

## FIRE-RESISTANCE

## OF GLUE-

LAMINATED

## TIMBER

ABSTRACT
Wood is becoming an increasingly popular material for construction of high-rise buildings. However, it has a bad reputation for not being a fire-safe alternative. But is this reputation rooted in truth or mostly due to negative public perception? How does glue-laminated timber compare to traditional materials like concrete and steel when considering fire-safety, economic and environmental factors?

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## Introduction

The use of timber and glulam (glue laminated timber) has, in recent years, become increasingly popular in construction of tall buildings. It offers a sustainable and environmentally friendly alternative to steel and concrete in construction and is also renewable to a degree that the others is not. Due to the lower cost of materials and possibility for offsite prefabrication of elements, it is also a time-and cost-efficient alternative to more traditional construction methods for high-rise buildings.

Timber tends to have a bad reputation when it comes to fire safety in buildings, however, this is mostly due to public perception. Although traditional materials like steel and concrete are fireproof, meaning they do not catch fire, they are not fully fire resistant, meaning a lot of its structural strength is lost during a fire. This fact coupled with the knowledge that its usually the contents (furniture, walls, flooring) of the building that contribute the most to the danger of a fire rather than the structure of the building itself, means that the focus should be on designing a firesafe building instead of one that is fireproof. During a buildingfire, the average temperature reached is between $680^{\circ} \mathrm{C}$ and $900^{\circ} \mathrm{C}$. A concrete structure is subject to heavy spalling, even at lower temperatures, and shows a significant reduction in strength at around $650^{\circ} \mathrm{C}$ [1], depending on aggregates used. Tests done for steel show that about $90 \%$ of the strength is lost if exposed to $750^{\circ} \mathrm{C}$ for 30 minutes, while timber has a strength loss of only $25 \%$ at the same temperature. One reason for the huge difference in strength-loss can be attributed to the Charing that occurs when wood burns, giving the structural element a natural insulation against the rising temperature [2].

It is easy to see why timber could be a good choice of material when designing a high-rise building. In this thesis, we will make a review of the techniques used for calculating and ensuring the fire safety of glue-laminated timber elements and design a building of 7 floors, with dimensioning for fire safety in R90 using a structure made from glue-laminated timber. For simplification the joints between structural elements is not considered in this thesis, but should normally get special attention as it is one of the main failure points of a timber structure during a fire [3]. A comparison of prize and $\mathrm{CO}_{2}$-emmissions between the same structure made from glue-laminated wood, steel and concrete will also be done.

## 2 Literature review of current fire safety methods and design methods.

When determining the effects of a fire on a structural component made from timber, we first need to find the charring-depth at a given time during the fire-situation. This is done by using the charring-rate multiplied by the number of minutes the structure has been exposed to fire. The element should be divided into two separate categories that have different calculations. For slabs and panels without any cracks or fissures the method used is called one-dimensional. It is one-dimensional as it does not have any exposed corners and only one side is subjected to the fire. For beams and columns or panels with fissures, the twodimensional method is used. In the two-dimensional method the structural element is exposed to fire on two or more sides, causing a rounding off the corners and a faster reduction in cross-section. The method of calculation is similar in both one- and twodimensional cases, but the charring-rate changes.

## 2.1 one-dimensional calculation of fire resistance:

The charring-rate is calculated from the expression:

## $\mathrm{d}_{\text {char }, 0}=\beta_{0} \times \mathrm{t}$

Where " t " is the time since exposure to fire in minutes, and $\beta_{0}$ is the charring-rate. The charring-rate is usually taken as being $0.9 \mathrm{~mm} / \mathrm{min}$ for wood panels with a thickness less than 30 mm , and $0.65 \mathrm{~mm} / \mathrm{min}$ for panels thicker than 30 mm . with a characteristic density of $450 \mathrm{~kg} / \mathrm{m}^{3}$. For wood panels with different density, and thickness less than 20 mm , the charring-rate is calculated as:

$$
\beta_{0, p, t}=\beta_{0} \times k_{p} \times k_{h}
$$

$\mathrm{K}_{\mathrm{p}}=\left(450 / p_{\mathrm{k}}\right)^{1 / 2} \quad$ where $p_{\mathrm{k}}$ is the characteristic density of the wood.
$K_{h}=\left(20 / h_{p}\right)^{1 / 2} \quad$ where $h_{p}$ is the thickness of the panel.

### 2.2 Two-dimensional charring:

In order to simplify the calculation for loss of cross-section with the two-dimensional method, the notional charring depth is used to include the effect of the rounding of corners.
$d_{\text {char }, n}=\beta_{n} \times t$
Where $\beta_{\mathrm{n}}$ is the notional charring rate according to EN 1995-1-2.
$\beta_{\mathrm{n}}=0.7 \mathrm{~mm} / \mathrm{min}$ is commonly used for glue-laminated timber beams and columns. Meaning that after 30 minutes of exposure, 21 mm of cross-section is lost on all exposed sides.

Different densities and species of wood have different charring rates, EN 1995-1-2:2004 use this table for determining the charring rate $\beta_{0}$ and $\beta_{n}$ for glue-laminated timber.

Table 1. charring rates for wood [4]

| Density | $\beta_{0} \mathrm{~mm} / \mathrm{min}$ | $\beta_{\mathrm{n}} \mathrm{mm} / \mathrm{min}$ |
| :---: | :---: | :---: |
| Softwood: <br> Density $\geq 290 \mathrm{~kg} / \mathrm{m}^{3}$ | 0.65 | 0.70 |
| Hardwood: <br> Density $\geq 290 \mathrm{~kg} / \mathrm{m}^{3}$ | 0.65 | 0.70 |
| Hardwood: <br> Density $\geq 450 \mathrm{~kg} / \mathrm{m}^{3}$ | 0.50 | 0.55 |
| Wood Panels with thickness $\leq$ <br> 30 mm | 0.90 | One-dimensional only |
| Wood Panels with thickness $\geq$ <br> 30 mm | 0.70 | One-dimensional only |

### 2.3 Reduced cross-section method

The general method for calculating fire resistance in timber structures is known as the "reduced cross-section method". This is the simplified method for calculating the fire resistance of timber. The method uses the reduction of cross-section of the structural element due to the charring and the thermal effect on the remaining wood to calculate its strength, in ALS (accidental limit state), during a fire.
timber beyond the charring depth is also affected by the heat of the fire, reducing its strength due to decomposing of the timber. It is therefore necessary to calculate an effective cross-section by determining the effective charring depth $d_{\text {ef }}$. This method of calculation is for timber without any fire-protection.
$D_{\text {ef }}=d_{\text {char }, n}+K_{0} \times d_{0}$
$\mathrm{d}_{0}=7.0 \mathrm{~mm}$ (constant)
$\mathrm{K}_{0}$ is determined by the table:
Table 2 Ko for effective depth

| Time in minutes | $\mathrm{K}_{0}$ |
| :---: | :---: |
| $\mathrm{t} \leq 20 \mathrm{~min}$ | $\mathrm{t} / 20$ |
| $\mathrm{t} \geq 20 \mathrm{~min}$ | 1 |

As seen in table 2 , with exposure to a fire for 20 minutes or more $\mathrm{k}_{0}$ should be taken as 1 . meaning that in most cases of fire resistance calculation, the timber structure is affected by a thickness of the charring depth +7 mm on all exposed sides. [4]


Key:
1 Residual cross-section
2 Char layer
3 Notional (equivalent) cross-section
4 Notional char-layer
5 Effective cross-section
6 Zero-strength layer below char-layer

Figure 1 Reduced cross-section method [5]

### 2.4 The reduced properties method.

The reduced properties method uses the reduced cross-section and the strength loss of the material in a fire-situation to calculate the design resistance of a member in ALS. It can be used on rectangular cross-sections exposed on three or more sides and round columns. It is used by calculating a strength modification factor $\mathrm{k}_{\text {mod, fi }}$ instead of effective charring-depth to find the strength of a member. To calculate the strength modification factor for the material these equations are used:
$k_{\text {mod, }, \mathrm{ii}}=1.0-(1 / 200) \times \mathrm{P} / \mathrm{A}_{\mathrm{t}}$ for members in bending.
$k_{\text {mod }, \mathrm{fi}}=1.0-(1 / 125) \times \mathrm{P} / \mathrm{A}_{\mathrm{t}}$ for members in compression.
$\mathrm{k}_{\text {mod, } \mathrm{fi}}=1.0-(1 / 300) \times \mathrm{P} / \mathrm{A}_{\mathrm{t}}$ for members in tension or to calculate modulus of elasticity.

Where $\mathrm{P}=$ perimeter of the residual cross-section and $\mathrm{A}_{\mathrm{t}}=$ area of the residual cross-section.

## 3 Protection and Cladding

In members protected by insulation or gypsum boards, the charring rate, immediately after failure of the protection, is exceedingly high until a charring depth of 25 mm is reached. After this initial charring it slows down to the notional charring rates for timber. This is especially important when calculating the fire resistance of walls and floors since they are usually clad with gypsum or another type of fire protection. The cross section of floor joists and wall studs is also smaller than most beams and columns and will usually fail before reaching a protective charring depth of 25 mm . [6]

A timber element can start charring due to an increase in heat before complete failure of the protection. There is no good way of calculating the real failure time of the protection, but it has been determined through experimentation with specific types of protection and methods of fastening. the start of charring behind the protection, however, is possible and important to calculate and is typically used as a failure time for protective cladding as well. Failure of protection made from gypsum is often related to dehydration of the panel, glassfiber reinforcement is sometimes used to increase the failure time.

If the protective layer consists of a wood-based panel, the time of start of charring for the undelaying element is found by the expression:
$t_{\mathrm{ch}}=h_{\mathrm{p}} / \beta_{0}$
$t_{\mathrm{ch}}=$ time before start of charring.
$h_{p}=$ thickness of the panel.
$\beta_{0}=$ charring rate of the panel.

With a protective cladding consisting of one layer of type $\mathrm{A}, \mathrm{F}$ or H gypsum, the given expressions can be used for calculation of delayed charring time. Even tough gypsum of type $E, D, R$ and I have better thermal properties, the expressions can be used as a conservative calculation.
$t_{\mathrm{ch}}=2.8 \times h_{\mathrm{p}}-14$ (with filled joints or gaps with a width less than 2 mm )
$t_{c h}=2.8 \times h_{p}-23$ (with unfilled joint or gaps larger than 2 mm )
if two layers of type A or H protective cladding is used, the inner layer should be assumed as having only $50 \%$ fire resistance since it will already be affected by the increase in temperature.

If using different layers, the strongest type should form the outer layer of the protection. In this case the inner layer retains $80 \%$ of its fire resistance [4].

A conservative way of determining the failure time of the protective layer is to calculate it as $t_{\mathrm{f}}=t_{\mathrm{ch}}$. Meaning that a protective layer has failed immediately after the timber behind it starts charring. This method of calculation is relevant for gypsum boards of type $\mathrm{A}, \mathrm{H}$ and wood panels. the failure time of the protective layer is influenced by factors such as vertical or horizontal orientation, size of the panels, and spacing and penetration of screws used for fastening. It has been determined that the minimum penetration depth of screws into the uncharred timber is 10 mm . calculated by the expression:
$I_{f, \text { req }}=h_{p}+d_{\text {char }, 0}+I_{a}$
$h_{p}=$ thickness of the panel.
$d_{\text {char }, 0}=$ charring depth of the timber member.
$I_{a}=10 \mathrm{~mm}$ (minimum depth of screw)
the failure time for a specific protection may be specified by the producer. In the case of $t_{c h} \leq t \leq t_{f}$ meaning that the protective layer fails some-time after the start of charring of the layer behind it. The charring rate can be calculated as $\beta_{0}$ or $\beta_{n}$ multiplied by factor $k_{2}$.
$K_{2}=1-0.018 \times h_{\mathrm{p}}$ (where $h_{\mathrm{p}}$ is the thickness of the gypsum layer. In the case of several layers, it is the thickness of the inner layer of gypsum)
for timber protected with rock fiber with a thickness between 20-45 mm, with a density of $26 \mathrm{~kg} / \mathrm{m}^{3}$ and being able to withstand $1000 \mathrm{C}^{\circ}$, the value for $k_{2}$ can be taken from the table.

Table 3 K2 for protected members.

| Thickness in mm | $K_{2}$ |
| :---: | :---: |
| 20 | 1 |
| $\geq 45$ | 0.6 |

$\mathrm{K}_{2}$ with thicknesses between 20 and 45 mm can be determined by linear interpolation. The expression $t_{\text {ch }}=0.07 \times\left(h_{\text {ins }}-20\right) \times\left(p_{\text {ins }}\right)^{1 / 2}$ can be used to calculate the charring time of timber protected by rock-fiber [4]. Where $h_{\text {ins }}$ is the thickness of the insulation, and $p_{\text {ins }}$ is the density.

After the failure of the protection, $t_{\mathrm{f}} \leq t \leq t_{\mathrm{a}}$ where $t_{\mathrm{a}}$ is the time limit, the charring-rate can be calculated by multiplying $\beta_{0}$ or $\beta_{n}$ with a factor $k_{3}=2$. When $t \geq t_{\mathrm{a}}$ the standard charringrate, $\beta_{0}$ or $\beta_{n}$, is used.

In the case of $t_{\mathrm{ch}}=t_{\mathrm{f}}$, as used with wood-panels and gypsum protection, $t_{\mathrm{a}}$ can be calculated by the expressions:
$t_{\mathrm{a}}=$ minimum value of $\left(2 \times t_{\mathrm{f}}\right)$ or $\left(25 / k_{3} \times \beta_{\mathrm{n}}+t_{\mathrm{f}}\right)$
for $t_{\mathrm{ch}}<t_{\mathrm{f}}$ :
$t_{\mathrm{a}}=\left(25-\left(t_{f}-t_{c h}\right) \times k_{2} \beta_{n}\right) /\left(k_{3} \beta_{\mathrm{n}}\right)+t_{f}$
$t_{a}$ being the time it takes for a protective charr-layer of 25 mm to build up, thus slowing down the charring-rate.

As walls and floors usually consist of several layers of wood panels, gypsum and insulation, it is necessary to calculate a sum fire-resistance for the element. This can be done by calculating the start of charring for the load-bearing structure, usually the studs in a wall or joists in a floor. the charring rate of the structure must also be determined, both before and after the failure of the protection.

## example:

a wall structure made with 20 mm timber CLT panel with density of $450 \mathrm{~kg} / \mathrm{m}^{3}$ and one layer of 15 mm gypsum panel of type F . the voids in the wall is filled with rock-wool insulation with a density $\geq 26 \mathrm{~kg} / \mathrm{m}^{3}$. The studs are made from hardwood with a cross section of $48 \times 148 \mathrm{~mm}$ and a charring rate of $\beta_{\mathrm{n}}=0.7 \mathrm{~mm} / \mathrm{min}, \beta_{0}=0.65 \mathrm{~mm} / \mathrm{min}$.

### 3.1 Method 1: Calculation of protection time

$t_{f, \text { panel }}=t_{\text {ch, panel }}=h_{p} / \beta_{0}=20 / 0.9=22 \mathrm{~min}$
$t_{f, \text { gypsum }}=t_{c h, \text { gypsum }}=2.8 \times h_{p}-14=28 \mathrm{~min}$
$t_{\mathrm{ch}, \text { stud }}=22+28=50$ minutes.
immediately after failure of the gypsum, $\mathrm{t}=50$ minutes, the charring rate is:

$$
\beta_{\mathrm{n}} \times k_{3}=0.7 \times 2.0=1.4 \mathrm{~mm} / \mathrm{min}
$$

$t_{\mathrm{a}}=\min (2 \times 50)$ or $(25 / 2 \times 0.7+50)$
$t_{\mathrm{a}}=17.8+50=67.8$ minutes from the start of the fire. Meaning that the full insulation effect from the char at 25 mm thickness will occur 67.8 minutes after the start of the fire. Since this is a calculation of fire-resistance on a wall-stud, it is likely to fail before reaching a char level of 25 mm . it would be a good idea to add a layer of gypsum on this wall if it is for a high-rise building.

### 3.2 Method 2: components additive method

The components additive method uses the sum protection time of all the layers, $t_{\text {ch }}=\sum t_{\text {prot }}$, to calculate the charring time for a member. [6]
layer 1.20 mm wood panel.
$t_{\text {prot }, 0,1}=\min$ of $\left(23 \times\left(h_{1} / 20\right)^{1.1}\right.$ or $h_{1} / \beta_{0}=23$
$k_{\text {pos, exp, } 1}=1.0$ (no preceding layer)
$k_{\text {pos, unexp, } 1}=1.0$ (backed by gypsum)
$k_{\mathrm{j}, 1}=1.0$ (joint coefficient, backed by gypsum)
$\Delta t_{1}=0$ (no preceding layer)
$t_{\text {prot }, 1}=\left(t_{\text {prot, }, 0,1} \times k_{\text {pos, }}\right.$ exp, $\left.1 \times k_{\text {pos, unep, } 1}+\Delta t\right) \times k_{\mathrm{j}, 1}=23$ minutes
Layer 2.15 mm gypsum type F .
$t_{\text {prot }, 0,2}=\min$ of $\left(24 \times\left(h_{2} / 15\right)^{1.4}\right)$ or $\left(30 \times\left(h_{2} / 15\right)^{1.2}\right)=24$
$k_{\text {pos, exp }, 2}=0.5 \times\left(t_{\text {ins }, 0,2} / \sum t_{\text {prot, } n-1}\right)^{1 / 2}=0.51$
$k_{\text {pos, unexp, } 2}=1.0$
$k_{\mathrm{j}, 2}=1.0$
$\Delta t_{2}=0.22 \times t_{\text {prot, } n-1}-0.1 \times t_{\text {ins, } 2}+4.7=7.36$
$t_{\text {prot, } 2}=\left(t_{\text {prot, }, 0,2} \times k_{\text {pos, exp }, 2} \times k_{\text {pos, unep, } 2}+\Delta t\right) \times k_{\mathrm{j}, 2}=19.6 \mathrm{~min}$
$t_{\mathrm{ch}}=42.6 \mathrm{~min}$
the stud will start charring after 42.6 minutes.
the charring-rate is then calculated the same way as with method 1.

