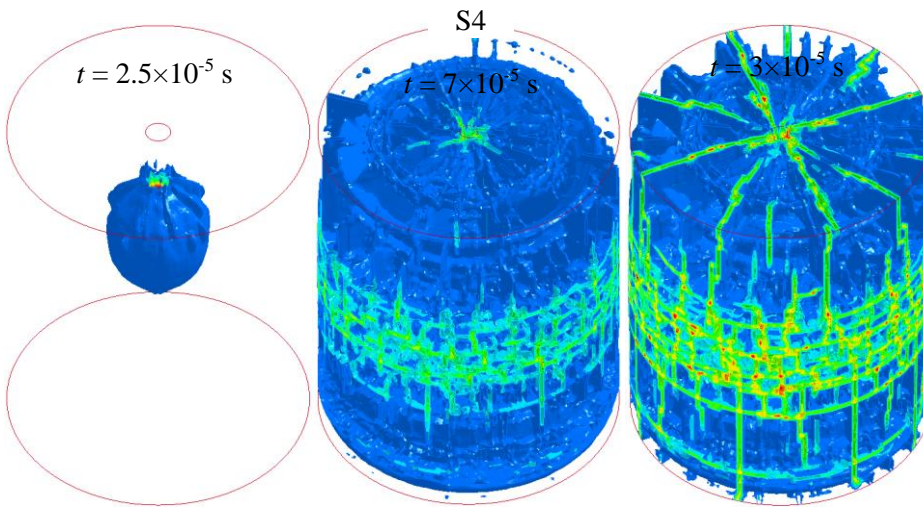
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S3

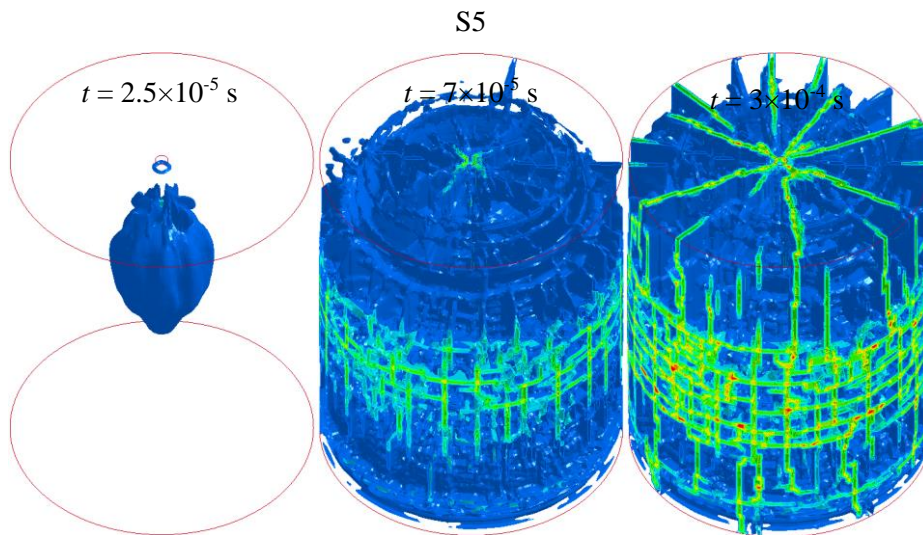
(a)



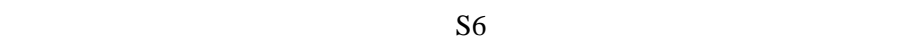
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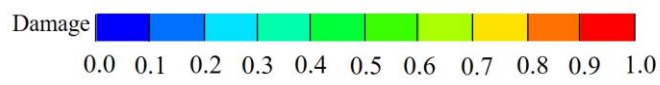
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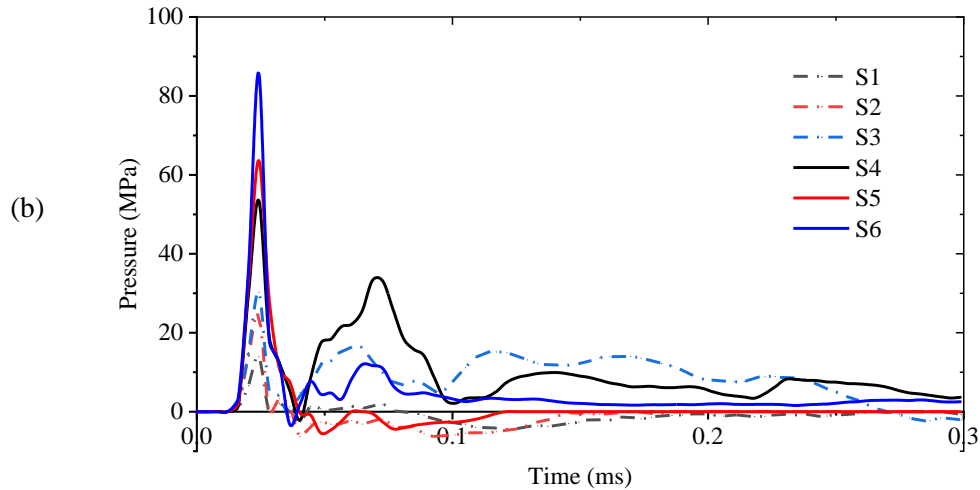


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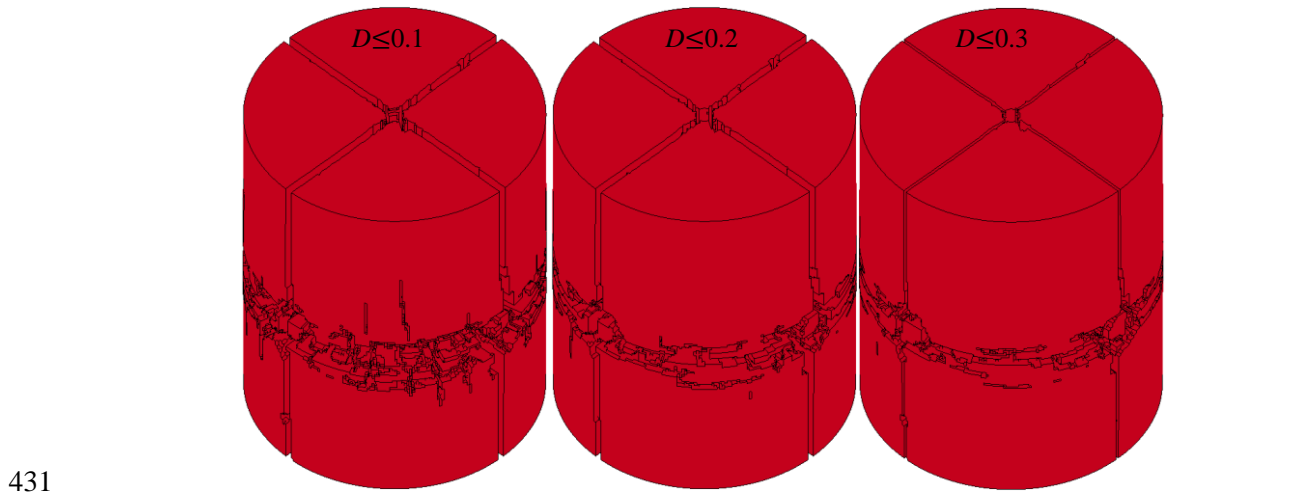
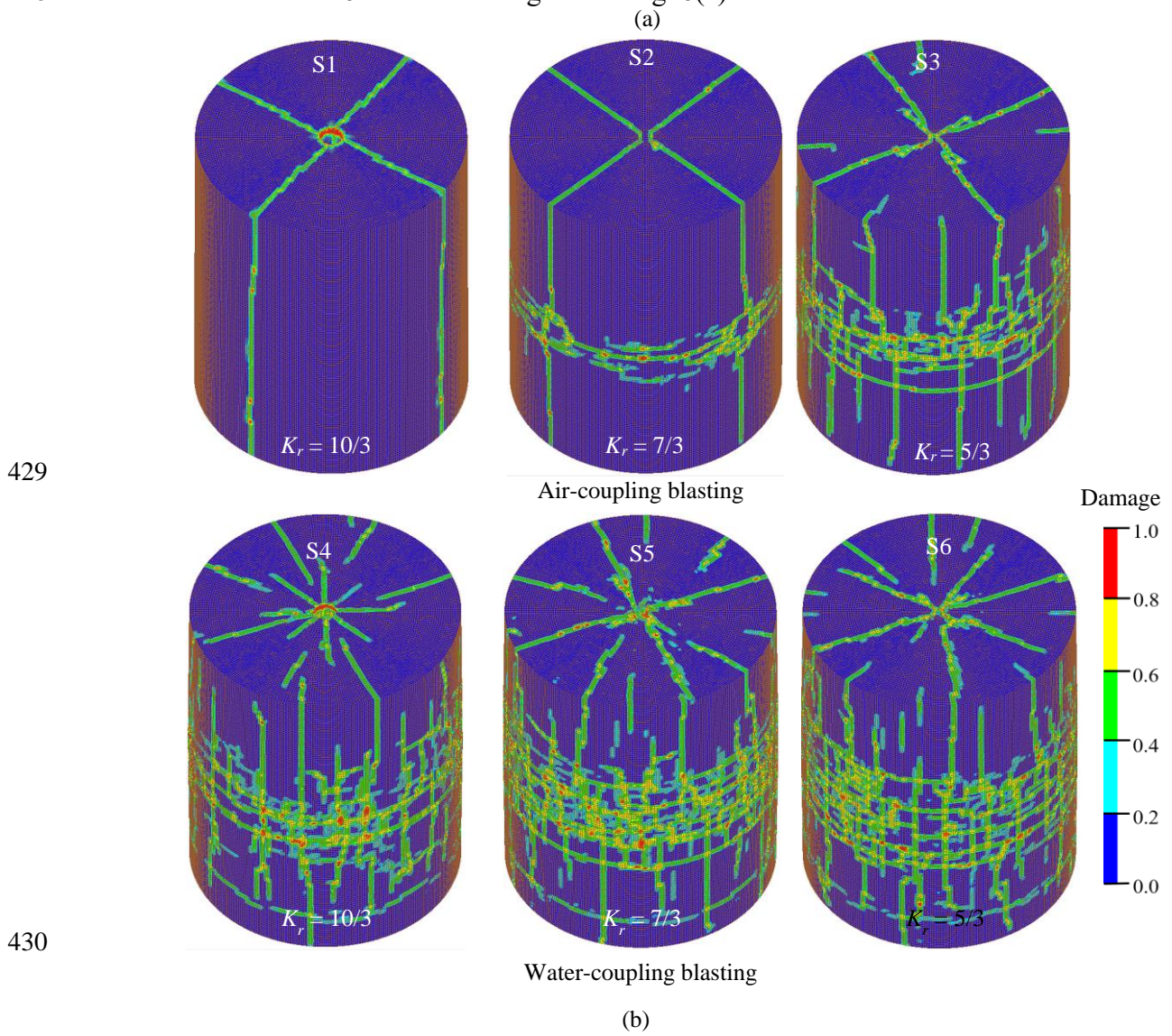
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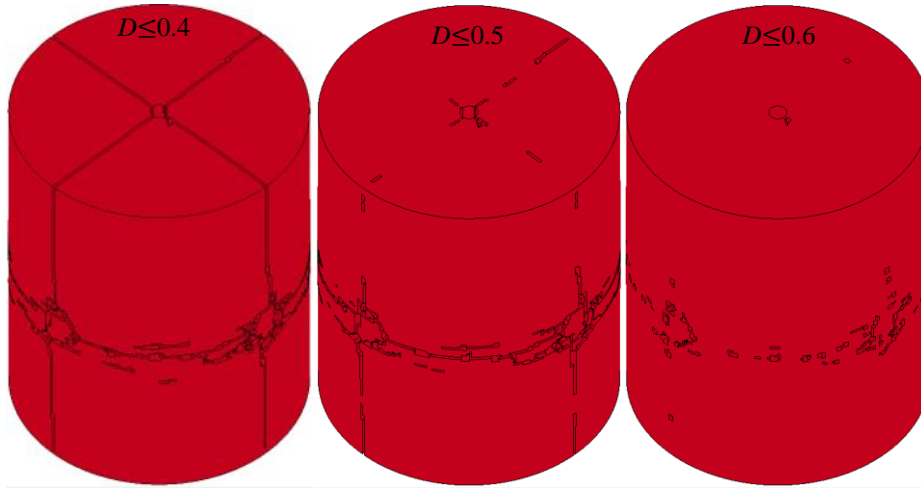
409 Fig. 5 Simulation of blast tests: (a) Damage pattern evolution, (b) History curves of explosion-induced  
 410 pressure at the target point

411 The simulated damage patterns for the abovementioned blast tests are shown in Fig. 6(a).  
 412 It should be pointed out that in the current study, no element erosion algorithm is used during  
 413 calculation since the element deletion is non-conservative energetically and may distort the  
 414 transmission of explosion-induced stress waves, resulting in unrealistic rock cracking (Bobaru  
 415 and Zhang, 2016, Song et al. 2008). In the current study, an alternative method in post-processing  
 416 using the Pre-post code is employed to evaluate rock fracture and rock disintegration. During  
 417 blasting simulation, the damage of rock material ( $D$ ) accumulates from 0 to 1, and the  $D$  denotes  
 418 the damage extent of rock element from slight degradation to complete failure. Under this  
 419 situation, the critical damage for rock cracking can be determined though comparing the  
 420 simulated crack pattern after blanking the damaged rock element with a certain level (an  
 421 example of simulated crack patterns with different damage levels of S2 is presented in Fig. 6(b)  
 422 with red background color), and the tested fragment morphology, as shown in Fig. 3. After  
 423 comprising, it is apparent that small damage level ( $\leq 0.3$ ) for blanking element produces too  
 424 large cracks whereas large damage level ( $\geq 0.5$ ) gives too few cracks, which is unreasonable  
 425 for generating simulated rock cracks. So, a critical value of  $D = 0.4$  is obtained for the



426 generation of rock fracture. Then, the simulated crack patterns for all blast tests can be obtained  
 427 by blanking rock elements whose damage level is over 0.4 in the Pre-post, and the resulting  
 428 fracture networks for 6 blast tests are given in Fig. 6(c).