### 3.3 Charring rates for studs and joists

There is a simplification done in the above calculation, as the voids in the wall is filled with insulation the charring would mostly be concentrated to the narrow side of the studs. due to the thermal heat-flux around the sides of the insulation there will be extensive rounding of the corners, and no consolidation of the charring rate due to an insulating charr-layer should be considered. For this to be true, it would have to be insured that the insulating batts are tightly fitted to the voids and fastened properly, this is commonly done by oversizing the insulation and mechanically fixing it to the studs with wire. Mineral wool insulation has the best properties for reducing charring on the sides of the studs after the failure of the protective cladding because it retains its shape, even during exposure to high temperatures. the charring rate can be calculated by the expression: $\beta_{n}=\beta_{0} \times k_{s} \times k_{n} \times k_{p}$
$k_{s}$ is related to the width of the stud, for insulation with stone-wool with a density of 26
$\mathrm{kg} / \mathrm{m}^{3}$ it can be found by:

Table 4. $K_{s}$ for voids with insulation.

| Width of stud or joist in mm | $k_{\mathrm{s}}$ |
| :---: | :---: |
| $38 \leq \mathrm{b} \leq 90$ | $0,00023 \times \mathrm{b}^{2}-0,045 \times \mathrm{b}+3,19$ |
| $\mathrm{~b} \geq 90$ | 1 |

$K_{\mathrm{n}}$ is a conversion of charring depth from the actual rounding of corners to an equivalent rectangular shape used to simplify the expression:

Table 5. $K_{n}$ for protected members

| Width of stud or joist in mm | $k_{\mathrm{n}}$ |
| :---: | :---: |
| $\mathrm{b} \leq 60$ | 1.5 |
| $\mathrm{~b} \geq 60$ | 1.25 |

$K_{\mathrm{p}}$ is dependent on protection given by the cladding at different stages:

Table $6 K_{p}$ for protected members

| Protection stage | $k_{\mathrm{p}}$ |
| :---: | :---: |
| Un-protected structure | Equal to $k_{1}$ |
| Protected but charring $t_{\mathrm{ch}} \leq t_{\mathrm{f}}$ | Equal to $k_{2}$ |
| After protection fails $t \geq t_{\mathrm{f}}$ | Equal to $k_{3}$ |

Using this information, assuming a stud width of 48 mm and the protection to fail as soon as charring of the wood behind it we get the values:
$\beta_{0}=0.65 \mathrm{~mm}$
$k_{s}=1.63$
$k_{\mathrm{n}}=1.5$
$k_{\mathrm{p}}=k_{3}=2.0$

## $\beta_{\mathrm{n}}=3.18 \mathrm{~mm} / \mathrm{min}$

previous charring-rate calculated without considering the insulation was $\beta_{\mathrm{n}}=1.4 \mathrm{~mm} / \mathrm{min}$. The new charring-rate is considerably higher than the value without rock-wool, however only for the narrow face of the stud instead of on all sides. the effective charring-depth can then be calculated as $d_{\text {eff }}=d_{\text {char, } n}+d_{0}$ where $d_{0}$ is found using:

Table 7 do for joists

| Exposed side | $d_{0}$ |
| :---: | :---: |
| In tension | $13.5+0.1 \times \mathrm{h}$ |
| In compression | $21.5+0.1 \times \mathrm{h}$ |

For floor joists with a height $\geq 95 \mathrm{~mm}$ and width $\geq 38 \mathrm{~mm}$.

Table 8 do for studs

| Exposure | Limitations mm | $d_{0} \mathrm{~mm}$ |
| :---: | :---: | :---: |
| Fire on one side. | $\mathrm{b} \geq 38$ |  |
| stiff $y$-y axis. | $\mathrm{h} \geq 95$ | $13.5+0.1 \times h$ |
| Fire on one side. | $\mathrm{b} \geq 38$ |  |
| weak $x$-x axis. | $\mathrm{h} \geq 95$ | $17+0.25 \times h$ |
| Fire on both sides. | $\mathrm{b} \geq 38$ |  |
| stiff $y$-y axis. | $\mathrm{h}=140$ | 25 |
| Fire on both sides. | $\mathrm{b} \geq 38$ |  |
| weak $x-x$ axis. | $\mathrm{h}=140$ | 44 |

For wall studs. [6]

### 3.4 Origin and use of the components-additive method

There is a difference in the charring time of 7.4 minutes between the two methods. The components additive method being the more conservative. This basic method for calculating the charring time of walls and floors can be found in annex E in Eurocode EN 1995-1-2 and is called the separating function. It relies on the use of tabulated values to determine the coefficient values needed to calculate the fire resistance. The components additive method is meant to offer a more precise way of calculating the fire resistance of a complex structure,
built up with different layers of protection and aesthetic panels. It is based on the separating function, which uses tabulated values found by testing, but instead offers general equations to calculate each coefficient. These equations have been formed by a finite number of tests done on both small- and full-scale fire-simulations. The tests were done on unloaded specimen, but the calculation should be accurate for loadbearing structures as well. By considering the fire resistance of each layer, $t_{\text {ins }}$ and $t_{\text {prot }}$ as the basic insulation and protection value, together with the interaction of the preceding and backing layer by using the position coefficients $k_{\text {pos, exp }}$ and $k_{\text {pos, unexp. }}$. It also considers the effect from different types of joints and their backing with the coefficient $k_{\mathrm{j}}$, and the correction time for the insulation or protection as $\Delta t$ for layers protected by type F gypsum.

This method has been extensively tested using the Eurocode testing standards and found to be a precise, versatile and safe way of calculating the fire resistance of complex structures consisting of an infinite number of layers.

## 4 design strength during a fire-situation

The calculation for design strength is done the same way in a fire-situation as in ultimatelimit state but with different safety-coefficients [4].
$f_{d, f i}=k_{\text {mod }, f i} \times \mathrm{f}_{20} / Y_{\mathrm{m}, \mathrm{fi}}$
$s_{d, f i}=k_{m o d, f i} \times s_{20} / Y_{m, f i}$
$f_{d, f i}$ is the design strength during a fire.
$f_{20}$ is the strength fractile $20 \%$ of a strength property at normal temperature, calculated as $f_{20}=f_{k} \times k_{f i}$.
$S_{d, f i}$ is design stiffness properties, modulus of elasticity or shear modulus.
$s_{20}$ is the strength fractile $20 \%$, calculated as $s_{20}=s_{0.5} \times k_{f i}$.
$K_{\text {mod, } f i}=1.0$ for glue-laminated wood in a fire-situation.
$Y_{m, f i}=1.0$ in a fire situation.
$k_{f i}=1.15$ for glue-laminated timber.

For a structural element to be suitable in a fire-situation, the following expression must be satisfied: $E_{d, f i} \leq R_{d, t, f i}$. Meaning that the design effect on the structure during a fire is smaller than the resistance of the structural element at the required time of fire resistance.
$E_{d, f i}$ can be simplified to, $E_{d, f i}=E_{d} \times \eta_{f i}$
$\eta_{f i}=$ the smaller value of $\left(G_{k}+\Psi_{f i} \times Q_{k, 1}\right) /\left(Y_{G} \times G_{k}+Y_{Q, 1} \times Q_{k, 1}\right)$ or
$\left(G_{k}+\Psi_{f i} \times Q_{k, 1}\right) /\left(\varepsilon^{\times} Y_{G} \times G_{k}+Y_{Q, 1} \times Q_{k, 1}\right)$
referring to load combinations from (6.10 a) and (6.10 b) in EN 1990:2002.
Equations ( 6.10 a) and ( 6.10 b ) can also be used directly to calculate design-loads by using reduction-factors for ALS design.

Strength calculations and dimensioning of construction elements will be discussed in greater detail in chapter 9-members in accidental limit state.

## 5 Factors and design considerations that may influence fire resistance.

There are several factors that influence the charring rate and fire resistance of timber. These include the type of lamination used, if its glue-laminated, what type of adhesive is used and how fire resilient is it? as well as the direction of the grain and density of the wood. The design detailing of elements can also have a large impact on fire resistance. Especially with regards to floors, ceilings and walls, where there can be huge variation in build-up of the protective cladding and structure. Even if the walls and floors are not part of the loadbearing structure, they help dividing a building into fireproof cells to prevent the spread of a fire. In order to design a building that maximizes fire-safety in the most economical and practical way possible it is important to have a good understanding of the factors that affects fire-resistance. A good way to get an understanding of these influencing factors would be Studying tests done on different encapsulation methods, adhesives and external factors. Even though there can be a lot of variation on how the tests are performed with regards to information about wood density, moisture content and the type of fire-test used, they can still give useful insight and guidelines into how we should- or should-not design a building for fire safety.

### 5.1 Considering different encapsulation methods.

Tests to determine the effect of encapsulation to increase the fire resistance has showed the effects of including an airgap between the protective gypsum-boards and the structural element. Initially the airgap has a positive impact on the rise of temperature of the wood due to the insulating effect of air. However, as the protective layer fails, the charring of the
timber is much greater than if the gypsum had been mounted directly on the wood. This might be due to a greater surface of timber being exposed to hot gasses when a crack eventually forms in the gypsum [7]. Due to the high standard for fire-safety, a fire resistance level of R90 being enforced on buildings up to 30 meters high, and the probability of the protection to fail before 90 minutes of exposure. It can be concluded that an unfilled airgap between the protective layer and the timber should be avoided.

A gap between the protective layer and the timber, filled with rock-wool or glass-wool, however proved to have a positive effect on the charring rate even after the failure of the gypsum protection. The increased thermal properties from the layer of insulation, and the elimination of hot gasses affecting the timber after failure of the protection resulted in a delayed charring time, $t_{c h}$. This method of encapsulation has also shown to greatly increased the failure time of the protection. From $t_{f}=27.7$ minutes with gypsum mounted directly on the wood, $t_{\mathrm{f}}=26.7 \mathrm{~min}$ with a 100 mm airgap (with an increased Charing-rate compared to directly mounted gypsum), to $t_{f}=78.6 \mathrm{~min}$ for gypsum with 100 mm of rock-wool insulation. With two layers of gypsum the failure time was found to be 70.8 min , which is more than double the failure time found for one layer of gypsum in the same test. these tests were done with 16 mm type X gypsum, which is equivalent to type F in terms of fire resistance. Failure of the protective cladding was considered as the time of charring of the wood behind it which is the criteria used according to EN 1995-1-2, $t_{f}=t_{c h}$ [7]. although this was a study done on small-scale specimen, the results correspond well with those from larger scale testing of fire protection [8], and calculations made according to the standard.

### 5.2 Adhesives and finger-joints

The methods used for calculating fire resistance is the same for solid timber as for gluelaminated timber. However, with a load bearing structure made from glue-laminated wood, one should consider the effects that the degradation of the adhesive both due to sunlight and heat from a fire-situation may have on strength. As the effect of adhesive strength and the mechanical strength of finger joints are closely related, they should be considered together. The current European standard for testing adhesives is a loaded specimen being
heated for two weeks at $70 \mathrm{C}^{\circ}$, which might be okay to check for degradation due to heating from sunlight, but not applicable in a fire situation. Even though Timber has naturally good thermal properties tests show that the temperature of timber reaches $360^{\circ} \mathrm{C}$ at the effective charr-depth $\left(d_{\text {eff }}\right)$, and $100^{\circ} \mathrm{C}$ at 15 mm from $d_{\text {eff }}[9]$, during a fire. Meaning the standard test parameters are not satisfactory to check suitability of an adhesive during a fire [10]. There are two main aspects to take into consideration when deciding if an adhesive is suitable.

1. what is the limiting factor, the strength loss of the adhesive, or the timber during a fire situation?
2. Does the charr-layer fall of when it reaches the glue-line (de-lamination)?

The ability of an adhesive to resist against heat is most important for beams in bending. Since the stress distribution for shear force is mostly towards the center of the beam, the fire resistance of the adhesive is less important for the timber element to resist shear force. bending moment, however, has a stress distribution towards the over-and under-side of the beam, meaning that a worse performing adhesive can have a large impact on its ability to resist bending. Research also show that adhesive strength has the largest impact on strength for members in tension, which is usually found on the underside of beams in bending [10].

Since the fire resistance of timber is highly dependent on it forming an insulating char-layer of 25 mm in order to reduce the rising temperature in a member and reduce the charring rate. It is important that the charr-layer stay in place even after reaching the glue-line between lamination layers, a failure to achieve this would result in de-lamination of the cross-section. An adhesive that allows the char to simply fall of will not have a chance to reduce the charring-rate and is therefore not satisfactory when designing a building with a high focus on fire resistance. A lamination thickness of 45 mm or more per layer will ensure that the insulating char layer of minimum 26 mm is maintained without excessive spalling when the char-depth reaches the glue-line. [11]

The National Standard specifies phenol-formaldehyde and amino-plastic type 1, as suitable adhesives for laminated structural elements. According to the standard no testing at elevated temperatures are required for these types of adhesives [6]. In order to cut cost and lower production time on structural elements, adhesives based on melamine-ureaformaldehyde and one-component polyurethane have been used in recent years. these are classified as type 1 adhesives, and therefore approved according to EN-301 and EN-15425. Polyurethane based adhesives have the added benefit of being more environmentally friendly than previously used adhesives as well. Research has been done at ETH Zurich [10] involving one melamine-urea- formaldehyde and four different one-component polyurethane adhesives to determine their strength in a fire-situation. In their research they tested the tensile strength of a finger-joint with different types of adhesives at temperatures up to $140^{\circ} \mathrm{C}$. They also included a control experiment with a solid, unjointed member at elevated temperature as a comparison to see how much the adhesive was compromised relative to the wood itself. The test results can be found in table 9 .

Table 9 performance of adhesives

| temperature | Control | $\mathrm{p}-1$ | $\mathrm{p}-2$ | $\mathrm{p}-3$ | $\mathrm{p}-4$ | $\mathrm{~m}-1$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 20 | 42.9 | 35.6 | 32.0 | 31.7 | 40.0 | 35.4 |
| 60 | 35.4 | 25.1 | 26.3 | 25.5 | 33.8 | 35.1 |
| 100 | 31.2 | 17.5 | 16.2 | 18.1 | 25.1 | 30.2 |
| 140 | 25.4 | 14.1 | 20.4 | 16.9 | 23.4 | 21.7 |
| $\Delta \mathrm{~F}_{140^{\circ} \mathrm{C}}$ | - | 11.3 | 5.0 | 8.5 | 2.0 | 3.7 |

Table 9 lists the temperature in Celsius. the control-specimen is timber without any joint. p-1 to $\mathrm{p}-4$ being the different one-component polyurethane based adhesives tested, and $\mathrm{m}-1$ is based on melamine-urea-formaldehyde. All the tests are for tensile forces in $\mathrm{N} / \mathrm{mm}^{2}$. $\Delta \mathrm{F}_{140}{ }^{\circ} \mathrm{C}$ lists the difference in tensile strength between the control specimen and the different adhesives at $140^{\circ} \mathrm{C}$ in $\mathrm{N} / \mathrm{mm}^{2}$. As can be seen from the table, the adhesive listed as $\mathrm{p}-4$ had the least strength loss at $140^{\circ} \mathrm{C}$, losing only $2.0 \mathrm{~N} / \mathrm{mm}^{2}$ of tensile strength when compared with the control-specimen. This makes it suitable for use in glue-laminated timber structures with high requirements for fire resistance. The chemical structure of the
adhesives was not specified in the test. large variations in temperature-resistance were observed between the different adhesives of the same type. Further testing is therefore necessary to decide the best chemical structure for fire safety, but an adhesive based on polyurethan can be satisfactory. Even though the adhesive did not decompose significantly compared to the wood, it is advised to avoid placing finger-joints near the point of maximum bending moment on a beam due to possible deficiency or variation in quality of the joint.

### 5.3 Density, moisture content and direction of the grain

The density of the wood could influence the charring rate. Even though it is widely accepted, and the table on charring-rates from EN 1995-1-2 states that a higher density timber has a lower charring-rate, there is contradicting evidence that support the case for using both lowand high-density timber for structural elements. Some tests done on correlation between charring-rate and density found that a higher density has a huge impact on charring rates. Logically a structural element with a higher density has more mass to decompose during a fire. However, many tests have found there to be little correlation between density and charring-rates, or a correlation only in specific circumstances like moisture-content or specific ranges of density in certain types of wood. The argument for low density timber being that the lower thermal conductivity works to keep the internal temperature of the element lower [9]. All tests done concluded that the charring-rates from the standard is conservative.

A higher moisture level will lead to lower charring-rates. In structural elements the moisture content is typically around $12-16 \%$. Most of the tests done on timber during a fire is within this moisture range. Since a higher moisture content can lead to lower structural strength and a faster degradation of the timber it should not be increased for the purpose of fire resistance.