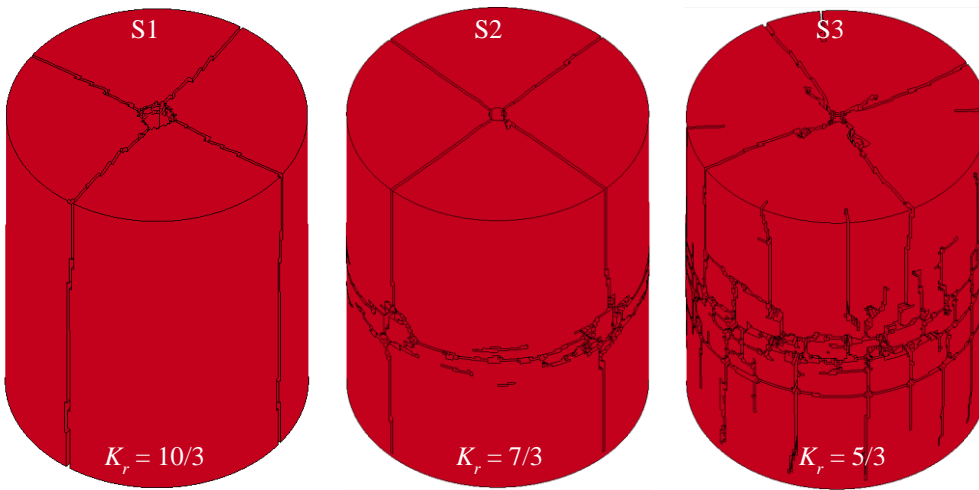




432

(c)

433



434

435

Air-coupling blasting



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437

438

Water-coupling blasting

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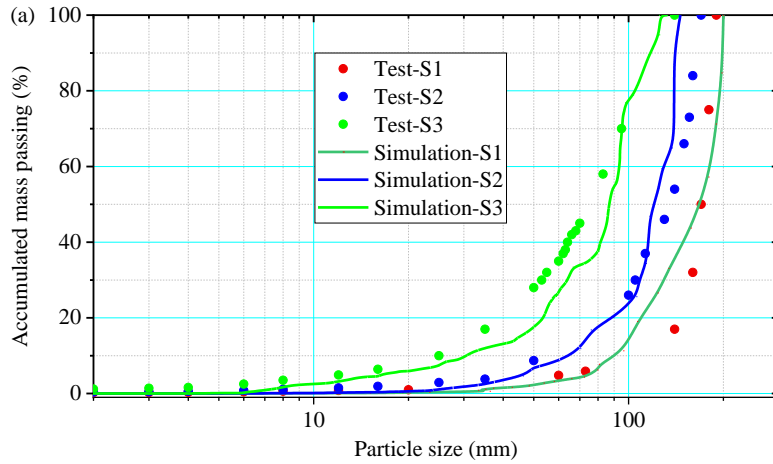
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Fig. 6 Simulation results of rock blast tests (a) the final damage crack patterns, (b) crack patterns with different damage levels of test S2 and (c) fracture networks after blanking damaged rock elements ( $D \leq 0.4$ )

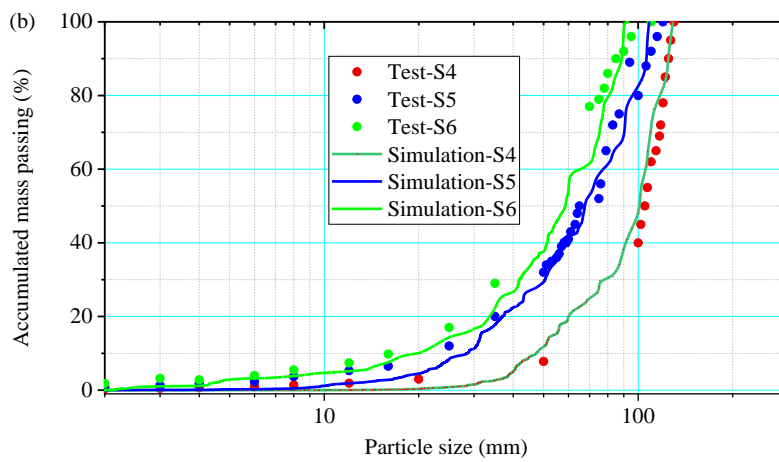


441 As can be seen in Fig. 6(c), the simulated cracks in sample S1 run through the whole  
442 specimen and break it into 4 fragments (quarter cylinder), and sample S2 is fragmented into 8  
443 main large pieces (about half of a quarter cylinder). Sample S3 is broken into smaller fragments  
444 due to the narrow air gap. By contrast, samples S4-S6 are disintegrated into more and smaller  
445 pieces than samples S1-S3 because water-coupling transmits higher explosion-induced stress  
446 to rock. Similar to the physical tests, the simulations of water-coupling blasting give rock  
447 fractures with not much difference. By comparing the fragment morphology in blasting tests  
448 and rock fracturing in numerical simulations, it can be pointed out that the rock fracture patterns  
449 obtained in simulations agree well with the cracking modes in physical experiments.

450 Noting that no rock fragment detaches and drops from granite sample in simulation  
451 because of finite element modelling. To add reliability to the current simulation, the FSDs are  
452 obtained by image-processing the simulated crack patterns and compared with those from  
453 blasting tests. After blanking the rock element damage level exceeding 0.4, the numerical  
454 model is uniformly cut at  $x = 0$  mm,  $y = 0$  mm, and  $z = 75, 150$  and  $225$  mm, and the geometry  
455 information of fragmentation in these 5 cut surfaces is identified using the image-processing  
456 code ImageJ (Durda et al., 2015). The resulting distributions of fragment size in these 5 cut  
457 surfaces are merged to represent the overall fragmentation in simulation. The comparison of  
458 cumulative frequency distributions of fragment size obtained by combined numerical  
459 modelling and image-processing, and from physical testing is shown in Fig. 7. As can be seen,  
460 the size and the distribution span of fragment increase with the increase of decoupling ratio.  
461 Meanwhile, in both air-coupling blasting and water-coupling blasting, the simulated FSDs are  
462 well consistent with those in the blasting experiment. Based on the good agreements in rock  
463 breakage and FSD between blasting test and numerical simulation, it can be concluded that the  
464 developed numerical model is suitable and applicable for modelling rock fragmentation  
465 induced by decoupled charge blasting using air-coupling and water-coupling with free surfaces.



466



467

468 Fig. 7 Comparison of tested and simulated FSDs: (a) FSDs in air-coupling blasting, (b) FSDs in water-  
 469 coupling blasting

### 470 3. Numerical modelling of rock fragmentation in decoupled charge blasting

#### 471 3.1. Computational model

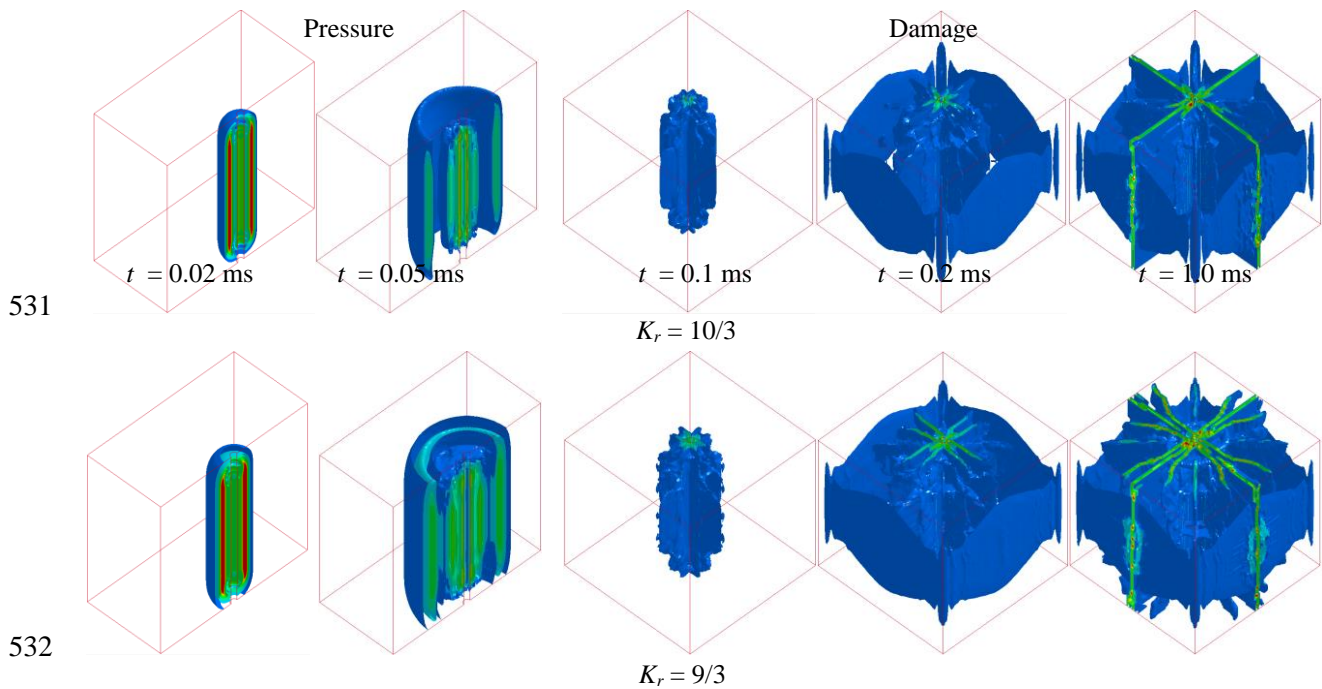
472 In this section, the cubic single-borehole models with a hole diameter  $D$  of 42 mm which  
 473 is commonly used in controlled blasting in China are built to investigate the rock fragmentation  
 474 induced by decoupled charge blasting, as shown in Fig. 8. Considering the specific charge  
 475 commonly used in practical blasting, the side length of model is set as 1 m, and the stemming  
 476 length at model top and bottom is 0.1 m. Two decoupled charge modes, i.e. radially decoupled  
 477 charge and axially decoupled charge, two coupling mediums, i.e. air and water, and seven  
 478 decoupling ratios (4/3, 5/3, 6/3, 7/3, 8/3, 9/3 and 10/3) are considered in the present simulation.

479 Different from the blasting tests introduced in Section 2, the decoupling ratio in the  
480 computational model is controlled by changing charge diameter or charge length instead of  
481 borehole diameter. The explosive is detonated at the centre of the model, i.e., at the middle  
482 point of charge column ( $z = 0.5$  m). All boundaries of model are set as free boundaries because  
483 free boundaries generally exist in actual blasting such as smoothwall blasting. Mesh size  
484 convergence tests are carried out with different meshes to minimize the effect of mesh size on  
485 numerical results, and the crack pattern is the main issue checked because of the topic of rock  
486 fragmentation. After the mesh size convergence test, the model is finally discretized with 1 014  
487 400 hexahedral elements. The elements with a size of  $1 \text{ mm} \times 1 \text{ mm} \times 10 \text{ mm}$  mesh for  
488 explosive, and the elements with a size of  $10 \text{ mm} \times 10 \text{ mm} \times 10 \text{ mm}$  mesh for rock. It should  
489 be pointed out that the mesh size varies in the vicinity of the hole and the max/min length for  
490 explosive element is 10 whereas it is 2 for rock element. The common nodes are shared in the  
491 elements at the interfaces between the explosive, air/water, rock and stemming, and the large  
492 deformation and material mix near the decoupling charge are solved by the *multi-material ALE*  
493 algorithm. An MPP LS-DYNA solver (version 8.0) with 28 Cores is used to run this modelling,  
494 and half an hour is taken for the typical simulation of this class of model. During calculation,  
495 the explosion pressure at the target point (0.25, 0, 0.5/m) is recorded to investigate the pressure  
496 attenuation in rock under decoupled charge blasting.