Test done on the effect of grain-direction also show contradictory evidence, with some tests concluding that the charring rate is highest along the grain direction and others finding that the grain direction is of little importance [9]. Timber is the strongest in both tension and compression parallel to the grain, with a loss of strength of more than $87 \%$ with forces
perpendicular to the grain, calculated from table 1 in NS-EN 338:2009. Due to the huge strength-loss as a result of grain direction, Any structural element should be constructed to ensure that the timber is loaded in its strongest direction.

## 6 Load calculation



Figure 2 overview of the load-bearing structure
In this thesis I will design and dimension the loadbearing structure of a building according to calculations from the standard. The external forces taken into consideration will be snow load and wind load, the effect of seismic activity will not be calculated. Considering a building with a height of 29 meters, the load bearing structure needs to be fire-resistant in R90, meaning that it can burn for 90 minutes without collapsing. The building will have a perfectly square cross-section with sides of 30 meters and an exterior covered with a glass facade. It will have 7 floors, each being 4 meters high except for the top floor which has a height of 5 meters, giving the building a total height of 29 meters. The walls dividing the rooms at each floor will not be loadbearing but will function as a fire-barrier to divide the
building into fire-cells, therefore they also need to be fire-resistant. The loadbearing structure will be made from glue-laminated beams and columns without any protective cladding. It also has loadbearing shear-walls on each side as well as the elevatorshaft/stairwell to resist against wind-load and seismic activity. All beams are supported against torsional buckling by the floor. All elements made from glue-laminated timber will be constructed by using one-component polyurethane based adhesives. The building components would be prefabricated in a factory before assembly at the construction-site. The first floor will function as a reception and cafeteria. $2^{\text {nd }}-6^{\text {th }}$ floor will have offices and $7^{\text {th }}$ Floor will be reserved for conference-rooms.
the building will be located next to scandic forum hotel in Tjensvoll, Stavanger with a height of 50 meters above sea level. Located 8 km from the coast with a terrain category III and being 2.5 km from terrain category II. The terrain surrounding the building is mostly flat.

### 6.1 Snow load

Using formulas and statistics found in NS EN 1991-1-3 2003+NA 2008. [12]
$S=n_{i} \times c_{e} \times c_{t} \times s_{k}$
$n_{i}$ is a shape coefficient regarding the angle of the roof, in this case the angle is $0^{\circ}$ which means $n_{i}=0.8$.
$C_{e}$ is an exposure coefficient and should be considered as 1.0 unless otherwise specified.
$c_{t}$ is a thermal coefficient which should be considered as 1.0.
$s_{k}$ is the characteristic snow load on the ground found in table NA.4.1 (901) for Stavanger it is specified as $1.5 \mathrm{kN} / \mathrm{m}^{2}$ under a height of 150 meters above sea level.
for our building the snow load on the roof is:
$s=0.8 \times 1.0 \times 1.0 \times 1.5=1.2 \mathrm{kN} / \mathrm{m}^{2}$
with a surface area of $900 \mathrm{~m}^{2}$ the total snow-load on the roof is 1080 kN .

### 6.2 Wind Ioad

using the simplified method of calculation from NS EN 1991-1-4 2005+NA 2009. [13]
$q_{(z), p}=k_{1} \times k_{2} \times k_{3} \times c^{2}{ }_{\text {dir }} \times c^{2}{ }_{\text {alt }} \times c^{2}$ season $\times c^{2}{ }_{\text {prob. }} \times q_{p, 0, z}$
$k_{1}$ is an orography factor considering the terrain. Set to 1.0
$k_{2}$ is a factor that takes steep terrain into account. Set to 1.0
$k_{3}$ is a factor considering the change of terrain, using values found in table v. 1 of the standard and $\Delta \mathrm{n}_{\mathrm{BA}}=1$.
$K_{3}=1.05$.
$c^{2}$ dir $/ c^{2}{ }_{\text {alt }} / c^{2}$ season $/ c^{2}{ }_{\text {prob }}$ are factors considering direction, altitude, season and the probability of wind strength in the next 50 years, they will all be considered as 1.0.
$V_{b, 0}=26 \mathrm{~m} / \mathrm{s}$ (value from table NA 4. (901.1)) is the basic wind velocity in Stavanger.
$q_{p, 0, z}$ with a building height of 29 meters and $v_{b, 0}=26 \mathrm{~m} / \mathrm{s}$ is $1.1 \mathrm{kN} / \mathrm{m}^{2}$ using fig. v. 1 c to calculate.
$q_{p, 0, z}=1.1 \mathrm{kN} / \mathrm{m}^{2}$
$q_{(z), p}=1.05 \times 1.1=1.16 \mathrm{kN} / \mathrm{m}^{2}$

To find the wind pressure working on the building we will simplify the calculations by assuming the wind will hit with $90^{\circ}$ on the sides being 30 meters wide.

Table 10 wind load on each side of the building

| side | $\mathrm{C}_{\mathrm{pe}, 10}$ | $\mathrm{C}_{\mathrm{pe}, 1}$ | Area $\mathrm{m}^{2}$ | $q_{(z), p}$ | Total wind force kN |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| A | -1.2 | -1.4 | 180 | 1.16 | -250.6 |  |  |  |  |
| B | -0.8 | -1.1 | 720 | 1.16 | -668.2 |  |  |  |  |
| D | 0.8 | 1.0 | 900 | 1.16 | 835.2 |  |  |  |  |
| E | -0.5 |  |  |  |  |  | 900 | 1.16 | -522 |



Figure 3 wind load on the building as seen from above.
using the self-weight of the building calculated in chapter 7, the building's ability to resist overturning was calculated: $\mathrm{M}_{\mathrm{w}}=(835.2+522) \mathrm{kN} \times 15 \mathrm{~m}=20358 \mathrm{kNm}$ is the moment on the building from wind-load.
$M_{b}=7 \times(1.47 \times 30 \times 30) \mathrm{kN} \times 15 \mathrm{~m}=138915 \mathrm{kNm}$ is the moment just from the self-weight of the floor.
$M_{b}=138915 \mathrm{kNm}>\mathrm{M}_{\mathrm{w}}=20358 \mathrm{kNm}$-> the building is safe from overturning.

## 6.3 imposed load

This is a building with offices and conference rooms. The values for imposed load are taken from table NA. 6.1 and NA. 6.2 in NS-EN 1991.1.1:2002/NA:2008.
floors 2-6 contain offices in category B, they have a characteristic imposed load of 3.0 $\mathrm{kN} / \mathrm{m}^{2}$.
$7^{\text {th }}$ floor is reserved for conference rooms, in category C2 with a characteristic imposed load of $4.0 \mathrm{kN} / \mathrm{m}^{2}$.

A reduction factor for the floors assigned to offices can be calculated as: $a_{\mathrm{n}}=2+(n-2) \times \psi_{0} / \mathrm{n}$ with $n$ being the number of consecutive floors of the same category and $\psi_{0}$ being the combination factor for offices.
$\mathrm{n}=4$
$\psi_{0}=0.7$
this reduction-factor is meant to be used when dimensioning the columns on the first floor.

## 7 Design and charring-times for walls and floors

To calculate the self-weight of each floor we first need to design the inner walls and floors. Even though the walls are not loadbearing, they will need to be fireproof in EI90 to make each room and floor function a fire-cell. EI90 means that the wall can be exposed to a fire for 90 minutes without the fire spreading to the unexposed side. Calculations will be done according to the components additive method.

### 7.1 Walls

Layer 1: type F gypsum, 15 mm .
Layer 2: type F gypsum, 15 mm .
Layer 3: CLT plywood, 12 mm .
studs: $148 \times 48 \mathrm{~mm}$ glue-laminated timber (hardwood) with a density $\geq 290 \mathrm{~kg} / \mathrm{m}^{3}$. CC 600 mm .
the voids between studs are filled with mineral wool which we assume is properly fitted. both sides of the walls are built up in the same way to create a fire-cell.

Fire- resistance, Layer 1:

[^0]$k_{\text {pos, }, \text { exp }, 1}=1.0$ (first layer)
$k_{\text {pos,unexp, } 1}=1.0$ (gypsum backing)
$k_{j, 1}=1.0$ (gypsum backing)
$\Delta t=0$ (first layer)
$t_{\text {prot }, 1}=\left(t_{\text {prot }, 0,1} \times k_{\text {pos }, \text { exp }, 1} \times k_{\text {pos }, \text { unexp }, 1}+\Delta t\right) \times k_{j, 1}=\underline{30.0 \mathrm{~min}}$
layer 2:
$t_{\text {prot, } 0,2}=30 \times\left(h_{1} / 15\right)^{1.2}=30.0 \mathrm{~min}$
for $\sum t_{\text {prot }, 1}>t_{\text {prot }, 0,2} / 2 \rightarrow k_{\text {pos }, \text { exp }, 2}=0.5 \times\left(t_{\text {prot }, 0,2} / \sum t_{\text {prot }, 1}\right)^{1 / 2}=0.5 \times(30.0 / 30.0)^{1 / 2}=0.5$
$k_{\text {pos, }, \text { unexp, } 2}=1.0$ (backed by timber)
for $t_{\text {prot }, 0,2} \geq 12->\Delta t=0.22 \times t_{\text {prot }, 1}-0.1 \times t_{\text {prot }, 0,2}+4.7=8.3 \mathrm{~min}$
$k_{j, 2}=1.0$ (backed by timber)
$t_{\text {prot }, 2}=(30.0 \times 0.5 \times 1.0+8.3) \times 1.0=\underline{23.3 \mathrm{~min}}$
layer 3:
$t_{\text {ins }, 0,3}=19 \times\left(h_{3} / 20\right)^{1.4}<h_{4} / \beta_{0}=12 / 0.9=13.3 \mathrm{~min}$
for $\sum t_{\text {prot }, 1,2}>t_{\text {ins }, 0,3} / 2->k_{\text {pos, }, \text { exp }, 3}=0.5 \times\left(t_{\text {ins }, 0,3} / \sum t_{\text {prot }, 1,2}\right)^{1 / 2}=0.5 \times(13.3 / 53.3)^{1 / 2}=0.25$
$k_{\text {pos, } \text {, }}$ nexp,, $3=0.5 \times h_{3}{ }^{0.15}=0.72$ (backed by insulation)
for $t_{\text {ins }, 0,3}>12->\Delta t=0.22 \times t_{\text {prot }, 2}-0.1 \times t_{\text {ins }, 0,3}+4.7=8.5 \mathrm{~min}$
$k_{j, 3}=1.0$ (backed by insulation)
$t_{\text {prot }, 3}=(13.3 \times 0.25 \times 0.72+8.5) \times 1.0=\underline{10.89 \mathrm{~min}}$
total time until charring of the studs occur $=\Sigma t_{\text {prot }}=64.19$ minutes.
The voids in the wall are filled with stone-wool, it is assumed that this is properly fitted to the studs. since the wall is non-structural, the stud can burn $2 / 3$ of the way through before we consider the wall as failed. Maximum charring depth is therefore 98.6 mm .
the charring rate can be calculated as $\beta_{n}=\beta_{0} \times k_{s} \times k_{n} \times k_{p}$.
$\beta_{0}=0.65 \mathrm{~mm} / \mathrm{min}$
$k_{s}=0,00023 \times b^{2}-0,045 \times b+3,19=1.56$
\[

$$
\begin{aligned}
& k_{n}=1.5 \\
& k_{p}=k_{3}=2.0
\end{aligned}
$$
\]

$\beta_{\mathrm{n}}=0.65 \times 1.56 \times 1.5 \times 2.0=3.04 \mathrm{~mm} / \mathrm{min}$
The charring time will therefore be $t_{c h, s t u d}=98.6 / 3.04=\underline{32.4} \mathrm{~min}$
the time from the start of fire until failure of the wall is then $t_{f}=64.19+32.4=96.59$ minutes. This satisfies our requirement of EIGO.

### 7.2 Self-weight of the wall

$\mathrm{g}_{\mathrm{q}, \mathrm{k}, \text { panels }}=\left(760 \mathrm{~kg} / \mathrm{m}^{3} \times 0.015 \mathrm{~m} \times 4+290 \mathrm{~kg} / \mathrm{m}^{3} \times 0.012 \times 2\right) \times 9.81 / 1000=0.51 \mathrm{kN} / \mathrm{m}^{2}$.
$\mathrm{g}_{\mathrm{q}, \mathrm{kstuds}}=290 \mathrm{~kg} / \mathrm{m}^{3} \times 0.048 \times 0.148 \mathrm{~m} \times 0.6 / 1 \times 9.81 / 1000=0.012 \mathrm{kN} / \mathrm{m}^{2}$
$\mathrm{g}_{q, \mathrm{k}, \text { ins }}=26 \mathrm{~kg} / \mathrm{m}^{3} \times 0.148 \mathrm{~m} \times 9.81 / 1000=0.04 \mathrm{kN} / \mathrm{m}^{2}$
self-weight of electrical equipment and piping is estimated at $g_{q, k, e x t}=0.05 \mathrm{kN} / \mathrm{m}^{2}$
total self-weight of the wall is then $g_{q, k, w a l l}=0.62 \mathrm{kN} / \mathrm{m}^{2}$

### 7.3 Floors

The construction of this element is different on each side. The floor construction needs to be fire-resistant in REI90, meaning it will both retain its structural integrity and limit the spread of fire for 90 minutes. One side acting as a ceiling for the floor below, and one side acting as a floor. The first calculation for fire resistance will be done by considering the floor as the side exposed to fire.

Layer 1: 30 mm hardwood with density $>290 \mathrm{Kg} / \mathrm{m}^{3}$.
layer 2: 15 mm , type F gypsum.
layer 3: 15 mm , type F gypsum.
the voids in the floor is filled with stone-wool insulation.

Layer 1:
$t_{\text {prot }, 0,1}=30 \times\left(h_{1} / 20\right)^{1.1}<h_{1} / \beta_{0}=30 / 0.70=42.8 \mathrm{~min}$
$k_{\text {pos, }, \text { exp }, 1}=1.0$ (first layer)
$k_{\text {pos, }, \text { unexp, },}=1.0$ (gypsum backing)
$k_{j, 1}=1.0$ (gypsum backing)
$\Delta t=0$ (first layer)
$t_{\text {prot }, 1}=\left(t_{\text {prot }, 0,1} \times k_{\text {pos }, \text { exp }, 1} \times k_{\text {pos, }, \text { nexe }, 1}+\Delta t\right) \times k_{j, 1}=\underline{42.8 \mathrm{~min}}$
Layer 2:
$t_{\text {prot, } 0,2}=30 \times\left(h_{1} / 15\right)^{1.2}=30.0 \mathrm{~min}$
for $\sum t_{\text {prot }, 1}>t_{\text {prot }, 0,2} / 2->k_{\text {pos }, \text { exp }, 2}=0.5 \times\left(t_{\text {prot }, 0,2} / \sum t_{\text {prot }, 1}\right)^{1 / 2}=0.5 \times(30.0 / 42.8)^{1 / 2}=0.41$
$k_{\text {pos, }, \text { unexp, },}=1.0$ (backed by gypsum)
for $t_{\text {prot }, 0,2}>8 \mathrm{~min}->\Delta t=0.1 \times t_{\text {prot }, 1}-0.035 \times t_{\text {prot }, 0,2}+1.2=4.43 \mathrm{~min}$
$k_{j, 2}=1.0$ (backed by gypsum)
$t_{\text {prot }, 2}=(30.0 \times 0.41 \times 1.0+4.43) \times 1.0=\underline{16.73 \mathrm{~min}}$

## Layer 3 :

$t_{\text {ins }, 0,3}=24 \times\left(h_{3} / 15\right)^{1.4}=24.0 \mathrm{~min}$
for $\sum t_{\text {prot }, 1,2}>t_{\text {ins }, 0,3} / 2 \rightarrow k_{\text {pos }, \text { exp }, 3}=0.5 \times(24.0 / 59.5)^{1 / 2}=0.31$
$k_{\text {pos, unexp, }, 3}=0.5 \times h_{3}{ }^{0.15}=0.75$
for $t_{\text {ins }, 0,3}>8 \mathrm{~min}->\Delta t=0.1 \times t_{\text {prot }, 1,2}-0.035 \times t_{\text {ins }, 0,3}+1.2=6.3 \mathrm{~min}$
$k_{j, 3}=1.0$ (voids filled with stone wool)
$t_{i n s, 3}=(24.0 \times 0.31 \times 0.75+6.3) \times 1.0=\underline{11.88 \mathrm{~min}}$
$t_{c h}$ for the joists when exposed to fire from the floor side is 71.4 minutes.
From the underside (ceiling) exposed to fire, the construction will consist of three layers of 15 mm , type F gypsum.
layer 1:
$t_{\text {prot, }, 0,1}=30 \times\left(h_{1} / 15\right)^{1.2}=30.0 \mathrm{~min}$
$k_{\text {pos, }, \text { exp }, 1}=1.0$ (first layer)
$k_{\text {pos,unexp, },}=1.0$ (gypsum backing)
$k_{j, 1}=1.0$ (gypsum backing)
$\Delta t=0$ (first layer)
$t_{\text {prot }, 1}=\left(t_{\text {prot }, 0,1} \times k_{\text {pos }, \text { exp }, 1} \times k_{\text {pos, }, \text { nexe }, 1}+\Delta t\right) \times k_{j, 1}=\underline{30.0 \mathrm{~min}}$
Layer 2:
$t_{\text {prot, } 0,2}=30 \times\left(h_{1} / 15\right)^{1.2}=30.0 \mathrm{~min}$
for $\sum t_{\text {prot }, 1}>t_{\text {prot }, 0,2} / 2->k_{\text {pos }, \text { exp }, 2}=0.5 \times\left(t_{\text {prot }, 0,2} / \sum t_{\text {prot }, 1}\right)^{1 / 2}=0.5 \times(30.0 / 30)^{1 / 2}=0.5$
$k_{\text {pos, }, \text { nexp, }, 2}=1.0$ (backed by gypsum)
for $t_{\text {prot }, 0,2}>8 \mathrm{~min} \rightarrow \Delta t=0.1 \times t_{\text {prot }, 1}-0.035 \times t_{\text {prot }, 0,2}+1.2=3.15 \mathrm{~min}$
$k_{j, 2}=1.0$ (backed by gypsum)
$t_{\text {prot }, 2}=(30.0 \times 0.5 \times 1.0+3.15) \times 1.0=\underline{18.15 \mathrm{~min}}$
Layer 3 :
$t_{\text {ins }, 0,3}=24 \times\left(h_{3} / 15\right)^{1.4}=24.0 \mathrm{~min}$
for $\sum t_{\text {prot }, 1,2}>t_{\text {ins }, 0,3} / 2->k_{\text {pos }, \text { exp }, 3}=0.5 \times(24.0 / 48.15)^{1 / 2}=0.35$
$k_{\text {pos, unexp, } 3}=0.5 \times \mathrm{h}_{3}{ }^{0.15}=0.75$
for $t_{\text {ins }, 0,3}>8 \mathrm{~min}->\Delta t=0.1 \times t_{\text {prot }, 1,2}-0.035 \times t_{\text {ins }, 0,3}+1.2=5.17 \mathrm{~min}$
$k_{j, 3}=1.0$ (voids filled with stone wool)
$t_{i n s, 3}=(24.0 \times 0.35 \times 0.75+5.17) \times 1.0=\underline{11.47 \mathrm{~min}}$
The charring-time for the joists exposed to fire from the underside is $t_{c h}=59.62$ minutes.
Using the information above it is possible to calculate an approximate self-weight of the floor to use when further dimensioning the floor-joists.

### 7.4 Self-weight of the floor

$\mathrm{g}_{q, k, \text { timber-panel }}=290 \mathrm{~kg} / \mathrm{m}^{3} \times 0.03 \mathrm{~m} \times 9.81 / 1000=0.085 \mathrm{kN} / \mathrm{m}^{2}$.
$\mathrm{gq}_{\mathrm{q}, \mathrm{k}, \text { gypsum }}=760 \mathrm{~kg} / \mathrm{m}^{3} \times 0.015 \mathrm{~m} \times 5 \times 9.81 / 1000=0.56 \mathrm{kN} / \mathrm{m}^{2}$. [1
the self-weight of ventilation, lighting and electrical equipment is estimated at $\mathrm{gq}_{\mathrm{k}, \mathrm{k}, \text { tech }}=0.55 \mathrm{kN} / \mathrm{m}^{2}$.
the estimated thickness and width of the floor-joists is $270 \times 73 \mathrm{~mm}$, thus putting the selfweight of the joist at $g_{q, k, j o i s t}=450 \mathrm{~kg} / \mathrm{m}^{3} \times 0.27 \times 0.073 \times 9.81 / 1000=0.09 \mathrm{kN} / \mathrm{m}$, and for the insulation at $\mathrm{g}_{\mathrm{q}, \mathrm{k}, \mathrm{ins}}=26 \mathrm{~kg} / \mathrm{m}^{3} \times 0.270 \mathrm{~m} \times 9.81 / 1000=0.07 \mathrm{kN} / \mathrm{m}^{2}$.
the longest span of the joists is 7.5 meters, with a spacing of 400 mm . we can therefore calculate the self-weight of the joists to be $\mathrm{g}_{\mathrm{q}, \mathrm{k}, \mathrm{joist}}=0.09 \times 1 / 0.4=0.225 \mathrm{kN} / \mathrm{m}$ the total self-weight of the floor is therefore $\mathrm{g}_{q, k, f l o o r}=1.47 \mathrm{kN} / \mathrm{m}^{2}$.

## 8 Dimensioning of structural elements



Figure 4 simple plan view of the building, floors 1-6th.


Figure 5 plan view of $7^{\text {th }}$ floor
From figure 4 we can see the plan view of the building from $1^{\text {st- }}-6^{\text {th }}$ floor. The beams and columns are named $X_{1-6}$ and $Y_{1-5}$. The beams are continuous from one side of the building to the other. The shear-walls are marked with thick lines.

The internal columns on line $X_{2}$ and $X_{5}$ stop after the $6^{\text {th }}$ floor with a total height of 24 meters. they do not help support the roof. This is done to give more space for the conference-rooms on the $7^{\text {th }}$ floor as seen in figure 5 . The beams holding up the roof in the Y -direction therefore span 11meters.

All the internal walls are supported by glue-laminated beams, they also support the floors. The longest span for a beam supporting an internal wall is 8 meters. All the calculations and dimensioning is done according to NS-EN 1995-1-1: 2004+A1: 2008+NA:2010. [15] for the $7^{\text {th }}$ floor we have an imposed load of $4.0 \mathrm{kN} / \mathrm{m}^{2}$. From table NA 6.1 in NS-EN 1991-11:2002+NA: 2008. [16]
the beam has a self-weight of $490 \mathrm{~kg} / \mathrm{m}^{3}$. the wall assembly has a load of $0.62 \mathrm{kN} / \mathrm{m}^{2}$. the floor and ceiling has a load of $1.47 \mathrm{kN} / \mathrm{m}^{2}$.
due to the floor joists the beams are supported against lateral torsional buckling. A simplification has been made by assuming that the loads from the floor distribute evenly to all beams in its influence area. Using 6.10 a and b with an approximated influence area of $30 \mathrm{~m}^{2}$ to find design values for loads:

$$
\begin{aligned}
6.10 \mathrm{a} .=1.35 \times\left(4 \mathrm{~m} \times 8 \mathrm{~m} \times 0.62 \mathrm{kN} / \mathrm{m}^{2}\right. & \left.+1.47 \mathrm{kN} / \mathrm{m}^{2} \times 30 \mathrm{~m}^{2}\right)+1.5 \times 0.7 \times 4.0 \mathrm{kN} / \mathrm{m}^{2} \times 30 \mathrm{~m}^{2} \\
= & \underline{212.3 \mathrm{kN}}
\end{aligned}
$$

$6.10 \mathrm{~b}=1.2 \times(4 \times 8 \times 0.62+1.47 \times 30)+1.5 \times 4.0 \times 30=\underline{256.7} \mathrm{kN}$
Using the partial factors from expression 6.10 b for dimensioning:
distributed design-loads from:

$$
\begin{gathered}
\text { walls }=3.0 \mathrm{kN} / \mathrm{m} \\
\text { floor }=1.76 \mathrm{kN} / \mathrm{m}^{2}
\end{gathered}
$$

imposed load on floor $=6 \mathrm{kN} / \mathrm{m}^{2}$
imposed load from snow $=1.8 \mathrm{kN} / \mathrm{m}^{2}$
as the forces on the $7^{\text {th }}$ floor is slightly higher than the others due to being in class $C 2$, we will use these values for dimensioning of all beams of the same position in all floors.
for a beam in the class GL 36h, values for characteristic strength are taken from NS-EN 1995-1-1: 2004+A1: 2008+NA :2010 table 1. [15]

Bending: $\mathrm{f}_{\mathrm{m}, \mathrm{g}, \mathrm{k}}=36 \mathrm{~N} / \mathrm{mm}^{2}$
Shear: $\mathrm{f}_{\mathrm{v}, \mathrm{g}, \mathrm{k}}=4.3 \mathrm{~N} / \mathrm{mm}^{2}$

Compression: $\mathrm{f}_{\mathrm{c}, 0 \mathrm{~g}, \mathrm{k}}=31 \mathrm{~N} / \mathrm{mm}^{2}$ and the design strength of the beam: $X_{d}=K_{\bmod } \times X_{k} / Y_{m}$
where:
$X_{k}$ is the characteristic value of strength is ether $36 \mathrm{~N} / \mathrm{mm}^{2}$ for bending, $4.3 \mathrm{~N} / \mathrm{mm}^{2}$ for shear or $31 \mathrm{~N} / \mathrm{mm}^{2}$ for compression.
$Y_{m}$ is the partial factor of a material property $=1.15$ for glue-laminated elements.
$K_{\text {mod }}$ is a modification factor $=0.8$ for service class 1 with medium term load such as imposed load being dominant.

$$
\begin{gathered}
f_{m, d}=0.8 \times 36 / 1.15=25 \mathrm{~N} / \mathrm{mm}^{2} \\
\mathrm{f}_{\mathrm{v}, \mathrm{~d}}=0.8 \times 4.3 / 1.15=2.99 \mathrm{~N} / \mathrm{mm}^{2} \\
f_{\mathrm{c}, \mathrm{~d}}=21.56 \mathrm{~N} / \mathrm{mm}^{2}
\end{gathered}
$$

### 8.1 Beams

As the thickness of the floor joists is set at $\mathrm{h}=270 \mathrm{~mm}$ and the thickness of the walls is $b=202 \mathrm{~mm}$, we will use a cross-section of $700 \times 202 \mathrm{~mm}$ for the beam. Doing this we can ensure the beam is not protruding outside the wall. maximum bending moment for beams has been calculated by using an online calculator with a triangular load distribution from the floor and imposed load, and a uniformly distributed load from the wall. for the beam with an 8 m span:
bending moment:
$M_{y, e d}=334.56 \mathrm{kNm}$
Shear forces:
$V_{z, \text { ed }}=128 \mathrm{kN}$

The beams are named $\mathrm{Y}_{2,4}$, as marked in figure 4, and span 8 m . the load from the floor and imposed load is distributed triangularly while self-weight of the beam and walls are uniformly distributed.

## Dimensioning against bending:

$$
\begin{gathered}
M_{y, r d}=W_{y} \times f_{m, d} \\
W_{y}=b \times h^{2} / 6=16496666.7 \mathrm{~mm}^{3}
\end{gathered}
$$

$M_{y, r d}=412.4 \mathrm{kNm}$ (design resistance of the beam against bending) self-weight of the beam being: $490 \times 0.7 \times 0.202 \times 9.8 / 1000=0.624 \mathrm{kN} / \mathrm{m} \times 1.2=0.75 \mathrm{kN} / \mathrm{m}$ it adds to the maximum moment with 6 kNm and the shear force with 3 kN .

$$
M_{y, r d}=412.4 \mathrm{kNm} \geq M_{y, e d}=340.56 \mathrm{kNm}
$$

Dimensioning against shear stress:
$T_{d} \leq f_{v, d}$ needs to be satisfied.

$$
T_{d}=3 v_{d} / 2 b_{\text {eff }} \times h
$$

$$
b_{\text {eff }}=k_{\text {cr }} \times b=0.8 \times 202=161.6 \mathrm{~mm}
$$

$$
V_{z, r, d}=V_{z, d}=2 / 3 \times(2.99 \times 161.6 \times 700)=225485.8 \mathrm{~N}=225.48 \mathrm{kN}
$$

$V_{2, e d}=128+3 \mathrm{kN} \leq \mathrm{V}_{2, r, \mathrm{~d}}=225.48 \mathrm{kN}$ cross-section is good in shear.
the beams designated for the outer perimeter supports a glass-front with a weight of 30

$$
\mathrm{kg} / \mathrm{m}^{2} .
$$

the force on the beam from the glass is therefore $q_{g, k}=0.29 \mathrm{kN} / \mathrm{m}^{2}$ and design force $\mathrm{q}_{\mathrm{g}, \mathrm{d}}=0.35$ $\mathrm{kN} / \mathrm{m}^{2}$. The beam has a length of 8 m on the X -axis and 7.5 m on the Y -axis. the imposed load and load from the floor has a triangular shape. The beams are named $X_{1,5}$ and $Y_{1,6}$.

> The design load is therefore: glass-front $=1.4 \mathrm{kN} / \mathrm{m}$
> floor $=1.76 \mathrm{kN} / \mathrm{m}^{2}$
> imposed load floor $=6 \mathrm{kN} / \mathrm{m}^{2}$
the forces are greatest on the beam in the X -axis and is therefore the dimensioning side.
maximum bending moment is then: $M_{y, e d}=170.0 \mathrm{kNm}$
with a shear force of: $V_{y, e d}=65.0 \mathrm{kN}$
Dimensioning against bending:
thickness of the beam is 148 mm . height is 550 mm .

$$
\begin{gathered}
W_{y}=7461666.6 \mathrm{~mm}^{3} \\
M_{y, r d}=186.5 \mathrm{kNm}
\end{gathered}
$$

Shear:

$$
T_{d}=3 v_{d} / 2 b_{\text {eff }} \times h
$$

$$
b_{\text {eff }}=k_{\mathrm{cr}} \times b=0.8 \times 148=118.4 \mathrm{~mm}
$$

$$
V_{z, \mathrm{r}, \mathrm{~d}}=V_{2, \mathrm{~d}}=2 / 3 \times(2.99 \times 118.4 \times 550)=129805.8 \mathrm{~N}=129.8 \mathrm{kN}
$$

forces from the self-weight amounts to $0.47 \mathrm{kN} / \mathrm{m}$. added bending moment is then 3.3 kNm and shear 1.76 kN .
$M_{y, r d}=186.5 \mathrm{kNm} \geq M_{y, e d}=173.3 \mathrm{kNm}$

$$
V_{z, r, \mathrm{~d}}=129.8 \mathrm{kN}>\mathrm{V}_{2, \mathrm{ed}}=65.5 \mathrm{kN}
$$

cross-section is good in both bending and shear.
For beam $X_{2,3,4,5}$. The length of the beam is 7.5 meters. loads from the wall, floor and imposed loads are the same as earlier and also in a triangular shape on each side of the beam.

Design bending stress:

$$
M_{y, \text { ed }}=227.3 \mathrm{kNm}
$$

Design shear stress:

$$
V_{y, e d}=94.3 \mathrm{kN}
$$

With a cross-section of $202 \times 550 \mathrm{~mm}$ :
$M_{y, r d}=254.6 \mathrm{kNm}>\mathrm{M}_{\mathrm{y}, \mathrm{ed}}=227.3 \mathrm{kNm}$

$$
V_{y, \mathrm{rd}}=177.1 \mathrm{kN}>\mathrm{V}_{\mathrm{y}, \mathrm{ed}}=94.3 \mathrm{kN}
$$

The floor joists, with dimensions of $270 \times 73 \mathrm{~mm}$ are experiencing a uniformly distributed load of $1.76 \mathrm{kN} / \mathrm{m}^{2} \times 0.4 \mathrm{~m}+6 \times 0.4=3.10 \mathrm{kN} / \mathrm{m}$ per meter of joist. They have a span of 7.5 meter.

$$
\begin{gathered}
M_{y, e d}=21.8 \mathrm{kNm} . \\
w=b \times h^{2} / 6=886950 \mathrm{~mm}^{3} \\
M_{y, r d}=22.17 \mathrm{kNm}>M_{y, e d}=21.8 \mathrm{kNm}
\end{gathered}
$$

$$
\begin{gathered}
\mathrm{V}_{\mathrm{z}, \mathrm{ed}}=11.63 \mathrm{kN} \\
\mathrm{v}_{\mathrm{z}, \mathrm{rd}}=2 / 3 \times 0.8 \times \mathrm{b} \times \mathrm{h} \times 2.99=31.4 \mathrm{kN}>\mathrm{v}_{\mathrm{z}, \mathrm{ed}}=11.63 \mathrm{kN} \\
\text { cross-section is suitable in bending and shear. }
\end{gathered}
$$

The beams holding up the roof for the conference rooms:
The floor is divided into a hallway and four conference rooms of equal size as seen in figure 5. The roof is being held up by columns giving the beams a span of 11 m in the x-direction with a spacing of 7.5 m in the y-direction. The snow-load is $1.2 \mathrm{kN} / \mathrm{m}^{2}$ and the self-weight is assumed to be $2 \mathrm{kN} / \mathrm{m}^{2}$. Using Eq 6.10 b the forces are $4.2 \mathrm{kN} / \mathrm{m}^{2}$. The beam around the edge is the same as for floors below. Using an influence area with 7.5 m of maximum width per meter of beam for calculations.

Bending moment: $\mathrm{M}_{\mathrm{y} \text {,ed }}=317.63 \mathrm{kNm}$
shear force: $V_{y, \text { ed }}=86.63 \mathrm{kN}$
Seeing that a beam of $202 \times 700 \mathrm{~mm}$ as used in the lower floors is sufficient it will be used for holding up the roof as well.

### 8.2 Columns

each of the columns will be built as a single unit with the same cross section for each floor. GL36h has a compressive strength of $f_{c, 0, g, k}=31 \mathrm{~N} / \mathrm{mm}^{2}$ giving the timber a design compressive strength of $f_{c, 0, d}=21.56 \mathrm{~N} / \mathrm{mm}^{2}$.