497 After running the following calculations and generating fracture networks, 9 cut surfaces  
498 ( $x = -0.25, 0, \text{ and } 0.25$  m;  $y = -0.25, 0 \text{ m and } 0.25$  m;  $z = 0.25, 0.5, \text{ and } 0.75$  m) are chosen  
499 to cut this model uniformly and are image-processed. The resulting FSDs of these 9 cut surfaces  
500 are emerged to represent the overall fragmentation created by decoupled charge blasting. Then,  
501 a three-parameter generalized extreme value (GEV) function (Hogan et al., 2012; Hou et al.,  
502 2015; Shen et al., 2017), which performs well in characterizing the FSD of rock under dynamic

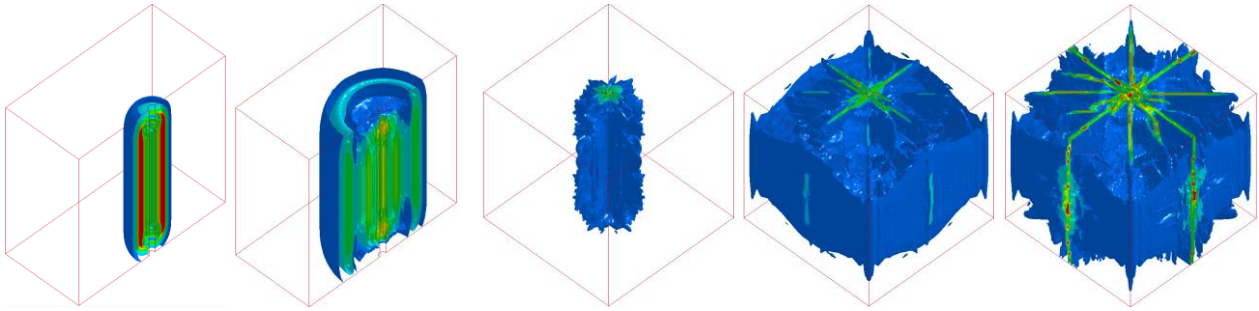


517 It can be found that after the initiation of the radially decoupling charge borehole, the  
518 explosion-induced pressure radially radiates away from borehole. Immediately, a crushed zone  
519 is generated in the vicinity of borehole due to the high explosion pressure, and the size of this  
520 crushed zone increases with the increase of charge diameter while it is larger in water-coupling  
521 blasting than air-coupling one. Then, the radial cracks extend in the rock because the tensile  
522 stress component of explosion-induced stress waves exceeds the tensile strength of rock, and  
523 they finally reach the free surface of rock and disintegrate rock into fragments. During this  
524 process, the spalling damage is generated near the surface due to the reflection of explosion-  
525 induced stress waves and it intensifies greatly with the decrease of decoupling ratio.  
526 Consequently, the radial cracks interact with spalling cracks, forming the final crack patterns.  
527 As expected, a larger high-pressure zone, as presented in Fig. 9, and higher pressure, as shown  
528 in Fig. 10, are formed by the detonation of decoupled charge with large charge diameter and  
529 water-coupling due to more explosive and great stress transmission performance of water, and  
530 therefore more damage cracks are formed with smaller decoupling ratio and water-coupling.



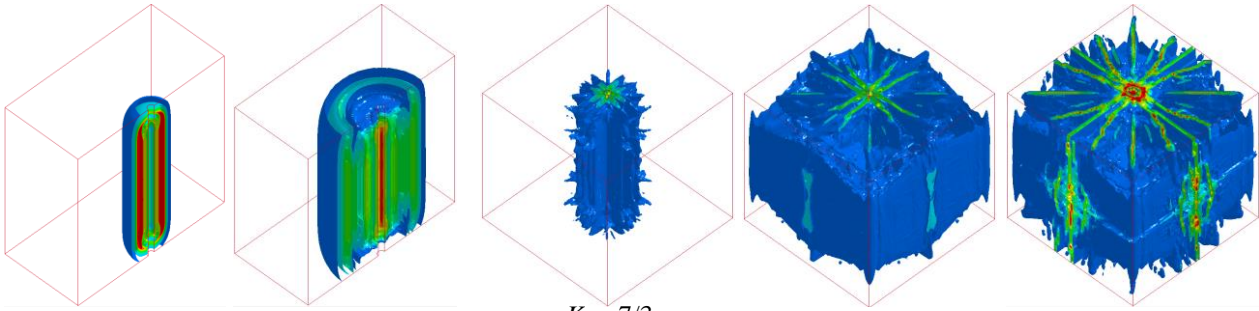


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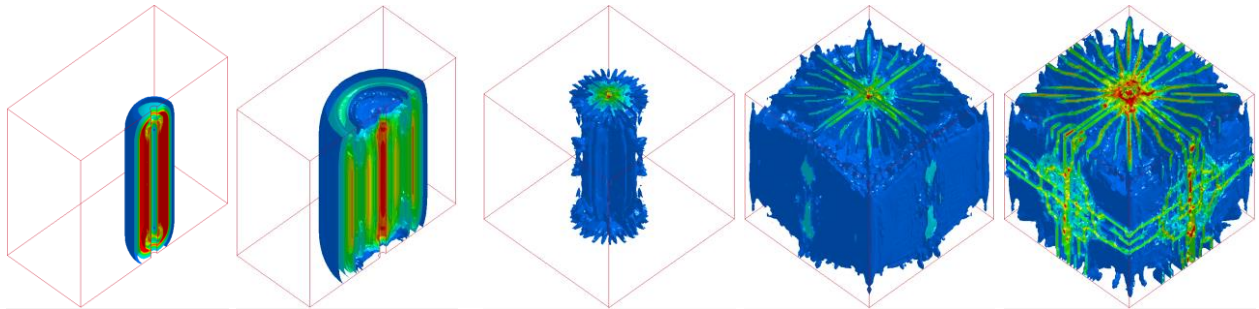
$K_r = 8/3$

534

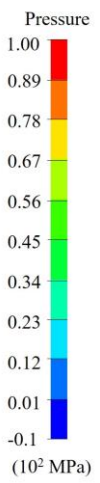


$K_r = 7/3$

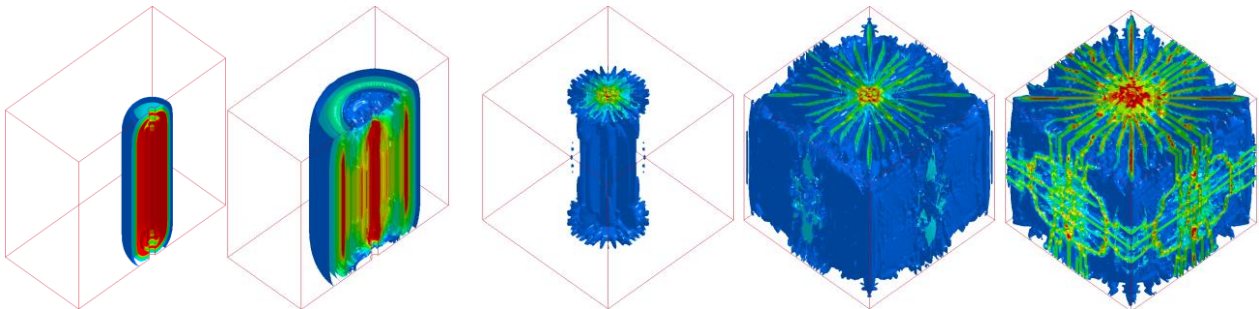
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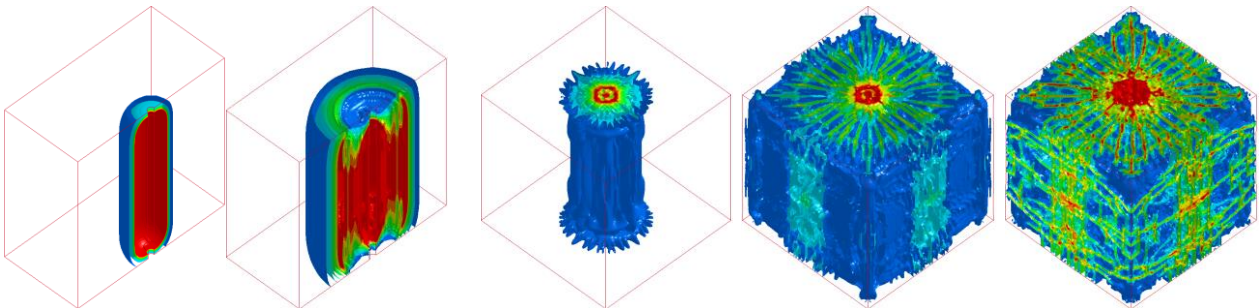
$K_r = 6/3$



538

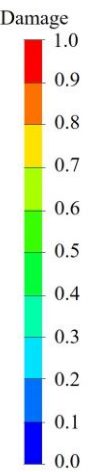


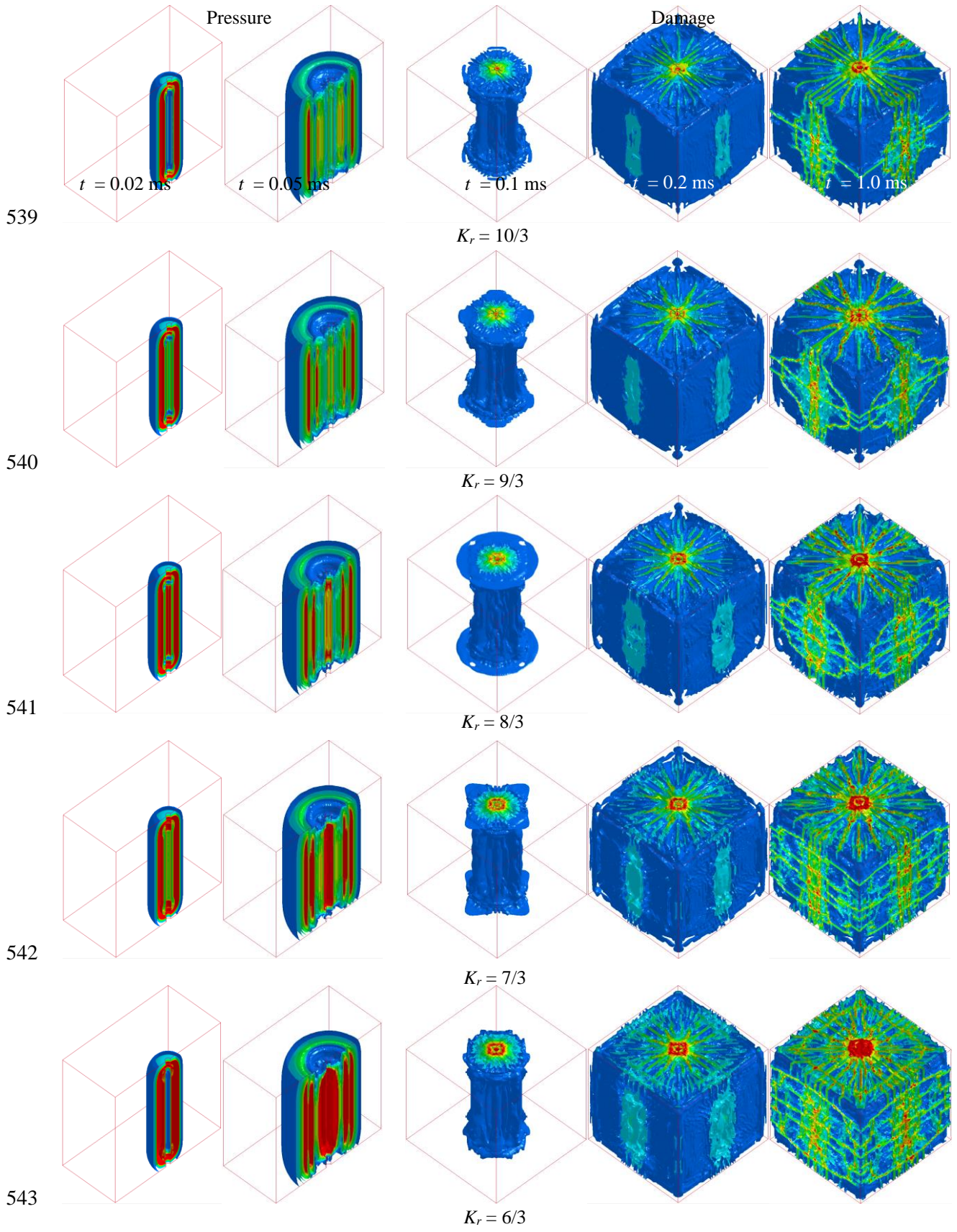
$K_r = 5/3$



$K_r = 4/3$

(a)