For the corner column the loads are:
from beams $=1.2 \times 490 \times(7.91) \times 9.81 / 1000=45.62 \mathrm{kN}$.
from floors $=1.764(20.6+15 \times 6)=195.1 \mathrm{kN}$.
imposed loads $=1.5 \times(4+1.2) \times 20.6+1.5 \times(3 \times 5) \times 15=498.18 \mathrm{kN}$.
from glass $=1.2 \times 0.29 \times 240=83.5$
combined load is $\mathrm{N}_{\mathrm{ed}}=822.4 \mathrm{kN}$.
Dimension will then be $300 \times 300 \mathrm{~mm} . N_{r, d}=A \times f_{c, 0, d}=300 \times 300 \times 21.56$. giving the cross-section a design compressive strength of $\mathrm{N}_{\mathrm{r}, \mathrm{d}}=1940.4 \mathrm{kN}$.

For the columns of the outer perimeter $y$-axis the loads are:

$$
\begin{gathered}
\text { from beams }=1.2 \times 490 \times 11.59 \times 9.81 / 1000=66.85 \mathrm{kN} \\
\text { from floors }=1.764 \times(30 \times 5+41.25)=317.52 \mathrm{kN} . \\
\text { from walls }=1.2 \times 0.62 \times 4 \times 3.3 \times 5=49.1 \mathrm{kN} \\
\text { imposed loads }=1.5 \times(4 \times 41.25+3 \times 5 \times 30)=909 \mathrm{kN} .
\end{gathered}
$$

> from roof=$=(1.2 \times 2+1.5 \times 1.2) \times 41.25=173.25 \mathrm{kN}$
> combined load is $\mathrm{N}_{\mathrm{ed}}=1515.7 \mathrm{kN}$.
we will utilize the same column as for the corners: $300 \times 300 \mathrm{~mm}$ cross-section.

$$
\begin{aligned}
& \text { For the columns of the outer perimeter } x \text {-axis loads are: } \\
& \text { from beams }=1.2 \times 490 \times 14.7 \times 9.81 / 1000=84.8 \mathrm{kN} \text {. } \\
& \text { from floors }=1.764 \times(20.6 \times 5+35.7)=244.7 \mathrm{kN} \text {. } \\
& \text { imposed loads }=1.5 \times(4 \times 35.7+3 \times 5 \times 20.6)=677.7 \mathrm{kN} \text {. } \\
& \text { from walls }=1.2 \times(0.62 \times 74.25+0.29 \times 185)=119.6 \\
& \text { from roof }=(1.2 \times 2+1.5 \times 1.2) \times 35.7=149.9 \mathrm{kN} \\
& \text { combined load is } \mathrm{N}_{\mathrm{ed}}=1276.7 \mathrm{kN} \text {. } \\
& \text { we will utilize the } 300 \times 300 \mathrm{~mm} \text { cross-section. }
\end{aligned}
$$

The internal columns of $x_{3,4}$ have loads as:
from beams $=1.2 \times 490 \times(2.4+1.84 \times 6) \times 9.81 / 1000=78.21 \mathrm{kN}$.
from floors $=1.764 \times(41.25 \times 6)=436.6 \mathrm{kN}$.
from roof $=1.2 \times 2 \times 71.25=171.0 \mathrm{kN}$
from walls $=1.2 \times 42.9 \times 0.62 \times 6=191.5 \mathrm{kN}$
imposed loads $=1.5 \times(3 \times 5 \times 41.25+4 \times 41.25+1.2 \times 71.25)=1303.9 \mathrm{kN}$.
combined load is $\mathrm{N}_{\text {ed }}=2181.2 \mathrm{kN}$.
a cross section of $350 \times 350 \mathrm{~mm}$ will be utilized, giving the cross-section a design strength of

$$
N_{r, d}=2641.1 \mathrm{kN} .
$$

The internal columns of $\mathrm{x}_{2,5}$ have the same loads as $\mathrm{x}_{3,4}$ but without the roof. combined load is therefore $\mathrm{N}_{\mathrm{ed}}=2010.2 \mathrm{kN}$ and cross-section $350 \times 350$ will be used.

### 8.3 Shear-walls

with a building of this size it is necessary to utilize shear-walls in order to stabilize the construction against horizontal forces such as wind load and seismic activity. The shear walls for this building is made up of massive cross-laminated timber that cover the full height of the building with a thickness of 202 mm . They are in position $Y_{3}$ on each side of the building, extending 8 meters towards the center to give support in the $X$-direction. As well as $X_{3}$ and $X_{4}$ on either side to support in the Y -direction. The elevator-shaft and staircase walls are made
in the same way and will also support against horizontal force while also supporting weight of the elevator and staircase vertically. The total wind load that will affect the building in each direction was calculated to be 1357.2 kN . as calculated before, GL36H has a design shear strength of $\mathrm{f}_{\mathrm{v}, \mathrm{d}}=2.99 \mathrm{~N} / \mathrm{mm}^{2}$.
The shear-walls in the $Y$-direction has a surface-area of $A=200 \times 7500 \mathrm{~mm}$ on each side of the building, giving it a design strength of

$$
V_{z, r d}=2 / 3 \times 0.8 \times 200 \times 7500 \times 2.99=2392.0 \mathrm{kN}>\mathrm{V}_{2, \mathrm{ed}}=1357.2 \mathrm{kN} .
$$

While in the $X$-direction they have a design strength of $\mathrm{V}_{z, \mathrm{rd}}=2551.4 \mathrm{kN}>\mathrm{V}_{\text {z,ed }}=1357.2 \mathrm{kN}$.
they also support the surrounding floor-area with a load of $\mathrm{Ned}_{\mathrm{ed}}=3697.0 \mathrm{kN}$ each.
The walls supporting the elevator and staircase have a design compressive strength of $N_{r, \text { ed }}=A \times f_{c, 0, e d}=(10000+5000+5000) \times 200 \mathrm{~mm} \times 21.56 \mathrm{~N} / \mathrm{mm}^{2}=862400 \mathrm{kN}$ when considering one wall as compromised due to doorways. These walls also support the surrounding floor-area with a load of 4362.4 kN .

## 9 Members in the accidental limit state



Figure 6 pyrolysis of a joist [17]
Figure 6 is taken from Limtreboka, [17] it shows charring on a wood element.

Design strength of timber in a fire situation is calculated as before with equations from the strandard [15] and limtreboka [17]. Using different values for $k_{\bmod }$ and $Y_{m}$.

$$
\begin{gathered}
X_{\mathrm{d}}=\mathrm{K}_{\mathrm{mod}, \mathrm{fi}} \times \mathrm{X}_{\mathrm{k}} / Y_{\mathrm{m}, \mathrm{fi}} \\
\mathrm{~K}_{\mathrm{mod}, \mathrm{fi}}=1.0 \\
Y_{\mathrm{m}, \mathrm{fi}}=1.0
\end{gathered}
$$

using this equation we find design strength in:
bending: $\mathrm{M}_{\mathrm{d}, \mathrm{fi}}=36.0 \mathrm{~N} / \mathrm{mm}^{2}$
shear: $\mathrm{V}_{\mathrm{d}, \mathrm{fi}}=4.3 \mathrm{~N} / \mathrm{mm}^{2}$
compression: $\mathrm{f}_{\mathrm{c}, \mathrm{d}, \mathrm{fi}}=31.0 \mathrm{~N} / \mathrm{mm}^{2}$

In the situation of a fire, the design loads are calculated as:

$$
1.0 \times g_{k}+1.0 \times \psi_{1} \times q_{k}+1.0 \times \psi_{2} \times s_{k}
$$

where $\psi_{1}=0.5$ for category $B$ and 0.7 for category $C$.
$\psi_{2}=0.3$ for category $B$ and 0.6 for category $C$. we will first calculate the limit state for $7^{\text {th }}$ floor, category $C$.
values taken from table NA.A1.1. [16]
load due to self-weight of the beams $=0.624 \mathrm{kN} / \mathrm{m}$
from walls $=1.0 \times 4 \mathrm{~m} \times 0.62=3.104 \mathrm{kN} / \mathrm{m}$

$$
\begin{aligned}
& \text { from floors }=1.0 \times 1.47 \mathrm{kN} / \mathrm{m}^{2}=1.47 \mathrm{kN} / \mathrm{m}^{2} \\
& \text { imposed load }=0.7 \times 4.0 \mathrm{kN} / \mathrm{m}^{2}=2.8 \mathrm{kN} / \mathrm{m}^{2}
\end{aligned}
$$

### 9.1 Beams

for the span of 8.0 meters with $202 \times 700 \mathrm{~mm}$ cross-section this means:

$$
\begin{gathered}
M_{e d, f i}=195.5 \mathrm{kNm} \\
\mathrm{~V}_{\mathrm{ed}, \mathrm{fi}}=76.42 \mathrm{kN}
\end{gathered}
$$

parts of the cross-section is protected by the wall and floor, however for simplicity and safety the effects of charring will be calculated with regards to a beam with two exposed sides.

Using two dimensional charring with the reduced cross-section method in R90:

$$
\begin{gathered}
\beta_{\mathrm{n}}=0.55 \mathrm{~mm} / \mathrm{min} \\
t=90 \mathrm{~min} \\
\mathrm{~d}_{\text {char }, \mathrm{n}}=\beta_{\mathrm{n}} \times t=90 \times 0.55=49.5 \\
\mathrm{~d}_{\text {eff }}=\mathrm{d}_{\text {char }, \mathrm{n}}+\mathrm{k}_{0} \times \mathrm{d}_{0} \\
\mathrm{k}_{0}=1.0 \\
\mathrm{~d}_{0}=7.0 \mathrm{~mm} \\
\mathrm{~d}_{\mathrm{eff}}=49.5+7.0=56.5 \mathrm{~mm}
\end{gathered}
$$

the residual cross-section is then $643.5 \times 145.5 \mathrm{~mm}$.
with a design strength of $M_{y, r d}=361.5 \mathrm{kNm}>\mathrm{Med}, \mathrm{fi}=195.5 \mathrm{kNm}$ and

$$
\mathrm{V}_{\mathrm{z}, \mathrm{rd}}=214.7 \mathrm{kN}>\mathrm{V}_{\mathrm{ed}, \mathrm{fi}}=76.42 \mathrm{kN} .
$$

this beam is sufficient in a fire situation.
the internal beams with a length of 7.5 meters and cross-section of $550 \times 202 \mathrm{~mm}$ experience the same loads and a $M_{\text {ed, }, \mathrm{i}}=131.9 \mathrm{kNm}$ and $\mathrm{V}_{\text {ed, }, \mathrm{i}}=55.67 \mathrm{kN}$. the reduction in cross-section is the same as before, a reduction of 56.5 mm after 90 minutes of exposure leaves a cross-section of $493.5 \times 145.5 \mathrm{~mm}$ with a $M_{y, r d}=212.1 \mathrm{kNm}>$

$$
M_{e d, f i}=131.9 \mathrm{kNm} \text { and } V_{2, \mathrm{rd}}=164.6 \mathrm{kN}>\mathrm{V}_{\mathrm{ed}, \mathrm{fi}}=55.67 \mathrm{kN} .
$$

for the beams holding up the roof the span is 11 m the cross-section is $202 \times 700$ and the loads are:

$$
\begin{gathered}
\text { from snow }=1.2 \times 0.6=0.72 \mathrm{kN} / \mathrm{m}^{2} \\
\text { self- weight of roof }=2 \mathrm{kN} / \mathrm{m}^{2} \\
\text { self-weight of beam }=0.624 \mathrm{kN} / \mathrm{m} \\
M_{\text {ed, }, \mathrm{i}}=181.86 \mathrm{kNm} \text { and } V_{\text {ed, }, \mathrm{fi}}=51.39 \mathrm{kN}
\end{gathered}
$$

the beam is exposed on three sides, the effective cross-section in R90 is therefore $643.5 \times 89 \mathrm{~mm}$ and $M_{y, \mathrm{rd}}=221.1 \mathrm{kNm}>\mathrm{M}_{\text {ed }, \mathrm{fi}}=181.86 \mathrm{kNm}$ and $\mathrm{V}_{2, \mathrm{rd}}=131.3 \mathrm{kN}>\mathrm{V}_{\text {ed, }, \mathrm{f}}=51.39 \mathrm{kN}$.

For the beams at the perimeter of the building the loads are:

$$
\begin{gathered}
\text { from glass }=1.45 \mathrm{kN} / \mathrm{m} \\
\text { from floor }=1.47 \mathrm{kN} / \mathrm{m}^{2} \\
\text { imposed load }=2.8 \mathrm{kN} / \mathrm{m}^{2} \\
\text { self-weight }=0.4 \mathrm{kN} / \mathrm{m} \\
\mathrm{M}_{\text {ed, } \mathrm{fi}}=107.8 \mathrm{kNm} \\
V_{\text {ed, }, \mathrm{fi}}=42.9 \mathrm{kN}
\end{gathered}
$$

the beam is exposed on 2 sides. After 90 minutes of exposure the cross-section is $493.5 \times 91.5 \mathrm{~mm}$ with a strength of $M_{y, r d}=133.7 \mathrm{kNm}>M_{\text {ed, } \mathrm{f}}=107.8 \mathrm{kNm}$ and

$$
V_{z, r d}=103.5 \mathrm{kN}>\mathrm{V}_{\mathrm{ed}, \mathrm{fi}}=42.9 \mathrm{kN} .
$$

From the ceiling side, the protection of the joists in the floor is 59.6minutes. 90-59.6= 30.4 minutes that they will be charring. They will charr at an increased pace due to the protection, since they are protected on the sides by rock-wool the charring is limited to the front of the member.
loads in accidental limit state is:
from self-weight $=1.47 \mathrm{kN} / \mathrm{m}^{2} \times 0.4 \mathrm{~m}=0.6 \mathrm{kN} / \mathrm{m}$
due to imposed load $=0.6 \times 4 \times 0.4=0.96 \mathrm{kN} / \mathrm{m}$

$$
\begin{aligned}
& M_{e d, f i}=10.97 \mathrm{kNm} \text { and } V_{e d, f i}=5.85 \mathrm{kN} . \\
& \text { charring rate: } \beta_{n}=\beta_{0} \times k_{s} \times k_{n} \times k_{p} . \\
& \quad \beta_{0}=0.5 \mathrm{~mm} / \mathrm{min} \\
& k_{s}=0,000167 \times b^{2}-0,029 \times b+2,27=1.04
\end{aligned}
$$

$$
\begin{gathered}
k_{n}=1.25 \\
k_{p}=k_{3}=2.0 \\
\beta_{\mathrm{n}}=1.3 \mathrm{~mm} / \mathrm{min} \\
\mathrm{~d}_{0}=13.5+0.1 \times \mathrm{h}=40.5 \mathrm{~mm}
\end{gathered}
$$

the effective charring after 30.4 min of burning is therefore $d_{\text {eff }}=80.02 \mathrm{~mm}$. with a new crosssection of $190.0 \times 73 \mathrm{~mm}$ the strength is then $\mathrm{M}_{\mathrm{y}, \mathrm{rd}}=18.1 \mathrm{kNm}>\mathrm{M}_{\text {ed, } \mathrm{fi}}=10.97 \mathrm{kNm}$ and

$$
\mathrm{V}_{\text {z, }, \mathrm{rd}}=31.8 \mathrm{kN}>\mathrm{V}_{\text {ed }, \mathrm{fi}}=5.85 \mathrm{kN} .
$$

With the floor-side exposed to fire the protection time is $t_{c h}=71.4$ minutes. the joists will therefore char for 18.6 minutes. Charring rate is the same as before, $\beta_{\mathrm{n}}=1.3 \mathrm{~mm} / \mathrm{min}$.

$$
\begin{gathered}
\mathrm{d}_{0}=21.5+0.1 \times \mathrm{h}=48.5 \mathrm{~mm} \\
d_{e f f}=72.68 \mathrm{~mm}
\end{gathered}
$$

The remaining cross-section is larger than for a fire-situation on the ceiling-side, the joists are strong enough to withstand a fire in R90.

## 9.2 columns

The columns experiencing the highest pressure are the internal columns on the first floor with a force of 2181.2 kN . It's also exposed on four sides. After 90 minutes of exposure the effective cross-section is then $237 \times 237 \mathrm{~mm}$ with a strength of $\mathrm{N}_{\mathrm{rd}}=1211.0 \mathrm{kN}$.

$$
\begin{gathered}
\text { from beams }=490 \times(2.4+1.84 \times 6) \times 9.81 / 1000=64.6 \mathrm{kN} . \\
\text { from floors }=1.47 \times(71.25+41.25 \times 6)=468.6 \mathrm{kN} . \\
\text { from roof }=2 \times 71.25=142.5 \mathrm{kN} \\
\text { from walls }=0.62 \times 42.9 \times 6=159.6 \mathrm{kN}
\end{gathered}
$$

imposed loads $=0.5 \times(3 \times 5 \times 41.25)+0.7 \times(4 \times 71.5)+0.6 \times(1.2 \times 71.25)=560.87 \mathrm{kN}$.
combined load is $\mathrm{N}_{\text {ed, } \mathrm{fi}}=1396.1 \mathrm{kN}$
the strength after exposure to fire is smaller than the design load in ALS. We need to use a bigger cross-section. $400 \times 400 \mathrm{~mm}$ has a strength of $\mathrm{N}_{\mathrm{rd}}=1775.8 \mathrm{kN}>\mathrm{N}_{\text {ed, }, \mathrm{fi}}=1396.1 \mathrm{kN}$ which is sufficient.