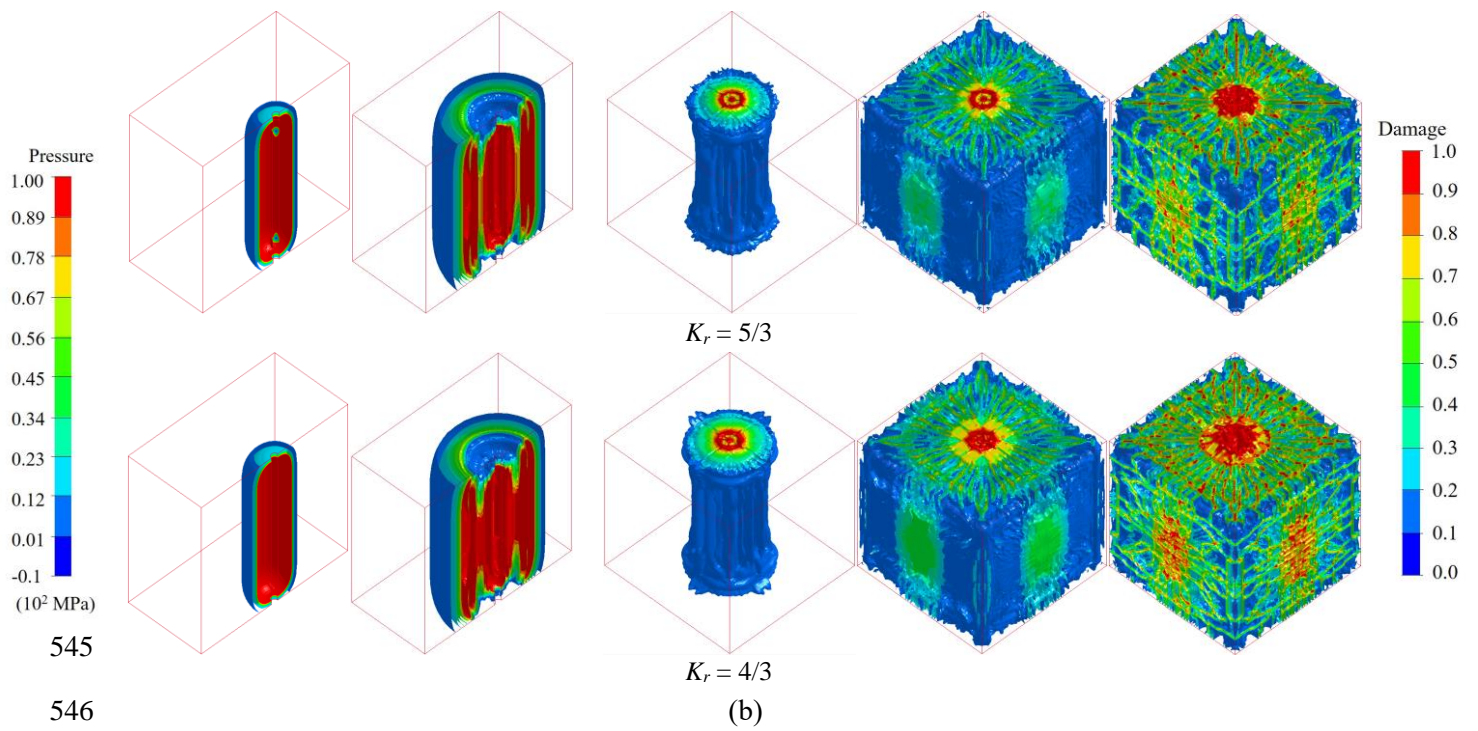
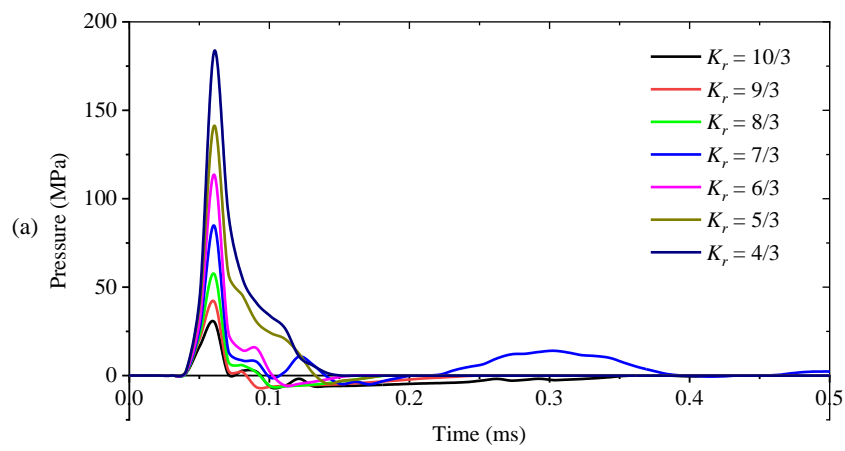
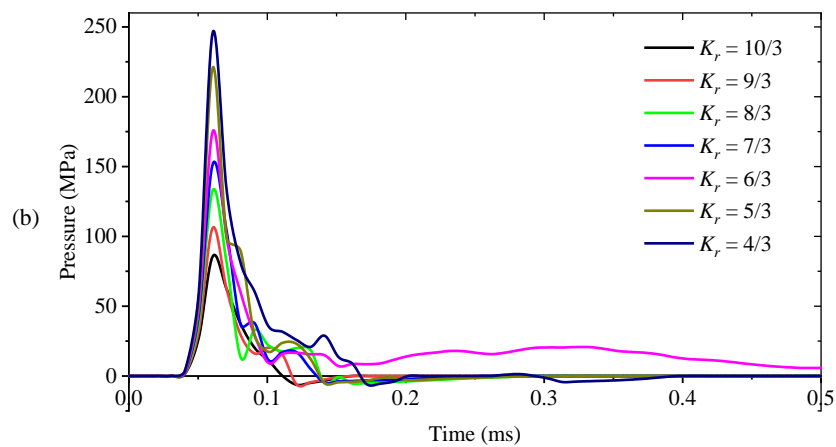


Fig. 9 Explosion pressure in rock and damage cracks induced by radially decoupling blasting with (a) air coupling and (b) water coupling



549



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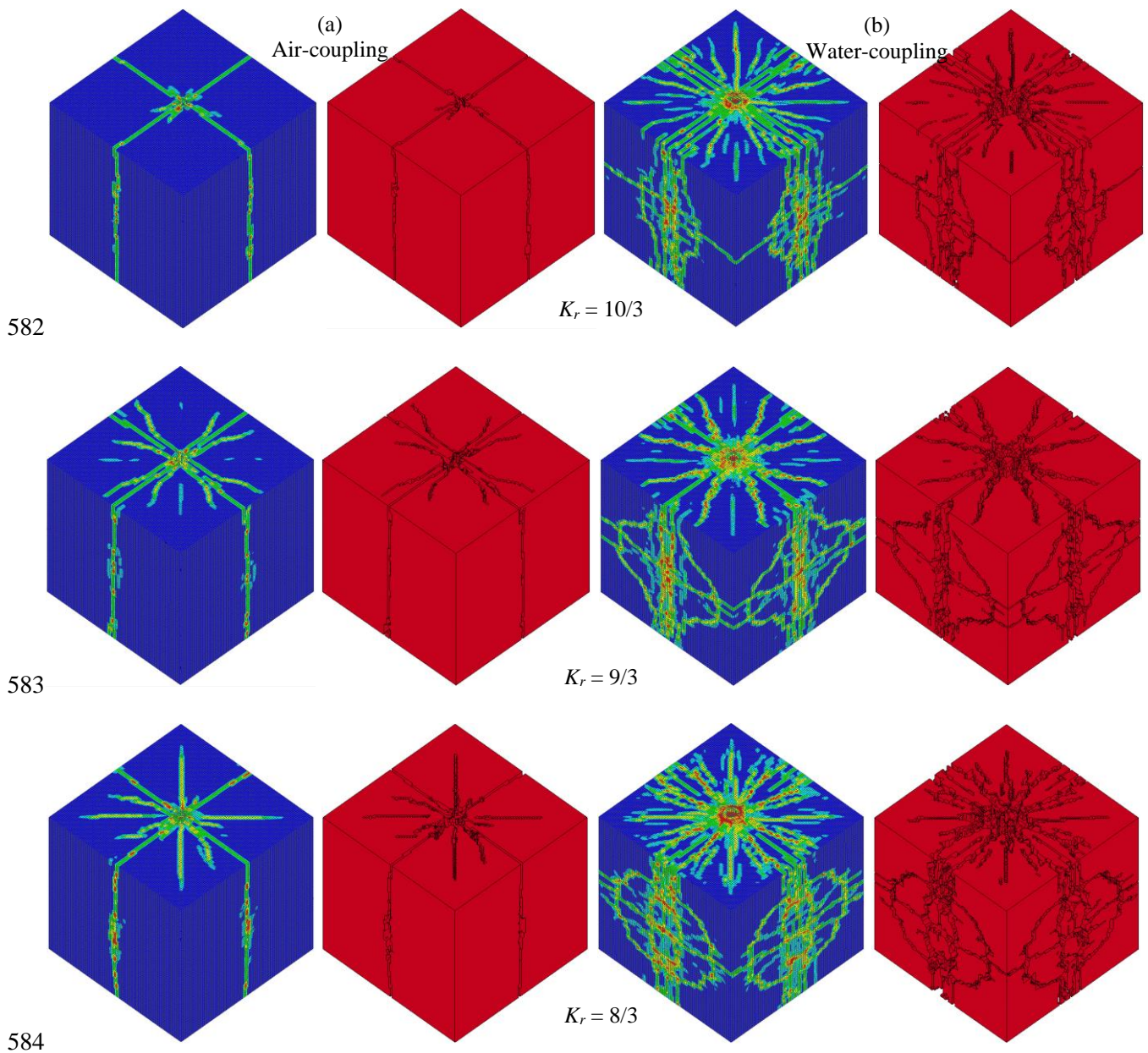


551 Fig. 10 Time-history curves of explosion pressure at target point (0.25, 0, 0.5/m) induced by radially  
552 decoupling blasting with (a) air coupling and (b) water coupling

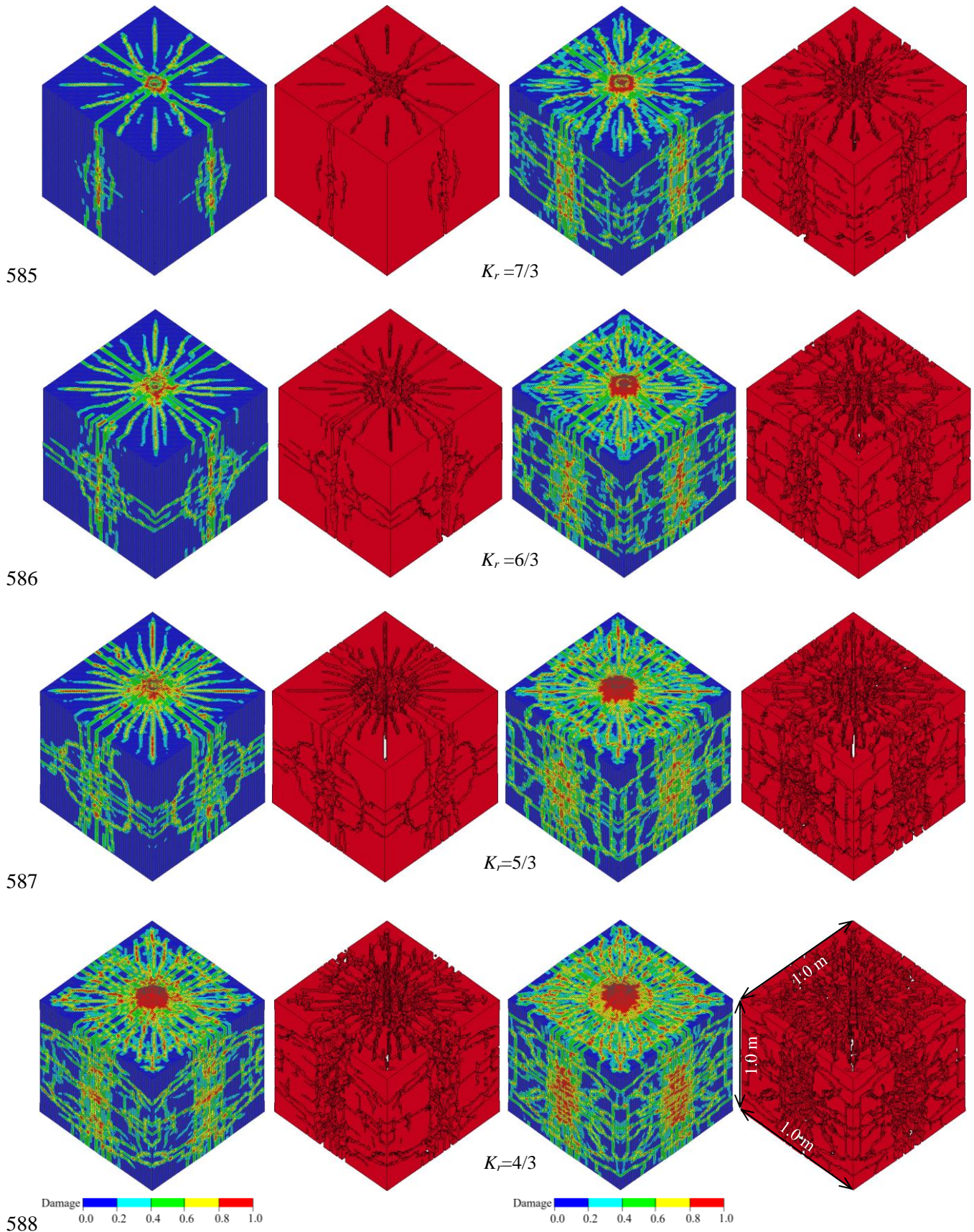
553 The final damage patterns induced by radially decoupled charge blasting (opaque view  
554 with mesh) and corresponding fracture networks are presented in Fig. 11. It is apparent that the  
555 changes in the charge diameter and coupling medium exert a significant influence on the  
556 development of blast-induced fractures. In the cases of air-coupling blasting, as shown in Fig.  
557 11(a), the numbers of radial cracks and vertical cracks (cracks propagating in the  $z$  direction)  
558 increase with the decrease of decoupling ratio due to the increased explosion energy. To be  
559 more specific, as the air-filled borehole detonates with  $K_r = 10/3$ , four main radial cracks  
560 develop in the rock and two mutually perpendicular cutting surfaces are formed. Consequently,  
561 this cubic rock block is uniformly cut into four big fragments (quarter cube). When the charge  
562 diameter increases, the number of radial cracks raises, and in the range of  $8/3 < K_r \leq 10/3$ , the  
563 cracking patterns in different planes vertical to borehole axial are almost identical, i.e., the  
564 blast-created rock fracture is in the form of radiation-shape cracking. Then, as the decoupling  
565 ratio continuously decreases from  $7/3$  to  $4/3$ , the crushed zone expands rapidly and more radial  
566 and vertical cracks initiate and propagate in the rock. Meanwhile, the blast-induced cracks  
567 propagating in the radial direction and axial direction interact with each other, forming  
568 massively developed rock cracks. Especially in the air-coupled blasting with  $K_r = 4/3$ , the blast-  
569 induced fractures massively develop inside the rock three-dimensionally and thus disintegrate  
570 the rock with a large number of small fragments.