For the outer columns, the highest compressive force in ALS is:

$$
\begin{gathered}
\text { from beams }=490 \times 11.59 \times 9.81 / 1000=55.7 \mathrm{kN} . \\
\text { from floors }=1.47 \times(30 \times 5+41.25)=281.1 \mathrm{kN} . \\
\text { from walls }=0.62 \times 3.75 \times 3.3=7.67 \mathrm{kN} \\
\text { imposed loads }=0.7 \times(4 \times 41.25)+0.5 \times(3 \times 5 \times 30)=340.5 \mathrm{kN} . \\
\text { from roof }=(0.7 \times 2+0.6 \times 1.2) \times 41.25=87.45 \mathrm{kN} \\
\text { combined load is then } \mathrm{N}_{\text {ed }, \mathrm{fi}}=772.42 \mathrm{kN} .
\end{gathered}
$$

The column is exposed on three sides and the cross-section after 90 minutes is $243.5 \times 187 \mathrm{~mm}$ with a design strength of $N_{r d}=981.7 \mathrm{kN}>\mathrm{N}_{\text {ed }, \mathrm{fi}}=772.42 \mathrm{kN}$. The cross-section is good in R90.

The columns on the corners has less load and is more protected in a fire-situation by only being exposed on two sides, it is not necessary to calculate the fire-resistance for the columns on the corners as we know it will be strong enough.

### 9.3 Shear walls

They are exposed to fire on one side and have only one-dimensional charring. For hardwood with a density $>450 \mathrm{~kg} / \mathrm{m}^{3} \beta_{0}=0.5$ and $d_{\text {char,eff }}=\beta_{0} \times t+7 \mathrm{~mm}$ after 90 minutes. Giving them a thickness of 148 mm and a strength of $\mathrm{V}_{2, \mathrm{rd}}=2545.6 \mathrm{kN}$ and $\mathrm{N}_{\mathrm{rd}}=23931.6 \mathrm{kN}$ each. Shear walls are good in R90.

## 10 Check for buckling of columns.

The columns on the first floor are not supported against buckling by the walls, it is therefore necessary to check for buckling.
the internal columns are not subject to bending, while the columns on the outside of the structure are subjected to bending due to uneven loading. Calculations are done according to:
NS-EN 1995-1-1:2004+A1:2008+NA:2010. [15]
$\mathrm{L}_{\mathrm{cr}}=3.5 \mathrm{~m}$
$\mathrm{E}_{\mathrm{d}}=\mathrm{E}_{0, \mathrm{~g}, 05} / \mathrm{Y}_{\mathrm{m}}=11900 / 1.15=10347.8 \mathrm{~N} / \mathrm{mm}^{2}$
$\mathrm{G}_{\mathrm{d}}=\mathrm{G}_{\mathrm{g}, \text { mean }} / \mathrm{Y}_{\mathrm{m}}=910 / 1.15=791.3 \mathrm{~N} / \mathrm{mm}^{2}$

Radius of gyration:
$\mathrm{i}_{y}=\mathrm{i}_{z}=\mathrm{h} / 12^{0.5}=300 / 12^{0.5}=86.6 \mathrm{~mm}$ for the 300 mm column and 115.4 mm for the 400 mm column.

Relative Slenderness:
$\lambda=\mathrm{L}_{\mathrm{cr}} / \mathrm{i}=3500 / 86.6 \mathrm{~mm}=40.41$ for the 300 mm column and 30.3 for the 400 mm column.
$\lambda_{\text {rel }}=\lambda / 3.14 \times\left(\mathrm{f}_{\mathrm{c}, 0 \mathrm{~g} /} / \mathrm{E}_{0, \mathrm{~g}, 05}\right)^{0.5}=0.70$ for the 300 mm column and 0.49 for the 400 mm column.

$$
K_{300}=0.5 \times\left(1+\beta_{c} \times\left(\lambda_{\text {rel }}-0.3\right)+\lambda_{\text {rel }}{ }^{2}=0.765\right.
$$

$$
K_{400}=0.63
$$

$\beta_{\mathrm{c}}=0.1$ for glulam.

Buckling reduction factor:
$\left.K_{c}=1 / K+\left(K^{2}-\lambda_{\text {rel }}\right)^{2}\right)^{0.5}=0.93$ for 300 mm and 0.97 for 400 mm .
design compressive stress:
$\sigma_{\mathrm{c}, 0 \mathrm{~g}, \mathrm{~d}}=\mathrm{N}_{\mathrm{ed}} / \mathrm{A}=16.84 \mathrm{~N} / \mathrm{mm}^{2}$ for the 300 mm and $13.63 \mathrm{~N} / \mathrm{mm}^{2}$ for the 400 mm .
$\sigma_{m, d}=M_{e, d} / w_{y}=383 \times 10^{6} / 4.5 \times 10^{6}=85.11$ only for the $300 \times 300 \mathrm{~mm}$ cross-section.
stability check of the column:
$\left(\sigma_{m, d} / f_{m, d}\right)+\sigma_{c, 0, \mathrm{~g}, \mathrm{~d}} / K_{c} \times f_{c, 0, \mathrm{gd}}=4.24<1.0=$ for the $300 \times 300 \mathrm{~mm}$ cross-section on the perimeter. Failure of cross-section. $\sigma_{c, 0, \mathrm{~g}, \mathrm{~d}} / \mathrm{K}_{\mathrm{c}} \times \mathrm{f}_{\mathrm{c}, 0, \mathrm{gd}}=0.65<1.0=$ for the $400 \times 400 \mathrm{~mm}$ cross-section. The cross-section is suitable.
the columns on the perimeter will buckle. new cross section for testing is $600 \times 400 \mathrm{~mm}$ :
$\sigma_{\mathrm{m}, \mathrm{d}}=15.95 \mathrm{~N} / \mathrm{mm}^{2}$
$\sigma_{\mathrm{c}, 0, \mathrm{~g}, \mathrm{~d}}=7.04 \mathrm{~N} / \mathrm{mm}^{2}$
$\left(\sigma_{\mathrm{m}, \mathrm{d}} / \mathrm{f}_{\mathrm{m}, \mathrm{d}}\right)+\sigma_{\mathrm{c}, 0 \mathrm{~g}, \mathrm{~d}} / \mathrm{K}_{\mathrm{c}} \times \mathrm{f}_{\mathrm{c}, 0, \mathrm{gd}}=0.96<1.0=$ for the $400 \times 600 \mathrm{~mm}$ cross-section.
The new cross-section is suitable.

The corner columns experience moment in two directions and must satisfy the expression:

$$
\left(\sigma_{m, v, d} / f_{m, d}\right)+k_{m} \times\left(\sigma_{m, z, d} / f_{m, d}\right)+\sigma_{c, 0, \mathrm{~g}, \mathrm{~d}} / K_{c} \times f_{c, 0, \mathrm{~g} d}<1.0
$$

with a cross-section of $400 \times 400 \mathrm{~mm} \mathrm{~N}_{\mathrm{ed}}=822.4 \mathrm{kN}$ and $\mathrm{M}_{\mathrm{y}, \mathrm{ed}}=\mathrm{M}_{\mathrm{z}, \mathrm{ed}}=82.24 \mathrm{kNm}$.

$$
\begin{gathered}
\sigma_{m, d}=7.71 \\
\sigma_{c, 0 \mathrm{~g}, \mathrm{~d}}=5.14 \\
k_{\mathrm{m}}=0.7 \text { for rectangular cross-sections } \\
\left(\sigma_{\mathrm{m}, \mathrm{y}, \mathrm{~d}} / \mathrm{f}_{\mathrm{m}, \mathrm{~d}}\right)+\mathrm{k}_{\mathrm{m}} \times\left(\sigma_{\mathrm{m}, \mathrm{z}, \mathrm{~d}} / \mathrm{f}_{\mathrm{m}, \mathrm{~d}}\right)+\sigma_{\mathrm{c}, \mathrm{o}, \mathrm{~g}, \mathrm{~d}} / \mathrm{K}_{\mathrm{c}} \times \mathrm{f}_{\mathrm{c}, 0, \mathrm{~g} \mathrm{~d}}=0.77<1.0
\end{gathered}
$$

The cross-section is suitable.

## 11 checking beams for failure

## 11.1 failure due to combined action

The beams will have a slight compressive force due to the strength of the wind acting on the building. It is necessary to check the beams for failure due to combined bending and compression. In order to calculate it a simplification was made where the wind force spreads evenly across all the beams on one side of the building. Since the combined wind load for
oppsing sides is 1357.2 kN , divided by 30 beams on each side the compression is then 45.2 kN .
the expression that needs to be satisfied is: $\left(\sigma_{m, d} / k_{c r i t} \times f_{m, d}\right)^{2}+\left(\sigma_{c, 0, d} / k_{c, 2} \times f_{c, 0, d}\right)<1.0$
$\sigma_{\mathrm{m}, \mathrm{d}}=$ design bending stress
$\mathrm{k}_{\text {crit }}=$ is a factor to compensate for torsional buckling, the beams are well supported in the z -axis $\mathrm{k}_{\text {crit }}=1.0$
$\sigma_{\mathrm{c}, \mathrm{o}, \mathrm{d}}=$ design compressive stress
$\mathrm{k}_{c, y}=1 / \mathrm{k}_{\mathrm{y}}+\left(\mathrm{k}_{\mathrm{y}}{ }^{2}-\lambda_{\text {rel, }}{ }^{2}\right)^{0.5}$ calculated in the same way as for columns.

## 8 m beam with $700 \times 202 \mathrm{~mm}$ cross-section:

$$
\begin{gathered}
\sigma_{\mathrm{m}, \mathrm{~d}}=\mathrm{M}_{\mathrm{ed}, \mathrm{y}} / \mathrm{w}_{\mathrm{y}}=17.4 \\
\mathrm{f}_{\mathrm{m}, \mathrm{~d}}=25 \mathrm{~N} / \mathrm{mm}^{2} \\
\sigma_{\mathrm{c}, \mathrm{o}, \mathrm{~d}}=\mathrm{N}_{\mathrm{ed}} / \mathrm{A}=0.29 \\
\mathrm{f}_{\mathrm{c}, \mathrm{o}, \mathrm{~d}}=21.56 \\
\mathrm{~K}_{\mathrm{c}, \mathrm{y}}=0.72
\end{gathered}
$$

$$
\left(\sigma_{m, d} / k_{c r i t} \times f_{m, d}\right)^{2}+\left(\sigma_{c, 0, d} / k_{c, 2} x f_{c, 0, d}\right)=0.7<1.0
$$

good.
7.5 m beam with a $550 \times 202$ cross-section:

$$
\begin{gathered}
\sigma_{m, d}=M_{e d, y} / w_{y}=22.3 \mathrm{~N} / \mathrm{mm}^{2} \\
f_{m, d}=25 \mathrm{~N} / \mathrm{mm}^{2} \\
\sigma_{\mathrm{c}, \mathrm{o}, \mathrm{~d}}=\mathrm{N}_{\mathrm{ed}} / \mathrm{A}=0.406 \mathrm{~N} / \mathrm{mm}^{2} \\
\mathrm{f}_{\mathrm{c}, \mathrm{~d}, \mathrm{~d}}=21.56 \mathrm{~N} / \mathrm{mm}^{2} \\
\mathrm{~K}_{\mathrm{c}, \mathrm{y}}=0.8 \\
\left(\sigma_{\mathrm{m}, \mathrm{~d}} / \mathrm{k}_{\mathrm{crit}} \times \mathrm{f}_{\mathrm{m}, \mathrm{~d}}\right)^{2}+\left(\sigma_{\mathrm{c}, \mathrm{o}, \mathrm{~d}} / \mathrm{k}_{\mathrm{c}, 2} \times \mathrm{f}_{\mathrm{c}, 0, \mathrm{~d}}\right)=0.82<1.0
\end{gathered}
$$

good.

Beam at the perimeter of the building $550 \times 148 \mathrm{~mm}$

$$
\sigma_{m, d}=M_{e d, y} / w_{y}=22.3 \mathrm{~N} / \mathrm{mm}^{2}
$$

$$
\mathrm{f}_{\mathrm{m}, \mathrm{~d}}=25 \mathrm{~N} / \mathrm{mm}^{2}
$$

$$
\begin{gathered}
\sigma_{\mathrm{c}, \mathrm{o}, \mathrm{~d}}=\mathrm{N}_{\mathrm{ed}} / \mathrm{A}=0.407 \mathrm{~N} / \mathrm{mm}^{2} \\
\mathrm{f}_{\mathrm{c}, 0, \mathrm{~d}}=21.56 \mathrm{~N} / \mathrm{mm}^{2} \\
\mathrm{~K}_{\mathrm{c}, \mathrm{y}}=0.8 \\
\left(\sigma_{\mathrm{m}, \mathrm{~d}} / \mathrm{k}_{\mathrm{crit}} \times \mathrm{f}_{\mathrm{m}, \mathrm{~d}}\right)^{2}+\left(\sigma_{\mathrm{c}, \mathrm{o}, \mathrm{~d}} / \mathrm{k}_{\mathrm{c}, 2} \times \mathrm{f}_{\mathrm{c}, 0, \mathrm{~d}}\right)=0.82<1.0 \\
\text { good. }
\end{gathered}
$$

11m beam supporting the roof with $700 \times 202$ cross-section:

$$
\begin{gathered}
\sigma_{m, d}=M_{e d, y} / w_{y}=19.25 \\
f_{m, d}=25 N / \mathrm{mm}^{2} \\
\sigma_{\mathrm{c}, 0, \mathrm{~d}}=\mathrm{N}_{\mathrm{ed}} / \mathrm{A}=0.29 \\
\mathrm{f}_{\mathrm{c}, 0, \mathrm{~d}}=21.56 \\
\mathrm{~K}_{\mathrm{c}, \mathrm{y}}=0.92 \\
\left(\sigma_{\mathrm{m}, \mathrm{~d}} / \mathrm{k}_{\mathrm{crit}} \times \mathrm{f}_{\mathrm{m}, \mathrm{~d}}\right)^{2}+\left(\sigma_{\mathrm{c}, \mathrm{o}, \mathrm{~d}} / \mathrm{k}_{\mathrm{c}, 2} \times \mathrm{f}_{\mathrm{c}, 0, \mathrm{~d}}\right)=0.61<1.0
\end{gathered}
$$

All beams pass the test for combined action.

## 11.2 serviceability limit state

The beams need to be checked for failure in serviceability limit state due to deflection. If a beam bends more than the limiting value it needs to be re-dimensioned. Calculations are done according to NS-EN 1995-1-1:2004+A1:2008+NA:2010. [15]

$$
\begin{aligned}
& W_{\text {inst }, G}=\text { deflection due to permanent loads }=5 / 384 \times\left(1.0 \times g_{k} / E_{0, \text { mean }} \times 1\right) \times L^{4} \\
& \mathrm{~W}_{\text {fin }, \mathrm{G}}=\mathrm{W}_{\text {inst, }} \mathrm{E} \times\left(1-\mathrm{k}_{\text {def }}\right) \text { where } \mathrm{k}_{\text {def }}=0.6 \text { for service class } 1 \text {. } \\
& W_{\text {inst }, Q}=5 / 384 \times\left(1.0 \times q_{k} / E_{0, \text { mean }} \times 1\right) \times L^{4} \\
& \mathrm{~W}_{\text {fin }, \mathrm{G}}=\mathrm{W}_{\text {inst, }, \mathrm{Q}} \times\left(1-\psi_{2} \times \mathrm{k}_{\text {def }}\right) \\
& \psi_{2}=0.6 \\
& \mathrm{~W}_{\text {fin }}=\mathrm{W}_{\text {fin }, \mathrm{G}}+\mathrm{W}_{\text {fin }, \mathrm{Q}}>\mathrm{L} / 300 \mathrm{~mm} \text { to pass the check. From table } 7.2 \text { in the NS. } \\
& \mathrm{g}_{\mathrm{k}}=2.624 \mathrm{kN} \\
& \mathrm{I}=\mathrm{bh}^{3} / 12=5.773 \times 10^{9} \mathrm{~mm}^{4} \\
& \mathrm{E}_{0, \text { mean }}=14700 \\
& W_{\text {inst }, G}=5.89 \mathrm{~mm} \\
& W_{\text {fin }, G}=W_{\text {inst }, G} \times(1-0.6)=2.36 \mathrm{~mm}
\end{aligned}
$$

$q_{k}=1.2 \mathrm{kN}$
$\mathrm{w}_{\text {inst, } \mathrm{Q}}=10.8 \mathrm{~mm}$
$\mathrm{~W}_{\text {fin }, \mathrm{Q}}=10.8 \times(1-0.6 \times 0.6)=6.91 \mathrm{~mm}$
$\mathrm{w}_{\text {fin }}=9.27<\mathrm{w}_{\text {lim }}=11000 / 300=36.6 \mathrm{~mm}$
Good.

## 8m span:

$g_{k}=8.3 \mathrm{kN}$
$q_{k}=15 \mathrm{kN}$
$W_{\text {inst }, G}=5.21 \mathrm{~mm}$
$W_{\text {fin, }}=2.08$
$W_{\text {inst }, \mathrm{Q}}=18.9 \mathrm{~mm}$
$\mathrm{W}_{\mathrm{fin}, \mathrm{Q}}=12.66 \mathrm{~mm}$
$\mathrm{W}_{\text {fin }}=14.74 \mathrm{~mm}<\mathrm{W}_{\text {lim }}=26.66 \mathrm{~mm}$
Good.