571 In contrast to air-coupled blasting, massively developed cracking is the main fracturing  
572 form in water-coupling blasting, as shown in Fig. 11(b), and much more cracks including radial  
573 cracks and vertical cracks are created after the detonation of water-filled borehole, implying  
574 that smaller rock fragment size is generated. Besides, it is noted that the discrepancy in rock  
575 breakage under water-coupling blasting with different decoupling coefficients is less obvious

576 compared with that under air-coupling blasting, indicating that the performance of water-  
577 coupling blasting is more robust to the change in charge diameter than that of air-coupling one.  
578 Furthermore, with the decrease in decoupling ratio, the difference in the rock fracture between  
579 air-coupled blasting and water-coupled blasting becomes smaller due to the thickness reduction  
580 of the coupling medium. Obviously, the extent of blast-induced fracture is jointly controlled by  
581 the characteristics and thickness of the coupling material.





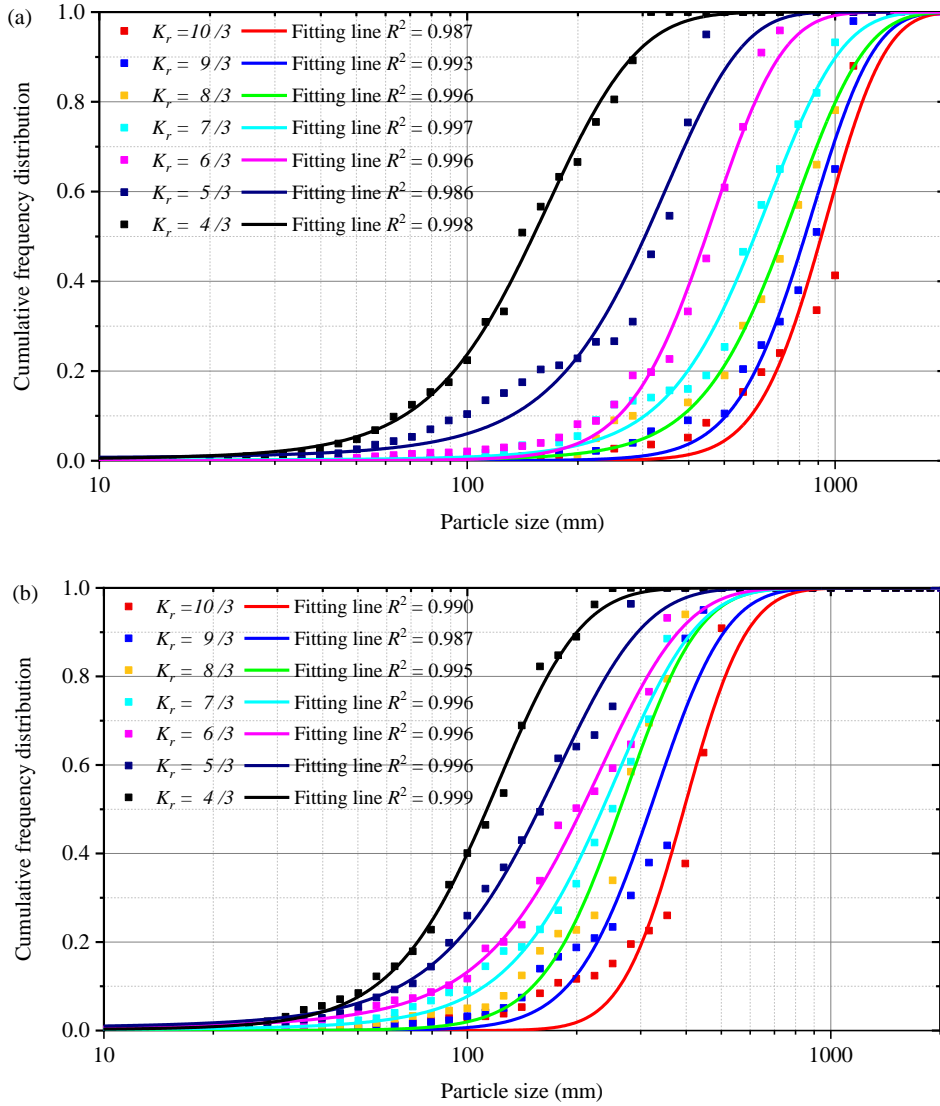


589 Fig. 11 Damage patterns and fracture networks induced by radially decoupling blasting with (a) air  
 590 coupling and (b) water coupling

591 It is acknowledged that when the explosion energy per unit volume increases, more  
592 fractures and cracking surfaces in rock are created in rock due to the violent dissipation of  
593 dynamic loading energy. At the same time, the steady growth of radial cracks is gradually  
594 replaced by the disordered development of 3D crack branching. As can be seen from Fig. 11,  
595 as the explosive mass in borehole increases, i.e. with the decrease of decoupling ratio, the  
596 cracking form induced by air-coupled blasting varies due to the increased explosion energy  
597 density acting on borehole wall. When the air-coupled borehole is detonated with a large  
598 decoupling ratio, the rock fracturing is mainly controlled by a few radial cracks, which can  
599 generate smooth excavation surfaces parallel to the borehole axial and is beneficial to  
600 controlled blasting. In fact, in controlled blasting such as presplitting and smoothwall blasting,  
601 lightly radial charged hole is widely adopted for the creation of smooth excavation perimeter  
602 (Hu et al. 2014, 2018; Singh et al. 2014). However, when increasing the charge diameter or  
603 filling the hole with water, the fracturing form changes from radial cracking to massively  
604 developed cracking, and thus the efficiency of rock fragmentation significantly improves,  
605 which is conducive to rock excavation in production blasting. These findings are similar to the  
606 observations in laboratory-scale blasting tests conducted by Chi et al. (2022). Additionally, in  
607 the actual blasting, small decoupling ratio and water coupling are commonly employed to  
608 improve the rock fragmentation performance (Huo et al. 2020; Jang et al. 2018).

609 The cumulative frequency distributions of rock fragmentation obtained in radially  
610 decoupled charge blasting via the combined finite element modelling and image-processing  
611 and the corresponding fitting curves using the three-parameter GEV function are presented in  
612 Fig. 12. It can be seen that the GEV function matches the data of FSDs created by decoupled  
613 charge blasting with good accuracy. With the reduction of decoupling ratio, the fitting curves  
614 rise earlier, and the size of the biggest fragment decrease, which implies that the rock fragment  
615 size gradually shifts toward finer dimension with a more uniform distribution. Furthermore, by

616 comparing the FSDs generated by air and water coupling blasting, it can be indicated that with  
 617 the same decoupling ratio, smaller fragment size and more uniform FSD is formed under water-  
 618 coupling blasting, which is consistent with the observations in numerical results shown in Fig.  
 619 11 and the findings in the experiments of Chi et al. (2022).



620

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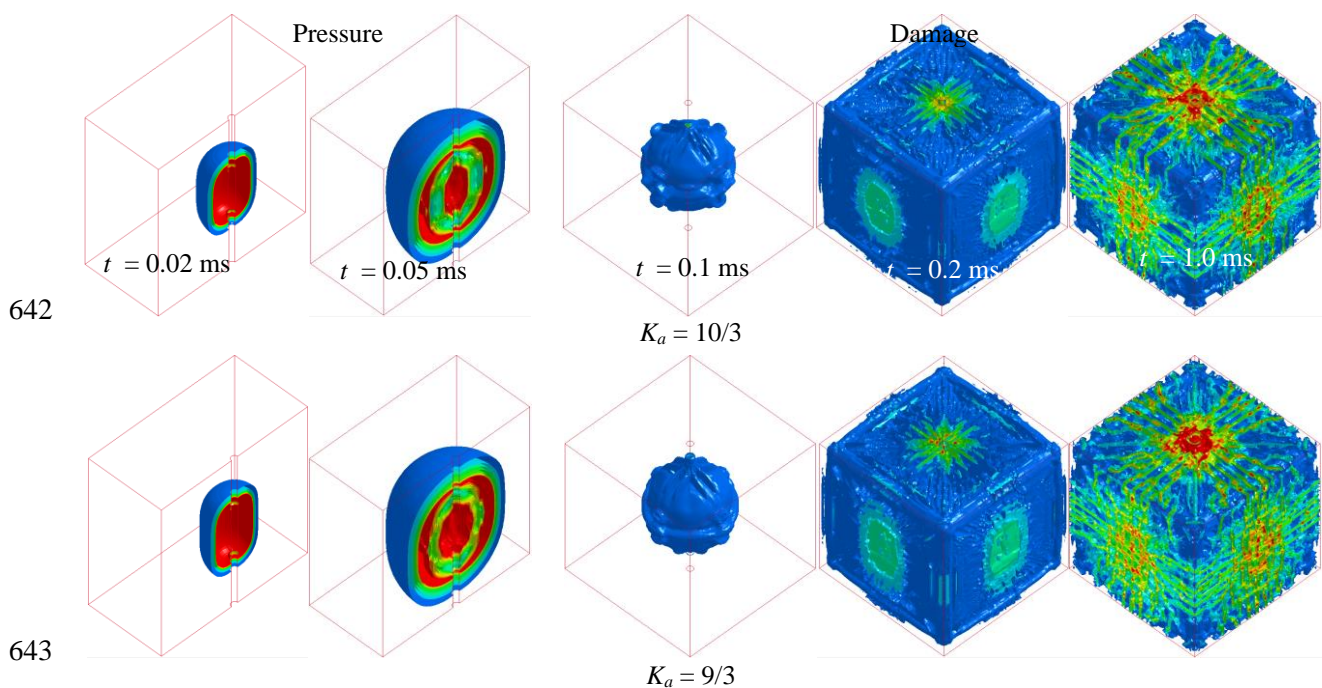
622 Fig. 12 FSDs and corresponding fitting curves in radially decoupled charge blasting with (a) air  
 623 coupling and (b) water coupling

624 **3.3. Rock fragmentation induced by axially decoupled charge blasting**

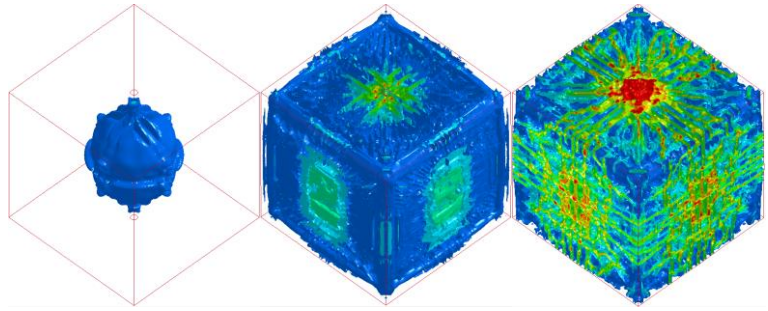
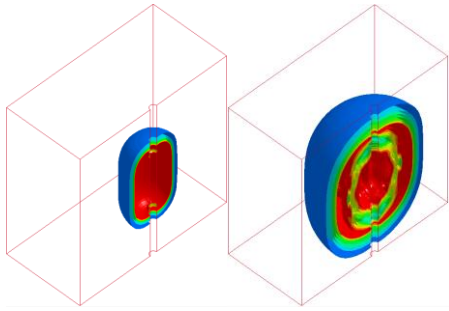
625 Then, the influences of axially decoupled charges on rock fragmentation are numerically  
 626 examined with different decoupling ratios and distinct coupling mediums, and the processes of



627 explosion pressure evolution and damage crack propagation induced by axially decoupling  
 628 blasting are given using transparent view in Fig. 13. Different from radially decoupled charge  
 629 blasting, after detonation, ellipsoidal explosion pressure radiates outward from the position of  
 630 explosive, and the blast-induced damage zone is also ellipsoidal in the early stage of blast-  
 631 induced damage evolution, especially in blasting with a large decoupling ratio. Then, radiation-  
 632 shape cracks propagating from the position of explosive develop outwards and finally cross  
 633 through the whole rock. During the development of radiation-shape cracks from the detonation  
 634 point, spalling damage is formed in the vicinity of surface and interacts with radiation-shape  
 635 cracks. Moreover, the corresponding time-history curves of explosion pressure at target point  
 636 are presented in Fig. 14. Similar to decoupled charge blasting using radially decoupled charge,  
 637 the explosion pressure peak increases with the decrease of decoupling ratio, and water-coupling  
 638 produces higher explosion pressure. But with the same decoupling ratio and coupling medium,  
 639 the explosion pressure peak in axially decoupled charge blasting is higher. Besides, a smaller  
 640 difference in pressure peak between air-coupling blasting and water-coupling blasting is found  
 641 in axially decoupled charge blasting.