## 7.5 m span:

$\mathrm{I}=2.8 \times 10^{9} \mathrm{~mm}^{4}$
$g_{k}=8.3 \mathrm{kN}$
$q_{k}=15 \mathrm{kN}$
$W_{\text {inst }, G}=8.31 \mathrm{~mm}$
$\mathrm{W}_{\mathrm{fin}, \mathrm{G}}=3.32$
$W_{\text {inst }, ~}=15.0 \mathrm{~mm}$
$\mathrm{w}_{\mathrm{fin}, \mathrm{Q}}=9.6 \mathrm{~mm}$
$\mathrm{W}_{\text {fin }}=12.92<\mathrm{W}_{\text {lim }}=25 \mathrm{~mm}$
Good.
Floor joists:
$\mathrm{I}=1.2 \times 10^{8} \mathrm{~mm}^{4}$
$g_{k}=0.6 \mathrm{kN} / \mathrm{m}$
$q_{\mathrm{k}}=0.96 \mathrm{kN} / \mathrm{m}$
$\mathrm{w}_{\text {inst, } \mathrm{g}}=14.0 \mathrm{~mm}$
$W_{\text {fin }, G}=5.61 \mathrm{~mm}$
$W_{\text {inst }, \mathrm{Q}}=22.4 \mathrm{~mm}$
$\mathrm{W}_{\text {fin }, \mathrm{Q}}=14.3 \mathrm{~mm}$

$$
\begin{gathered}
\mathrm{W}_{\text {fin }}=19.9 \mathrm{~mm}<\mathrm{W}_{\text {lim }}=25 \mathrm{~mm} \\
\text { Good. }
\end{gathered}
$$

all beams and joists pass the check for failure in the serviceability limit state.
After checking for failure, we end up with these beams:
Table 11 final beam dimensions

| position | Thickness mm | Height mm | $\mathrm{M}_{\mathrm{y}, \mathrm{r} \mathrm{c}} \mathrm{kNm}$ | $\mathrm{V}_{\mathrm{y}, \mathrm{rd}} \mathrm{kN}$ |
| :---: | :---: | :---: | :---: | :---: |
| $\mathrm{X}_{1,5}$ | 202 | 550 | 254.6 | 177.1 |
| $\mathrm{Y}_{2,4}$ | 202 | 700 | 412.4 | 225.48 |
| $\mathrm{Y}_{1,6}$ | 202 | 550 | 254.6 | 177.1 |
| $\mathrm{X}_{2,3,4}$ | 202 | 550 | 254.6 | 177.1 |
| For roof | 202 | 700 | 412.4 | 225.48 |

and these columns:
Table 12 final column dimensions

| Position | Cross-section | $N_{r d}$ |
| :---: | :---: | :---: |
| Corners | $400 \times 400$ | 3449.6 kN |
| Edges | $600 \times 400$ | 5174.4 kN |
| Internal | $400 \times 400$ | 3449.6 kN |



Figure 7 the building seen from $X$-axis


Figure 8 the building seen from $Y$-axis

## 12 structure made from concrete

The walls and floors will remain the same as before, the dimensioning being done with columns and beams made from B30 concrete with $\mathrm{c} / \mathrm{s} 20 \mathrm{~mm}$ double rebar and 50 mm cnom. Using the same bending moments due to the weight of floors, walls and imposed loads as before. Since the biggest strength loss of concrete in a fire-situation is the loss of tensilestrength, shear forces for the beams will not be calculated. The calculations are done in accordance with NS-EN 1992-1-1:2004+NA:2008. [18]

### 12.1 Beams in bending

$$
\frac{8 \text { meter beam: }}{M_{\text {ed }}=340.56 \mathrm{kNm}}
$$

$$
\begin{gathered}
V_{\mathrm{ed}}=128 \mathrm{kN} \\
\mathrm{f}_{\mathrm{yk}}=500 \mathrm{~N} / \mathrm{mm}^{2} \\
\mathrm{f}_{\mathrm{yd}}=434.8 \mathrm{~N} / \mathrm{mm}^{2} \\
\mathrm{f}_{\mathrm{ck}}=30 \mathrm{~N} / \mathrm{mm}^{2} \\
\mathrm{f}_{\mathrm{cd}}=17 \mathrm{~N} / \mathrm{mm}^{2} \\
\mathrm{C}_{\text {nom }}=50 \mathrm{~mm} \\
\mathrm{~h}=700 \mathrm{~mm} \\
\mathrm{t}=202 \mathrm{~mm} \\
\mathrm{~d}=632 \mathrm{~mm} \\
\mathrm{~d}^{\prime}=68 \mathrm{~mm}
\end{gathered}
$$

Calculating the steel area in tension:
$A_{s, \text { tension }}=M_{\text {bal }} / 0.82 \times d \times f_{y d}+\left(M_{e d}-M_{\text {bal }}\right) /\left(d-d^{\prime}\right) \times f_{y d}=1640 m^{2}->$ with 5 bars $A_{s}=1570 \mathrm{~mm}^{2}$
$\mathrm{A}_{\mathrm{s}, \text { compression }}=$ using 2 bars $=628 \mathrm{~mm}^{2}$
$M_{\text {bal }}=0.167 \times b \times d^{2} \times f_{c k}=4.15 \times 10^{8}$
$x=f_{y d} \times\left(A_{s, \text { tension }}-A_{s, \text { compression }}\right) / 0.8 \times b \times f_{c d}=149.1<0.617 \times d=394.88$ to ensure failure of tensile $r / f$.
$M_{r d}=0.8 \times X \times b \times f_{c d} \times(d-0.4 X)+f_{y d} \times A_{s, c o m p} \times\left(d-d^{\prime}\right)=396 \mathrm{kNm}$
bar spacing, $A_{h}$, is then 17.2 mm . minimum spacing is 40 mm . we need to try a wider crosssection of 400 mm .
$A_{s, \text { tension }}=M_{\text {bal }} / 0.82 \times d \times f_{y d}+\left(M_{\text {ed }}-M_{\text {bal }}\right) /\left(d-d^{\prime}\right) \times f_{y d}=1676.8 \mathrm{~mm}^{2}->$ with 6 bars $A_{s}=1884 \mathrm{~mm}^{2}$
$\mathrm{A}_{\mathrm{s}, \text { compression }}=$ using 2 bars $=628 \mathrm{~mm}^{2}$
$M_{b a l}=0.167 \times b \times d^{2} \times f_{c k}=8.0 \times 10^{8}$
$x=f_{y d} \times\left(A_{s, \text { tension }}-A_{s, c o m p r e s s i o n}\right) / 0.8 \times b \times f_{c d}=100.4<0.617 \times d=390$ to ensure failure of tensile $r / f$. $M_{r d}=0.8 \times X \times b \times f_{c d} \times(d-0.4 X)+f_{y d} \times A_{s, c o m p} \times\left(d-d^{\prime}\right)=477.2 k N m$ $A_{h}=44 \mathrm{~mm}$. the self-weight of the beam adds to the moment with 56 kNm .

$$
\mathrm{M}_{\mathrm{rd}}=477.2 \mathrm{kNm}>\mathrm{M}_{\mathrm{ed}}=396.56 \mathrm{kNm} .
$$

For the 7.5 m span:

$$
\begin{gathered}
\mathrm{M}_{\mathrm{ed}}=227.3 \mathrm{kNm} \\
\mathrm{f}_{\mathrm{yk}}=500 \mathrm{~N} / \mathrm{mm}^{2} \\
\mathrm{f}_{\mathrm{yd}}=434.8 \mathrm{~N} / \mathrm{mm}^{2} \\
\mathrm{f}_{\mathrm{ck}}=30 \mathrm{~N} / \mathrm{mm}^{2} \\
\mathrm{f}_{\mathrm{cd}}=17 \mathrm{~N} / \mathrm{mm}^{2} \\
\mathrm{C}_{\mathrm{nom}}=50 \mathrm{~mm} \\
\mathrm{~h}=550 \mathrm{~mm} \\
\mathrm{t}=400 \mathrm{~mm} \\
\mathrm{~d}=482 \mathrm{~mm} \\
\mathrm{~d}^{\prime}=68 \mathrm{~mm}
\end{gathered}
$$

Calculating the steel area in tension:

$$
\begin{gathered}
A_{s, \text { tension }}=M_{\text {bal }} / 0.82 \times d \times f_{y d}+\left(M_{\text {ed }}-M_{\text {bal }}\right) /\left(d-d^{\prime}\right) \times f_{y d}=1385 \mathrm{~mm}^{2}->\text { with } 5 \text { bars } A_{s}=1570 \mathrm{~mm}^{2} \\
A_{s, \text { compression }}=u s i n g 2 \text { bars }=628 \mathrm{~mm}^{2} \\
M_{\text {bal }}=0.167 \times b \times d^{2} \times f_{c k}=4.66 \times 10^{8}
\end{gathered}
$$

$x=f_{y d} \times\left(A_{s, t e n s i o n}-A_{s, c o m p r e s s i o n ~}\right) / 0.8 \times b \times f_{c d}=75<0.617 \times d=297.4$ to ensure failure of tensile $r / f$.

$$
M_{r d}=0.8 \times X \times b \times f_{c d} \times(d-0.4 X)+f_{y d} \times A_{s, c o m p} \times\left(d-d^{\prime}\right)=297.4 \mathrm{kNm}
$$

with two layers of rebar we can make the beam 300 mm wide with $A_{v}=32 \mathrm{~mm}$, new $d=465 \mathrm{~mm}$ and $A_{h}=55 \mathrm{~mm}$. $\mathrm{M}_{\mathrm{rd}}=282.4 \mathrm{kNm}>\mathrm{M}_{\mathrm{ed}}=256.7$.

## For the span of 11 meters

$$
\begin{gathered}
\mathrm{M}_{\mathrm{ed}}=227.3 \mathrm{kNm} \\
\mathrm{f}_{\mathrm{yk}}=500 \mathrm{~N} / \mathrm{mm}^{2} \\
\mathrm{f}_{\mathrm{yd}}=434.8 \mathrm{~N} / \mathrm{mm}^{2} \\
\mathrm{f}_{\mathrm{ck}}=30 \mathrm{~N} / \mathrm{mm}^{2} \\
\mathrm{f}_{\mathrm{cd}}=17 \mathrm{~N} / \mathrm{mm}^{2} \\
\mathrm{c}_{\mathrm{nom}}=50 \mathrm{~mm} \\
\mathrm{~h}=700 \mathrm{~mm} \\
\mathrm{~b}=300 \mathrm{~mm} \\
\mathrm{~d}=632 \mathrm{~mm} \\
\mathrm{~d}^{\prime}=68 \mathrm{~mm}
\end{gathered}
$$

Calculating the steel area in tension:
$A_{s, \text { tension }}=M_{\text {bal }} / 0.82 \times d \times f_{y d}+\left(M_{\text {ed }}-M_{\text {bal }}\right) /\left(d-d^{\prime}\right) \times f_{y d}=1676.8 \mathrm{~mm}^{2}->$ with 6 bars $A_{s}=1884 \mathrm{~mm}^{2}$
$A_{s, \text { compression }}=u s i n g 2$ bars $=628 \mathrm{~mm}^{2}$
$M_{b a l}=0.167 \times b \times d^{2} \times f_{c k}=8.0 \times 10^{8}$
$x=f_{y d} \times\left(A_{s, \text { tension }}-A_{s, c o m p r e s s i o n}\right) / 0.8 \times b \times f_{c d}=100.4<0.617 \times d=390$ to ensure failure of tensile $r / f$. $M_{r d}=0.8 \times X \times b \times f_{c d} \times(d-0.4 X)+f_{y d} \times A_{s, c o m p} \times\left(d-d^{\prime}\right)=477.2 k N m$
$A_{h}=44 \mathrm{~mm}$. using two layers of rebar with $A_{v}=32 \mathrm{~mm}$ new $d=618 \mathrm{~mm}$ we can make the crosssection $300 \mathrm{~mm} \times 700 \mathrm{~mm}$. $A_{h}=41 \mathrm{~mm}$ with a $M_{r d}=456.0 \mathrm{kNm}$. seeing that this strength is sufficient for beams $Y_{2,4}$ it will be used there as well.
the self-weight adds to the moment with $\mathrm{M}_{\mathrm{ed}}=79.4 \mathrm{kNm}$, new $\mathrm{M}_{\mathrm{ed}}=306.7 \mathrm{kNm}$.

## Beams around the perimeter of the building

$$
\begin{gathered}
\mathrm{M}_{\mathrm{ed}}=157.9 \mathrm{kNm} \\
\mathrm{f}_{\mathrm{yk}}=500 \mathrm{~N} / \mathrm{mm}^{2} \\
\mathrm{f}_{\mathrm{yd}}=434.8 \mathrm{~N} / \mathrm{mm}^{2} \\
\mathrm{f}_{\mathrm{ck}}=30 \mathrm{~N} / \mathrm{mm}^{2} \\
\mathrm{f}_{\mathrm{cd}}=17 \mathrm{~N} / \mathrm{mm}^{2} \\
\mathrm{c}_{\mathrm{nom}}=50 \mathrm{~mm} \\
\mathrm{~h}=550 \mathrm{~mm} \\
\mathrm{~b}=300 \mathrm{~mm} \\
\mathrm{~d}=482 \mathrm{~mm} \\
\mathrm{~d}^{\prime}=68 \mathrm{~mm}
\end{gathered}
$$

Calculating the steel area in tension:
$A_{s, \text { tension }}=M_{\text {bal }} / 0.82 \times d \times f_{y d}+\left(M_{\text {ed }}-M_{\text {bal }}\right) /\left(d-d^{\prime}\right) \times f_{y d}=1354 m^{2}->$ with 5 bars $A_{s}=1570 m^{2}$
$\mathrm{A}_{\mathrm{s}, \text { compression }}=$ using 2 bars $=628 \mathrm{~mm}^{2}$
$M_{\text {bal }}=0.167 \times b \times d^{2} \times f_{c k}=3.49 \times 10^{8}$
$x=f_{y d} \times\left(A_{s, \text { tension }}-A_{s, \text { compression }}\right) / 0.8 \times b \times f_{c d}=100<0.617 \times d=284.6$ to ensure failure of tensile $r / f$.

$$
M_{r d}=0.8 \times X \times b \times f_{c d} \times(d-0.4 X)+f_{y d} \times A_{s, c o m p} \times\left(d-d^{\prime}\right)=279.2 \mathrm{kNm}
$$

the bars will be spaced to close, bars in tension needs to be put in two layers with $A_{v}=32 \mathrm{~mm}$ $\mathrm{d}=461.2 \mathrm{~mm}$. $\mathrm{M}_{\mathrm{rd}}=279.2>$ new $\mathrm{M}_{\mathrm{ed}}=191.3 \mathrm{kNm}$.

Table 13 beams made from concrete

| position | Cross-section | $\mathrm{M}_{\text {rd }} \mathrm{kNm}$ | $\mathrm{M}_{\text {ed }} \mathrm{kNm}$ |
| :---: | :---: | :---: | :---: |
| $\mathrm{Y}_{2,4}$ | $700 \times 300$ | 456.0 | 396.56 |
| $\mathrm{Y}_{1,2}$ and $\mathrm{X}_{1,2}$ | $550 \times 300$ | 279.2 | 191.3 |
| $\mathrm{X}_{2,3,4,5}$ | $550 \times 300$ | 282.4 | 256.7 |
| For the roof | $700 \times 300$ | 456.0 | 306.7 |

## 12.2 concrete columns

The columns will be designed in the same manner as the beams, with $\mathrm{C}_{\text {nom }}=50 \mathrm{~mm}$ and B30 concrete with 8 mm stirrups and 20 mm bars. The compressive force will be higher than for the wooden construction due to the self-weight of the concrete columns and beams.