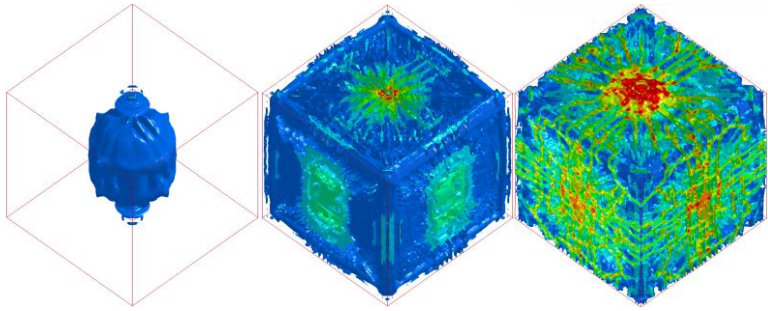
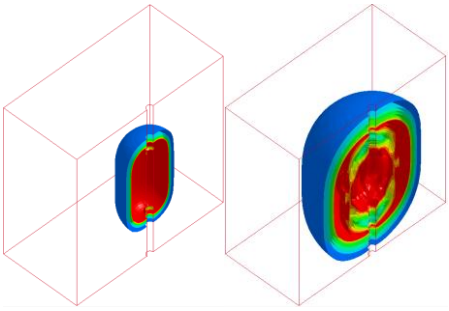


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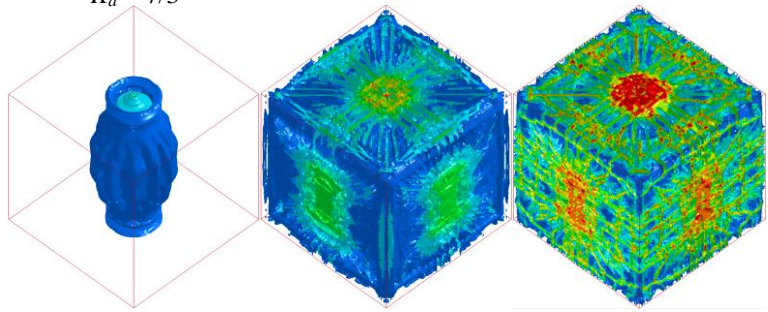
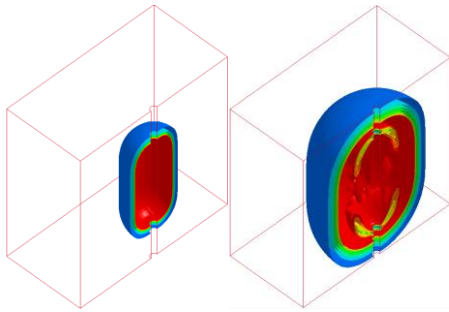
$K_a = 8/3$

645

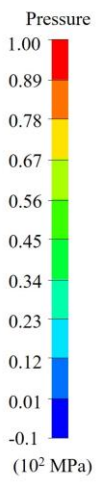


$K_a = 7/3$

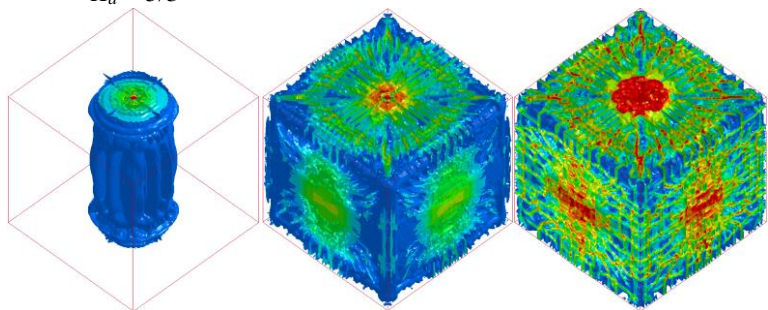
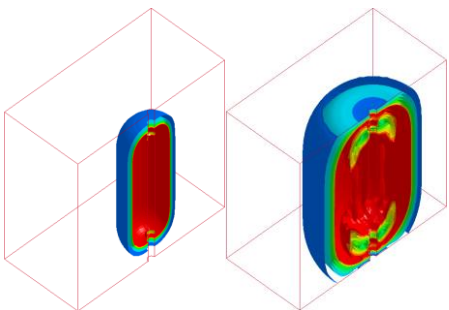
646



$K_a = 6/3$



648



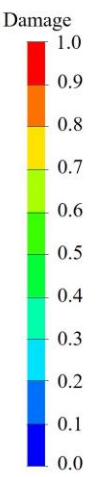
$K_a = 5/3$

649

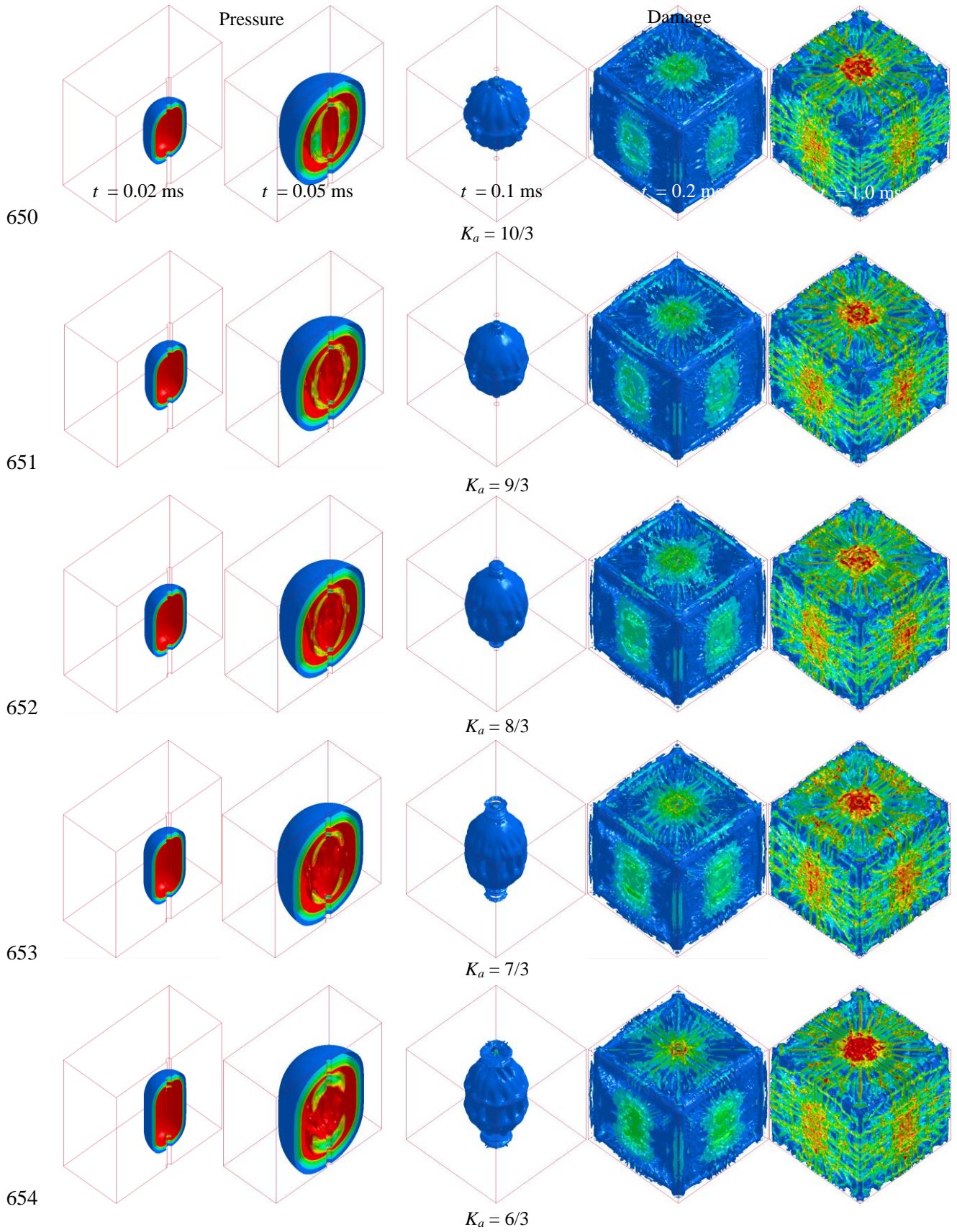


$K_a = 4/3$

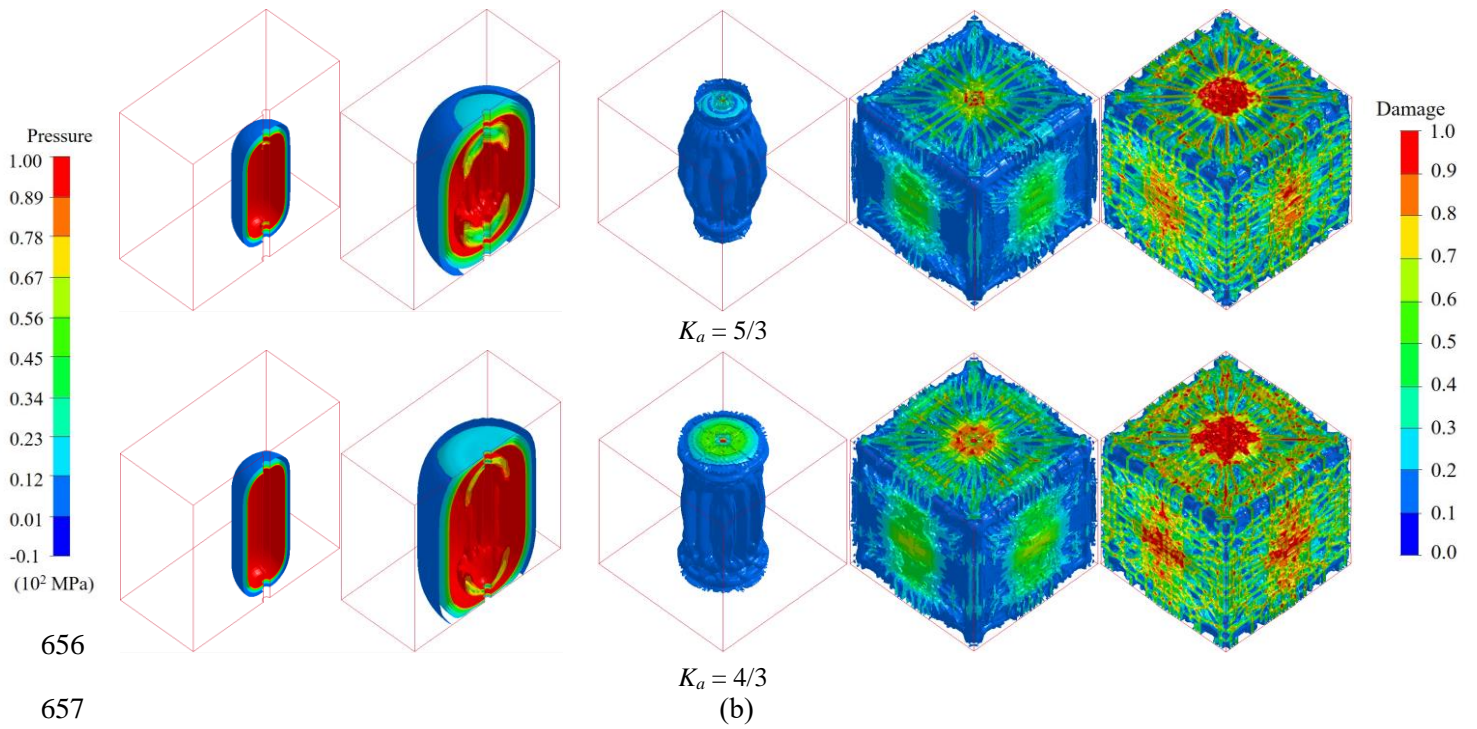
(a)



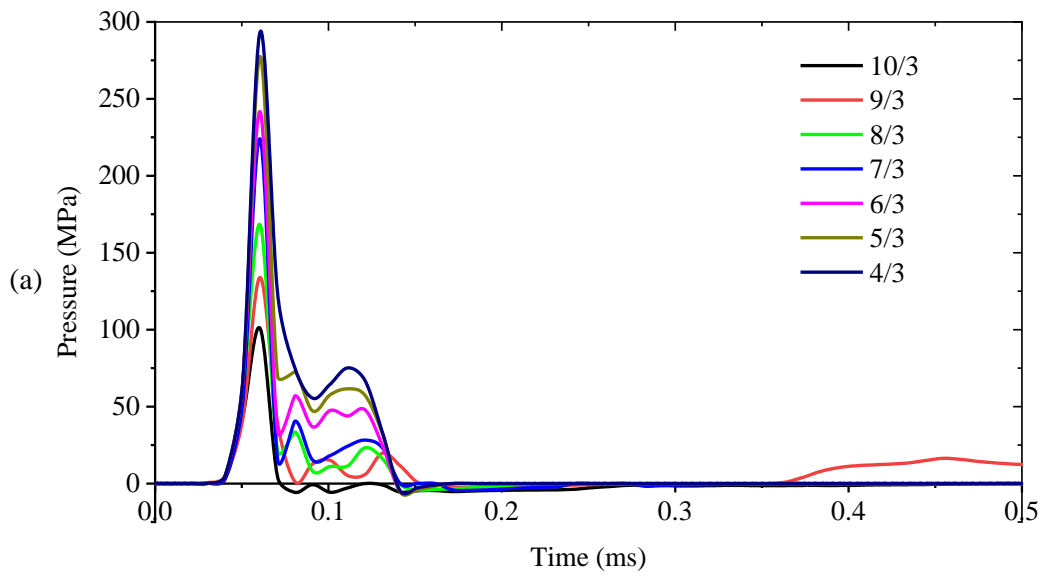


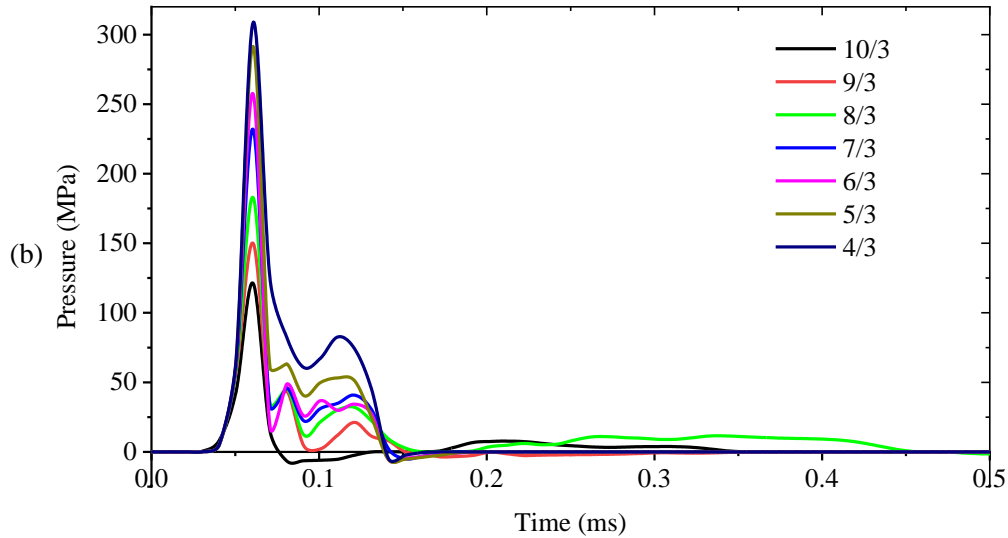






658 Fig. 13 Explosion pressure in rock and damage cracks induced by axially decoupling blasting with (a)  
 659 air coupling and (b) water coupling





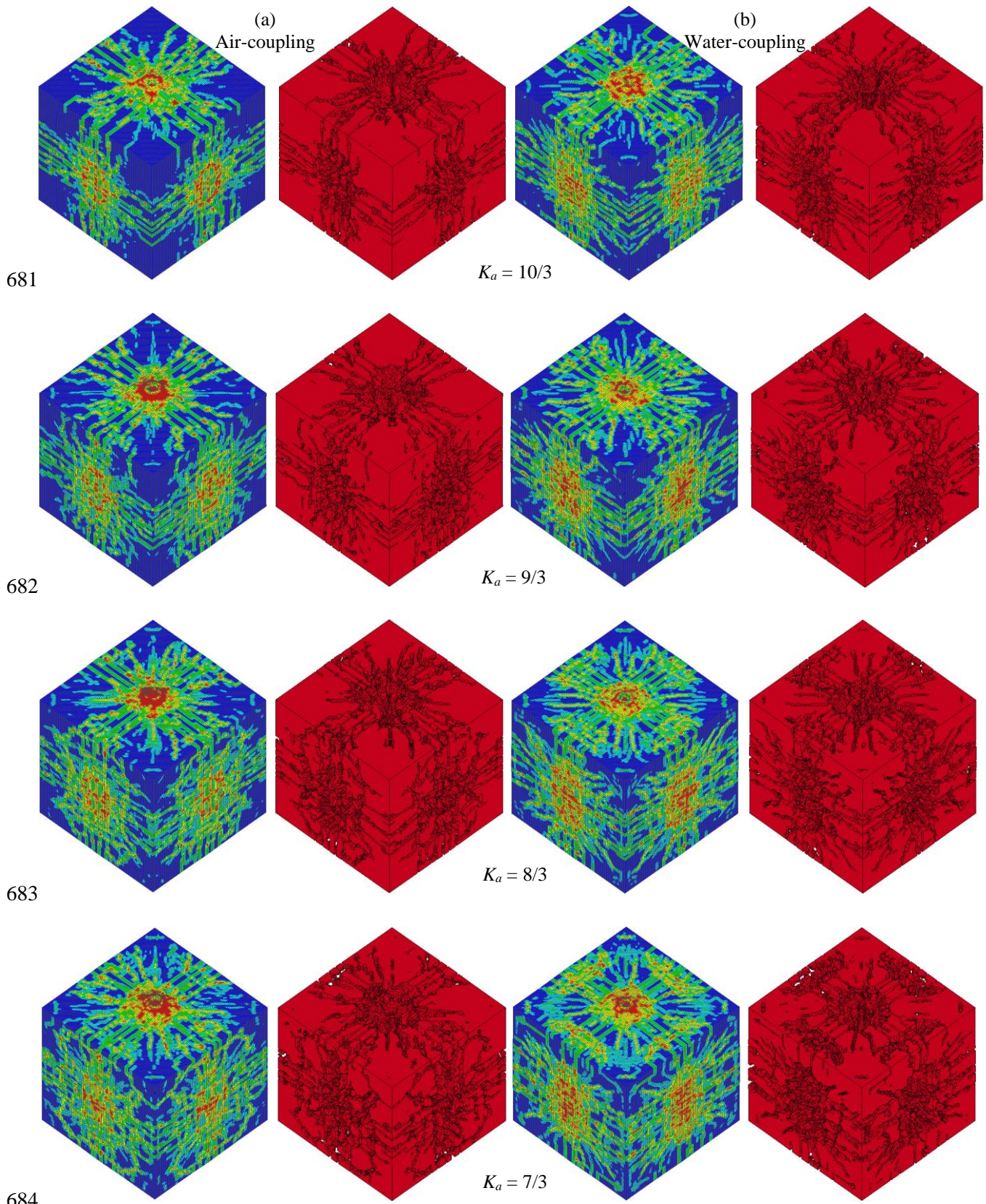
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662 Fig. 14 Time-history curves of explosion pressure at target point (0.25, 0, 0.5/m) induced by axially  
 663 decoupling blasting with (a) air coupling and (b) water coupling

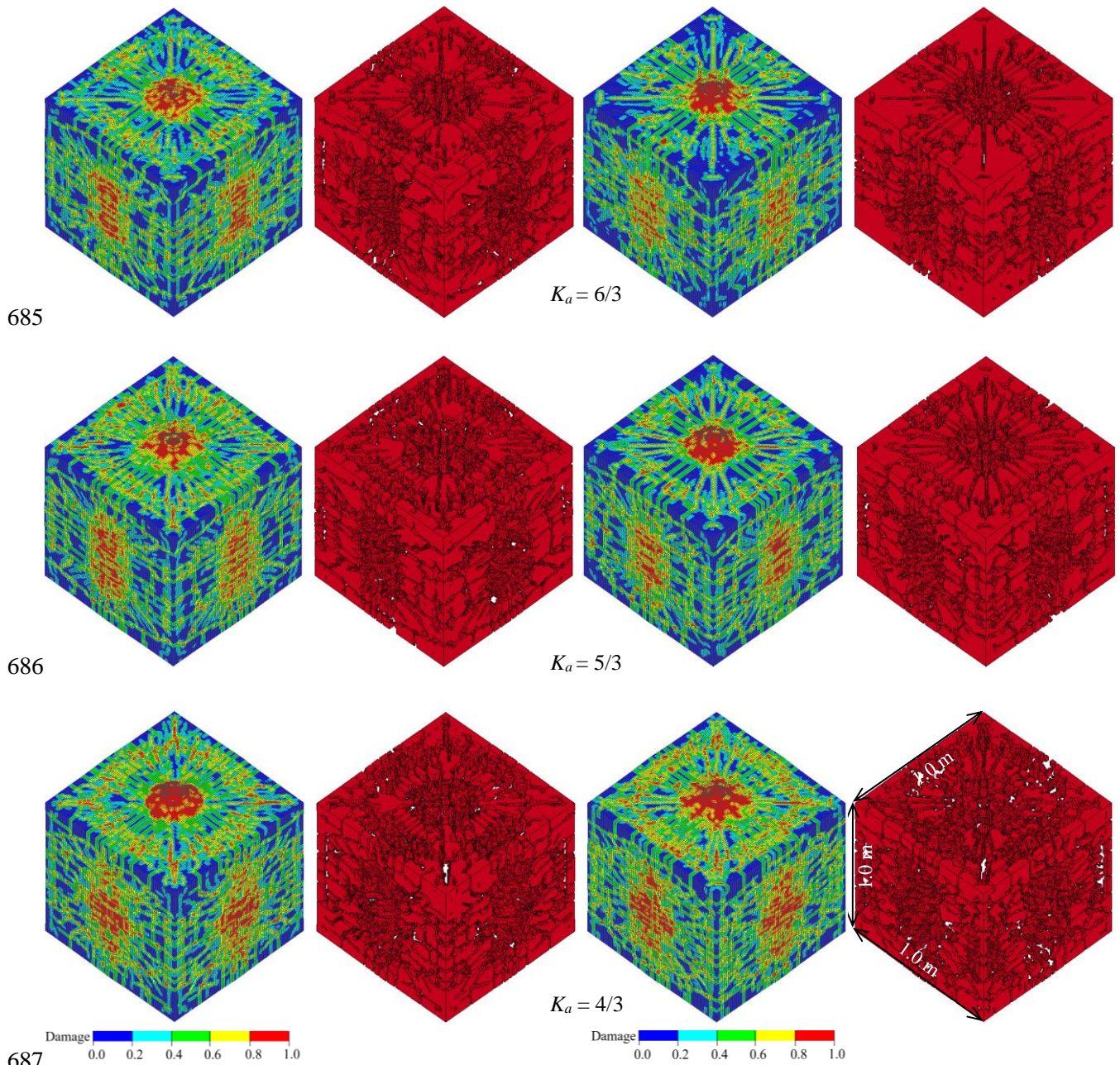
664 The damage patterns using opaque view and corresponding fracture networks are shown  
 665 in Fig. 15. In consistency with blasting with radially decoupled charge, the extent of rock  
 666 fracture gradually becomes higher as the decoupling ratio decreases, and the rock disintegration  
 667 under air-coupling blasting is slighter than that under water-coupling blasting. These findings  
 668 also agree with the simulated explosion pressure presented in Fig. 14. Besides, the rock  
 669 fracturing under water-coupling blasting with different decoupling coefficients shows a smaller  
 670 difference compared with that under air-coupling blasting. This can be expected since the  
 671 difference in explosion pressure peak between air-coupling blasting and water-coupling  
 672 blasting in axially decoupled charge blasting is smaller than that in radially decoupled charge  
 673 blasting, as can be compared and found between Fig. 10 and Fig. 14. However, in the cases of  
 674 axially decoupled charge blasting, massively developed cracks are created in all air-coupling  
 675 and water-coupling blasts, which increases the potential for the formation of finer fragments.  
 676 Moreover, the difference in rock cracking induced by blasting with various decoupling ratios  
 677 and the discrepancy in rock fracture with different coupling mediums are much smaller  
 678 compared with those in radially decoupled charge blasting, implying a small dependence of



679 rock fracturing on decoupling coefficient and coupling material in axially decoupled charge  
680 blasting.



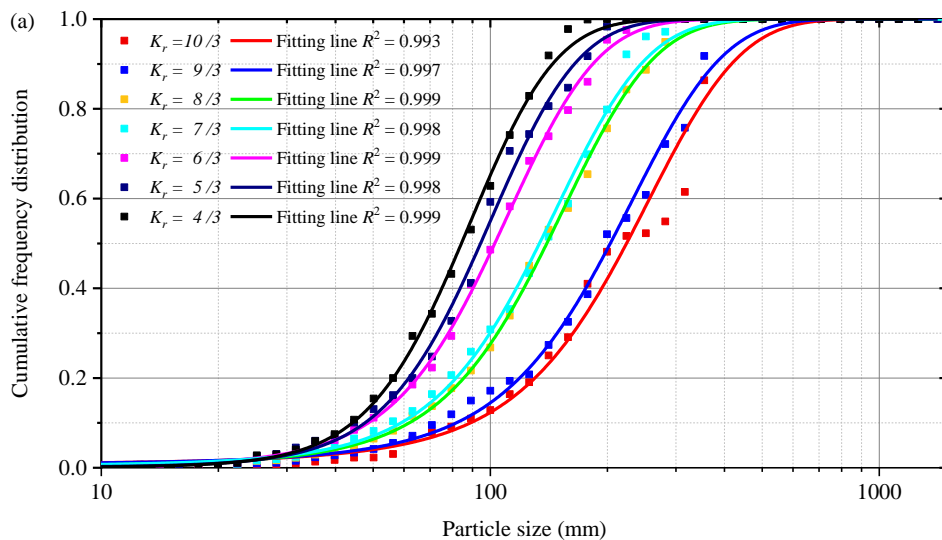




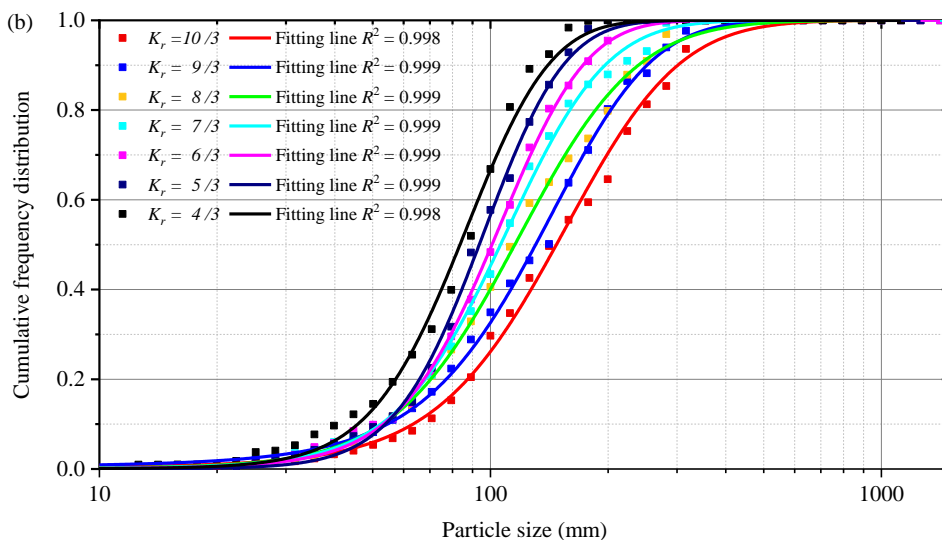
688 Fig. 15 Damage patterns and fracture networks induced by axial decoupling blasting with (a) air  
 689 coupling and (b) water coupling

690 Furthermore, the biggest difference between radially decoupled blasting and axially  
 691 decoupled blasting is the extent of rock fracture. It can be easily observed by comparing Fig.  
 692 11 and Fig. 15 that the rock cracking under axial decoupling blasting is greatly intensified  
 693 compared with that under radial decoupling one. This is the result that the explosion pressure  
 694 peak induced by axially decoupled charge blasting is higher than radially decoupled charge one,  
 695 as shown in Fig. 10 and Fig. 14, and it is attributed to the existence of explosive-rock interface

696 when using axially decoupled charge mode. In other words, the direct contact between  
 697 explosive and rock greatly enhances the energy transmission from explosion products into rock  
 698 mass. Therefore, in practice, a gap between explosive and hole-wall filling coupling medium  
 699 is considerably necessary for alleviating damage to surrounding rock, and the charge structure  
 700 of direct contact is important and highly efficient to facilitate the growth of rock fractures. In  
 701 controlled blasting, lightly loaded boreholes with air-coupling should be employed for the  
 702 stability of the remaining rock, while the axially decoupled charge or decked charge with water-  
 703 coupling can be adopted to fragment rock with high efficiency and cut down the consumption  
 704 of explosive in production blasting.



705



706

707 Fig. 16 FSDs and corresponding fitting curves using the three-parameter GEV function under axially  
708 decoupled charge blasting with (a) air coupling and (b) water coupling

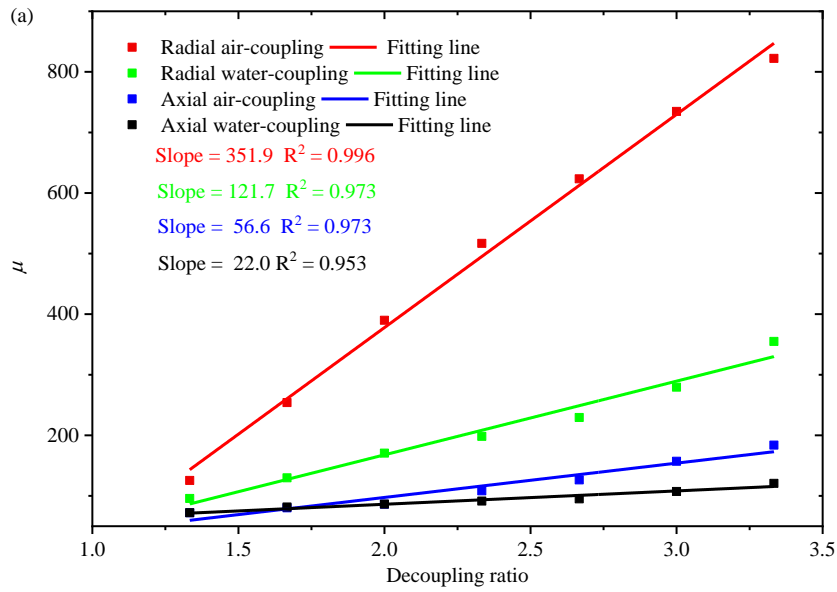
709 Figure 16 shows the resulting cumulative frequency distributions of rock fragmentation  
710 induced by axially decoupled charge blasting and the corresponding fitting curves. Some data  
711 that show relatively large discrepancy against the fitted curve among others are induced by  
712 insufficient fragmentation, i.e., oversize fragmentation. Similar discrepancy can be found in  
713 Fig. 12, especially for data of blasting with a large decoupling ratio, due to the same reason. It  
714 can be seen that the fitting curves rise later with a larger decoupling ratio, and at the same  
715 decoupling coefficient, the fitting curve for cumulative frequency distribution generated by air-  
716 coupling blasting rises later than that of water-coupling one. These results also indicate that  
717 under axially decoupled charge blasting, finer fragments and more uniform FSDs are generated  
718 with the increase of charge length, i.e. the increase of explosion energy. Moreover, air-coupling  
719 blasting creates coarser fragments and more scattering FSD due to the lower efficiency in stress  
720 transmission of air. Compared with FSDs obtained in radially coupled charge blasting, in both  
721 air and water coupling blasts, finer fragment size and narrower range of FSD are formed in  
722 blasting with axially decoupled charge, indicating a growing number of small fragments and a  
723 decreasing size difference between large fragments and fine fragments upon changing the  
724 charge mode from radial decoupling to axial decoupling. This finding means that the axially  
725 decoupled charge mode is more efficient in the energy transmission from explosive to rock  
726 mass.

#### 727 **4. Discussion**

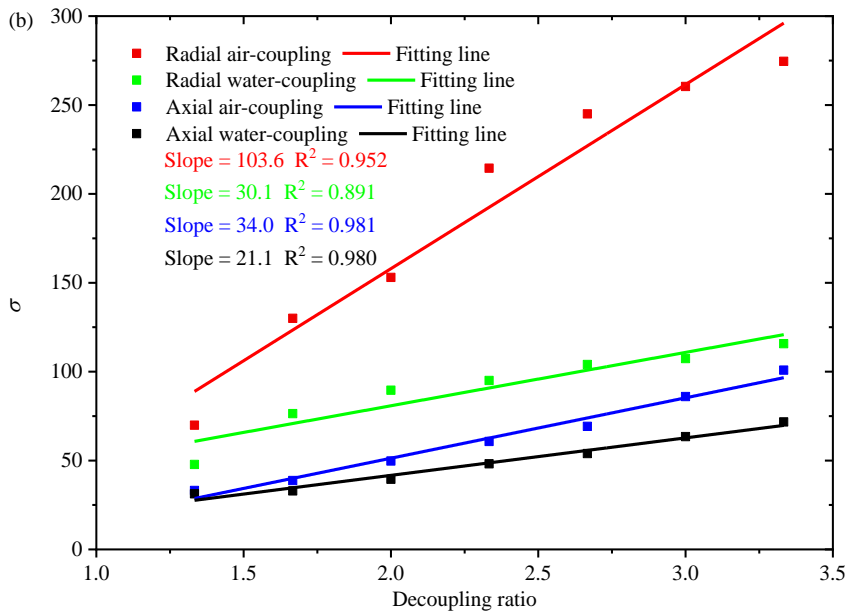
728 It has demonstrated in the present numerical modelling and image processing that the  
729 fragment size and the FSD range under blasting with various coupling mediums and different  
730 decoupled charge modes respond similarly to the change of decoupling ratio. However, the  
731 rates at which the fragment size and the FSD span change are markedly different among these

732 cases of blasting. Figures 17(a) and 17(b) show the variations of the parameters  $\mu$  and  $\sigma$  of the  
733 GEV distribution with respect to the increase of decoupling ratio, which scale with the average  
734 size and size distribution range of the rock fragment, respectively. These plots show that both  
735 the parameters of  $\mu$  and  $\sigma$  increase with the increase of decoupling ratio, suggesting an overall  
736 increase of the fragment size and broadening of the distribution span with the reduction of  
737 charge amount. Moreover, with the same decoupling ratio, larger  $\mu$  and  $\sigma$  are obtained under  
738 blasting with axial decoupling than their counterparts with radial decoupling, and higher values  
739 of  $\mu$  and  $\sigma$  are gotten in blasting with water-coupling, indicating that changing charge mode  
740 from axial decoupling to radial decoupling and replacing coupling material water with air play  
741 extremely remarkable roles in increasing overall fragment size and broadening the range of  
742 FSD.

743 It can be found in Fig. 17 that both the parameters of  $\mu$  and  $\sigma$  show a linearly increasing  
744 trend with the increase of the decoupling coefficient. By linear fitting parameters of  $\mu$  and  $\sigma$ ,  
745 the effects of decoupling ratios on the average size and distribution span of rock fragments with  
746 different coupling mediums and decoupled charge modes can be quantitatively evaluated by  
747 the corresponding slopes. Obviously, the slopes of  $\mu$  and  $\sigma$  with radial air-coupling are much  
748 higher than those with axial decoupling and water-coupling, and they have the lowest value in  
749 the case of axial water-coupling, suggests that the overall fragment size and the FSD range are  
750 the most and the minimal sensitive to the change of decoupling coefficient under radial air-  
751 coupling blasting and axial water-coupling blasting, respectively. Under this situation, the  
752 extent of crack fracture can be easily controlled in blasting with radial air-coupling such that  
753 the formation of smooth excavation surface in controlled blasting can be achieved by adjusting  
754 charge diameter. In comparison, the consumption of explosive can be significantly cut down in  
755 production blasting using the charge configuration of axial water-coupling.



756



757

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Fig. 17 Variations of fragment parameters with the increase of decoupling ratio: (a)  $\mu$ ; (b)  $\sigma$

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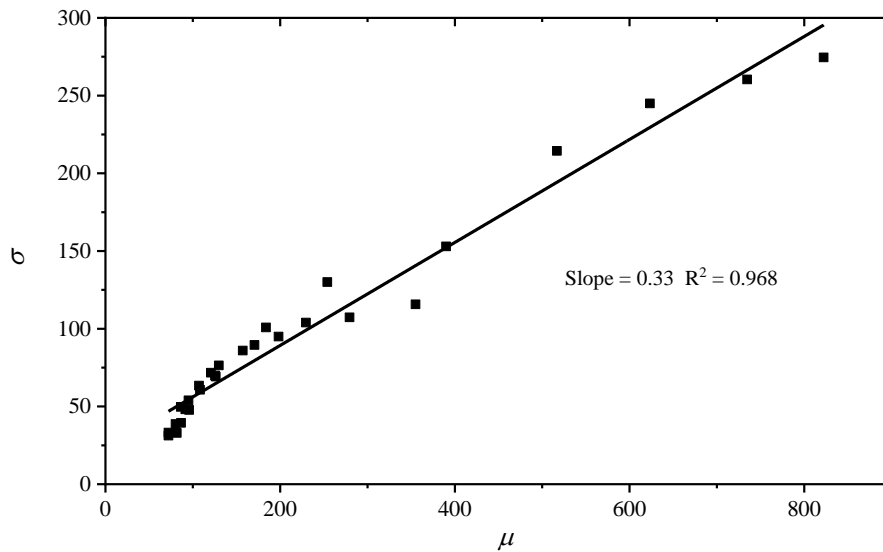
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764

The fragment size and FSD range also show a linear relationship, and the linear fitting line of  $\mu$  vs.  $\sigma$  is plotted in Fig. 18. This linear correlation suggests that the distribution range of fragment size broadens with the increase of average fragment size and can be explained as follows: with the increase of decoupling ratio, altering water-coupling to air-coupling or adjusting axial decoupling to radial decoupling, the explosion energy transmitted from explosive to rock mass decreases, which consequently lead to the creation of larger fragments.



765 Due to the increase in the overall fragment size, the difference between oversize fragments and  
766 small or fine particles gets larger, which eventually gives rise to the formation of a broader  
767 FSD range. The strong correlation in Fig. 18 indicates that both the parameters of  $\mu$  and  $\sigma$  can  
768 serve as valuable indicators of fragmentation efficiency. The smaller values of  $\mu$  and  $\sigma$  imply  
769 the better performance of rock fragmentation in decoupling charge blasting.



770

771 Fig. 18 Correlations between the fragment size and FSD range

## 772 5. Conclusions

773 In this study, the rock fragmentation induced by decoupled charge blasting is  
774 systematically investigated with the changes in decoupling ratio, coupling medium and  
775 decoupled charge mode by combining finite element simulation and image processing. Based  
776 on the numerical findings and data analysis, the following conclusions can be drawn:

777 Parameters for rock, explosive and coupling materials in numerical modelling are  
778 determined based on basic rock mechanical parameter, theoretical calculation and reference,  
779 and the currently developed numerical model is suitable and applicable for modelling rock  
780 fragmentation induced by decoupled charge blasting using air-coupling and water-coupling  
781 with free surfaces. The fracture networks in simulation are obtained by blanking the damaged  
782 elements whose damage level is over the threshold of crack formation, and the rationality of

783 this method is verified by comparing the simulated crack pattern and experimental fragment  
784 morphology.

785 In blasting with radial air-coupling, the rock fracturing varies from radiation-shape  
786 fracture pattern to massively developed rock cracks with the decreasing of decoupling ratio,  
787 whereas 3D cracking is the main fracturing form in water-coupling and axial decoupling blasts.  
788 The blast-induced rock fragmentation becomes finer and the FSD range gets narrower with the  
789 decrease of decoupling ratio. Meanwhile, smaller fragment sizes and narrower FSD spans are  
790 formed when changing coupling material from air to water and altering radial decoupling to  
791 axial decoupling. The overall fragment size and the FSD range have the highest and the  
792 minimal sensitivity to the change of decoupling coefficient under radial air-coupling blasting  
793 and axial water-coupling blasting, respectively. Coarser fragments lead to a broader FSD range.  
794 The strong correlation between the fragment size and FSD range highlights that the parameters  
795 of  $\mu$  and  $\sigma$  can serve as valuable indicators of fragmenting efficiency.

## 796 **CRedit authorship contribution statement**

797 **Xudong Li**: Conceptualization, Investigation, Writing - Original Draft. **Kewei Liu**:  
798 Supervision, Methodology, Writing - review & editing. **Yanyan Sha**: Supervision, Writing -  
799 review & editing. **Jiacai Yang**: Validation. **Ruitao Song**: Writing – review & editing.

## 800 **Acknowledgments**

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802 Foundation of China under Grant no. 51974360 for carrying out this research work.

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