## The corner columns:

The columns on the corners are subject to bending in two directions, the reinforcement should therefore be placed on all sides of the column.
from beams $=1.2 \times 25 \times(0.55 \times 0.3 \times 7.75) \times 7=268.54 \mathrm{kN}$.
from floors $=1.764(20.6+15 \times 6)=195.1 \mathrm{kN}$.
imposed loads $=1.5 \times(4+1.2) \times 20.6+1.5 \times(3 \times 5) \times 15=498.18 \mathrm{kN}$.
from glass $=1.2 \times 0.29 \times 240=83.5$
combined load is 1045.32 kN .
if we consider a cross-section of $350 \times 350 \mathrm{~mm}$ self-weight will be $88.8 \mathrm{kN} \mathrm{M}_{\mathrm{ed}}=182.9 \mathrm{kNm}$,
$\mathrm{N}_{\mathrm{ed}}=1134.13 \mathrm{kN}$ and $\mathrm{h}^{\prime}=214 \mathrm{~mm}$.
$h^{\prime} / h=0.61$
$\mathrm{A}_{c}=b \times h=122500$
$\mathrm{n}=\mathrm{N}_{\mathrm{ed}} / \mathrm{f}_{\mathrm{cd}} \times \mathrm{A}_{\mathrm{c}}=0.54$
$\mathrm{m}=\mathrm{M}_{\mathrm{ed}} / \mathrm{f}_{\mathrm{cd}} \times \mathrm{A}_{c} \times \mathrm{h}=0.25$
$\mathrm{w}=0.2$ from diagram 1.3 found in EC clause 9.5
$A_{s}{ }^{\prime}=A_{s}=w \times A_{c} \times f_{c d} / f_{y d}=957.9 \mathrm{~mm}^{2}->4$ bars on each side $=1256 \mathrm{~mm}^{2}<A_{s, m a x} / 2=4900 \mathrm{~mm}^{2}$ spacing of the of stirrups is 250 mm . spacing of the longitudinal bars are 50 mm .

$$
N_{r d}=A_{c} \times f_{c d}+A_{s} \times f_{y d}=3174.7 \mathrm{kN}>\mathrm{N}_{\mathrm{ed}}=1134.13 \mathrm{kN}
$$

## Columns on the perimeter

$$
\begin{gathered}
\text { from beams }=25 \times 0.7 \times 0.4 \times(7.5+4) \times 7=563.5 \mathrm{kN} . \\
\text { from floors }=1.764 \times(30 \times 5+41.25)=317.52 \mathrm{kN} . \\
\quad \text { from walls }=1.2 \times 0.62 \times 4 \times 3.3 \times 5=49.1 \mathrm{kN} \\
\text { imposed loads }=1.5 \times(4 \times 41.25+3 \times 5 \times 30)=909 \mathrm{kN} . \\
\text { from roof }=(1.2 \times 2+1.5 \times 1.2) \times 41.25=173.25 \mathrm{kN}
\end{gathered}
$$

combined load is 2012.4 kN . with a $400 \times 600$ cross-section $\mathrm{M}_{\mathrm{ed}}=603.7 \mathrm{kNm}$ and $\mathrm{N}_{\mathrm{ed}}=2186.4 \mathrm{kN}$.

$$
\begin{gathered}
\mathrm{h}^{\prime}=464 \mathrm{~mm} \\
\mathrm{~h}^{\prime} / \mathrm{h}=0.77 \\
\mathrm{~A}_{\mathrm{c}}=\mathrm{b} \times \mathrm{h}=240000 \\
\mathrm{n}=\mathrm{N}_{\mathrm{ed}} / \mathrm{f}_{\mathrm{cd}} \times \mathrm{A}_{\mathrm{c}}=0.53 \\
\mathrm{~m}=\mathrm{M}_{\mathrm{ed}} / \mathrm{f}_{\mathrm{cd}} \times \mathrm{A}_{\mathrm{c}} \times \mathrm{h}=0.25
\end{gathered}
$$

$\mathrm{w}=0.2$ from diagram 1.3 found in EC clause 9.5
$A_{s}{ }^{\prime}=A_{s}=w \times A_{c} \times f_{c d} / f_{y d}=1876.7 \mathrm{~mm}^{2}->6$ bars on each side $=1884 \mathrm{~mm}^{2}<A_{s, m a x} / 2=9600 \mathrm{~mm}^{2}$ spacing of the of stirrups is 250 mm . spacing of the longitudinal bars are 44 mm .

$$
N_{r d}=A_{c} \times f_{c d}+A_{s} \times f_{y d}=5718.3 \mathrm{kN}>\mathrm{N}_{\mathrm{ed}}=2186.4 \mathrm{kN} .
$$

## Central columns:

the central columns are only subjected to compression.
from beams $=25 \times 0.7 \times 0.4 \times(4+3.75+7.5) \times 7=747.25 \mathrm{kN}$.
from floors $=1.764 \times(41.25 \times 6)=436.6 \mathrm{kN}$.
from roof $=1.2 \times 2 \times 71.25=171.0 \mathrm{kN}$
from walls $=1.2 \times 42.9 \times 0.62 \times 6=191.5 \mathrm{kN}$
imposed loads $=1.5 \times(3 \times 5 \times 41.25+4 \times 41.25+1.2 \times 71.25)=1303.9 \mathrm{kN}$.
combined load is $\mathrm{N}_{\text {ed }}=2850.3 \mathrm{kN}$. seeing that a cross-section of $350 \times 350 \mathrm{~mm}$ as used for the corners is strong enough it will be utilized.

Table 14 columns made from concrete

| Position | Cross-section | $\mathrm{N}_{\mathrm{rd}}$ | $\mathrm{N}_{\text {ed }}$ |
| :---: | :---: | :---: | :---: |
| corners | $350 \times 350$ | 3174.7 | 1134.13 |
| perimeter | $400 \times 600$ | 5718.3 | 2186.4 |
| internal | $350 \times 350$ | 3174.7 | 2966.3 |

## 13 Concrete structure in a fire-situation

Calculations are done according to NS-EN 1992-1-2: 2004+NA: 2010- Design of Concrete StructuresPart 1-2: Structural Fire Design. [19]

### 13.1 Beams

## 8 meter beam

load due to self-weight of the beams $=0.7 \times 0.4 \times 25=7.0 \mathrm{kN} / \mathrm{m}$
from walls $=1.0 \times 4 \mathrm{~m} \times 0.62=3.104 \mathrm{kN} / \mathrm{m}$
from floors $=1.0 \times 1.47 \mathrm{kN} / \mathrm{m}^{2}=1.47 \mathrm{kN} / \mathrm{m}^{2}$
imposed load $=0.7 \times 4.0 \mathrm{kN} / \mathrm{m}^{2}=2.8 \mathrm{kN} / \mathrm{m}^{2}$
this means $\mathrm{M}_{\mathrm{d}, \mathrm{fi}}=251.66 \mathrm{kNm}$
the calculation of fire resistance is based on tabulated date regarding critical temperature of the reinforcement steel.

$$
\begin{gathered}
A_{s, \text { required }}=1676.8 \mathrm{~mm}^{2} \\
A_{s, \text { provided }}=1884 \mathrm{~mm}^{2} \\
M_{d}=396.56 \mathrm{kNm} \\
Y_{s}=1.15 \\
\sigma_{s, f i}=M_{d, f i} \times f_{y k} \times A_{s, \text { required }} / M_{d} \times Y_{s} \times A_{s, \text { provided }}=245.57 \\
K_{s(\Theta c r)}=\sigma_{s, f i} / f_{y k}=0.49
\end{gathered}
$$

$\Theta_{\mathrm{cr}}=530^{\circ} \mathrm{C}>500^{\circ} \mathrm{C}$ no adjustments needed (from fig.5.1 of the standard) as it is exposed on 2 sides minimum width is 300 mm and cover to reinforcement is 40 mm .

From table 5.5. the cross section is good for R90.

## For the 7.5 meter beam:

$M_{d, f i}=211.17$
$\mathrm{A}_{\mathrm{s}, \text { required }}=1385.0 \mathrm{~mm}^{2}$
$A_{s, \text { provided }}=1570.0 \mathrm{~mm}^{2}$

$$
\mathrm{M}_{\mathrm{d}}=256.7 \mathrm{kNm}
$$

$Y_{s}=1.15$
$\sigma_{s, f i}=M_{d, f i} \times f_{y k} \times A_{s, \text { required }} / M_{d} \times Y_{s} \times A_{s, \text { provided }}=315.5$

$$
\mathrm{K}_{\mathrm{s}(\Theta \mathrm{cr})}=\sigma_{\mathrm{s}, \mathrm{fi}} / \mathrm{f}_{\mathrm{yk}}=0.63
$$

$\Theta_{\mathrm{cr}}=460^{\circ} \mathrm{C}>500^{\circ} \mathrm{C}$ adjustments are needed (from fig.5.1)
Need to change the minimum distance to reinforcement $\Delta a=0.1 \times\left(500-\theta_{\text {cr }}\right)=4 \mathrm{~mm}$ as it is exposed on 2 sides minimum width is 300 mm and cover to reinforcement is $40+\Delta a=44 \mathrm{~mm}$. From table 5.5. the cross section is good for $R 90$.

## 11meter beams holding up the roof:

$$
M_{\mathrm{d}, \mathrm{fi}}=283.7
$$

$\mathrm{A}_{\mathrm{s}, \text { required }}=1676.8 \mathrm{~mm}^{2}$
$A_{s, \text { provided }}=1884.0 \mathrm{~mm}^{2}$
$\mathrm{M}_{\mathrm{d}}=456.0 \mathrm{kNm}$
$Y_{\mathrm{s}}=1.15$
$\sigma_{s, f i}=M_{d, f i} \times f_{y k} \times A_{s, r e q u i r e d} / M_{d} \times Y_{s} \times A_{s, p r o v i d e d}=240.8$
$\mathrm{K}_{\mathrm{s}(\theta \mathrm{cr})}=\sigma_{\mathrm{s}, \mathrm{f}} / \mathrm{f}_{\mathrm{yk}}=0.48$
$\theta_{\mathrm{cr}}=540^{\circ} \mathrm{C}>500^{\circ} \mathrm{C}$ no adjustments are needed (from fig.5.1)
as it is exposed on 3 sides minimum width is 300 mm and cover to reinforcement is 40 mm .
From table 5.5. the cross section is good for R90.

$$
\begin{gathered}
\text { perimeter beams: } \\
M_{d, f i}=130.4 \\
A_{s, \text { required }}=1354 \mathrm{~mm}^{2} \\
A_{s, \text { provided }}=1570.0 \mathrm{~mm}^{2} \\
M_{d}=191.3 \mathrm{kNm} \\
Y_{s}=1.15 \\
\sigma_{s, \text { fi }}=M_{d, f i} \times f_{y k} \times A_{s, \text { required }} / M_{d} \times Y_{s} \times A_{s, \text { provided }}=255.6 \\
K_{s(\theta c r)}=\sigma_{s, f i} / f_{y k}=0.51
\end{gathered}
$$

$\Theta_{\mathrm{cr}}=520^{\circ} \mathrm{C}>500^{\circ} \mathrm{C}$ no adjustments are needed (from fig.5.1)
as it is exposed on 2 sides minimum width is 300 mm and cover to reinforcement is 40 mm .
From table 5.5. the cross section is good for R90.

## 13.2 columns

## Corner columns:

$$
\begin{gathered}
\mathrm{N}_{\mathrm{d}, \mathrm{fi}}=959.9 \mathrm{kN} \\
\mathrm{~N}_{\mathrm{d}}=1134.14 \mathrm{kN} \\
\mathrm{~A}_{\mathrm{s}, \text { required }}=957.9 \mathrm{~mm}^{2} \\
\mathrm{~A}_{\mathrm{s}, \text { provided }}=1256 \mathrm{~mm}^{2} \\
\sigma_{s, \text { fi }}=\mathrm{N}_{\mathrm{d}, \mathrm{fi}} \times \mathrm{f}_{\mathrm{yk}} \times \mathrm{A}_{\mathrm{s}, \text { required }} / \mathrm{N}_{\mathrm{d}} \times \mathrm{Y}_{\mathrm{s}} \times \mathrm{A}_{\mathrm{s}, \mathrm{provided}}=280.64 \\
\mathrm{~K}_{\mathrm{s}(\Theta \mathrm{Acr})}=\sigma_{\mathrm{s}, \mathrm{fi}} / \mathrm{f}_{\mathrm{yk}}=0.56
\end{gathered}
$$

$\theta_{\text {cr }}=510^{\circ} \mathrm{C}>500^{\circ} \mathrm{C}$ no adjustments are needed (from fig.5.1)
minimum required width and cover to reinforcement is then $b=300 \mathrm{~mm}$ and $\mathrm{C}_{\text {min }}=25 \mathrm{~mm}$ from table 5.2(a). of the standard.

## Internal columns:

$$
\begin{aligned}
& \mathrm{N}_{\mathrm{d}, \mathrm{i}}=1529.9 \mathrm{kN} \\
& \mathrm{~N}_{\mathrm{d}}=2186.4 \mathrm{kN}
\end{aligned}
$$

$\mathrm{A}_{s, \text { required }}=300 \mathrm{~mm}^{2}$
$A_{s, \text { provided }}=628 \mathrm{~mm}^{2}$
$\sigma_{s, f i}=N_{d, f i} \times f_{y k} \times A_{s, \text { required }} / N_{d} \times Y_{s} \times A_{s, \text { provided }}=145.33$
$\mathrm{K}_{\mathrm{s}(\Theta \mathrm{cr})}=\sigma_{\mathrm{s}, \mathrm{fi}} / \mathrm{f}_{\mathrm{yk}}=0.3$
$\Theta_{c r}=610^{\circ} \mathrm{C}>500^{\circ} \mathrm{C}$ no adjustments are needed (from fig.5.1)
minimum required width and cover to reinforcement is then $b=300 \mathrm{~mm}$ and $\mathrm{C}_{\text {min }}=25 \mathrm{~mm}$ from table 5.2(a).

## Columns in the perimeter:

$N_{\mathrm{d}, \mathrm{fi}}=1500.2 \mathrm{kN}$
$\mathrm{N}_{\mathrm{d}}=2186.4 \mathrm{kN}$
$\mathrm{A}_{\mathrm{s}, \text { required }}=1876.7 \mathrm{~mm}^{2}$
$A_{s, \text { provided }}=1884 \mathrm{~mm}^{2}$
$\sigma_{s, f i}=N_{d, f i} \times f_{y k} \times A_{s, \text { required }} / N_{d} \times Y_{s} \times A_{s, \text { provided }}=297.17$
$\mathrm{K}_{\mathrm{s}(\Theta \mathrm{cr})}=\mathrm{\sigma}_{\mathrm{s}, \mathrm{fi}} / \mathrm{f}_{\mathrm{yk}}=0.6$
$\theta_{c r}=500^{\circ} \mathrm{C}>500^{\circ} \mathrm{C}$ no adjustments are needed (from fig.5.1)
minimum required width and cover to reinforcement is then $\mathrm{b}=300 \mathrm{~mm}$ and $\mathrm{C}_{\text {min }}=25 \mathrm{~mm}$ from table $5.2(a)$. well bellow our values of $b=400 \mathrm{~mm}$ and $C_{\text {nom }}=50 \mathrm{~mm}$.

## 14 Structure made from steel

The building will be designed with a structure made from steel beams and columns. The calculations are done according to Eurocode3 -NS-EN 1993-1-1:2005+A1:2014+NA:2015 [20]

### 14.1 Beams

$$
\begin{aligned}
& \underline{Y}_{2,4} \text { with a span of } 8 \text { meters. } \\
& M_{y, e d}=340.56 \mathrm{kNm} \\
& \mathrm{f}_{\mathrm{y}}=355 \mathrm{~N} / \mathrm{mm}^{2} \\
& \mathrm{~W}_{\mathrm{pl}, \mathrm{y}}>\mathrm{M}_{\mathrm{y}, \mathrm{ed}} / \mathrm{f}_{\mathrm{y}}=959.3 \times 10^{3} \\
& \mathrm{~W}_{\mathrm{pl}, \mathrm{y}}=2 \times \mathrm{s}_{\mathrm{y}}=2 \times 527 \times 10^{3} \mathrm{~mm}^{3} \text { for beam HE240-B } \\
& \text { checking class-classification of web and flange. } \\
& \mathrm{cf}_{f} / \mathrm{t}_{\mathrm{fe}}=\left(\left(\mathrm{b}-2 \times \mathrm{r}-\mathrm{t}_{\mathrm{w}}\right) / 2\right) / \mathrm{t}_{\mathrm{fe}}=5.53<9->f \text { lange is in class } 1 \text {. } \\
& c_{w} / t_{w e}=\left(h-2 \times t_{f}-2 \times r\right) / t_{w e}=16.4<72->w e b \text { is class } 1 . \\
& M_{c, r d}=f_{y} \times 2 \times s_{y} / Y_{m, 0}=355 \times 2 \times 527 \times 10^{3} / 1.05 \times 10^{6}=356.35 \mathrm{kNm} \\
& \mathrm{M}_{\mathrm{y}, \mathrm{ed}}=227.3 \mathrm{kNm} \\
& \mathrm{f}_{\mathrm{y}}=355 \mathrm{~N} / \mathrm{mm}^{2} \\
& \mathrm{~W}_{\mathrm{pl}, \mathrm{y}}>\mathrm{M}_{\mathrm{y}, \mathrm{ed}} / \mathrm{f}_{\mathrm{y}}=640.2 \times 10^{3} \\
& \mathrm{~W}_{\mathrm{pl}, \mathrm{y}}=2 \times \mathrm{s}_{\mathrm{y}}=2 \times 414 \times 10^{3} \mathrm{~mm}^{3} \text { for beam HE220-B } \\
& \text { checking class-classification of web and flange. } \\
& \mathrm{c}_{\mathrm{f}} / \mathrm{t}_{\mathrm{fe}}=\left(\left(\mathrm{b}-2 \times \mathrm{r}-\mathrm{t}_{\mathrm{w}}\right) / 2\right) / \mathrm{t}_{\mathrm{fe}}=5.47<9->f \text { lange is in class } 1 \text {. } \\
& c_{w} / t_{w e}=\left(h-2 \times t_{f}-2 \times r\right) / t_{w e}=16.0<72->w e b \text { is class } 1 . \\
& M_{c, r d}=f_{y} \times 2 \times s_{y} / Y_{m, 0}=355 \times 2 \times 414 \times 10^{3} / 1.05 \times 10^{6}=279.9 \mathrm{kNm}
\end{aligned}
$$

$\underline{X}_{1,6}$ and $Y_{1,5}$
$M_{\mathrm{y}, \mathrm{ed}}=157.9 \mathrm{kNm}$
$\mathrm{f}_{\mathrm{y}}=355 \mathrm{~N} / \mathrm{mm}^{2}$
$\mathrm{~W}_{\mathrm{pl}, \mathrm{y}}>\mathrm{M}_{\mathrm{y}, \mathrm{ed}} / \mathrm{f}_{\mathrm{y}}=444.8 \times 10^{3}$
$\mathrm{~W}_{\mathrm{pl}, \mathrm{y}}=2 \times \mathrm{s}_{\mathrm{y}}=2 \times 241 \times 10^{3} \mathrm{~mm}^{3}$ for beam HE180-B
checking class-classification of web and flange.

$$
\begin{gathered}
c_{f} / \mathrm{t}_{\mathrm{f}}=\left(\left(\mathrm{b}-2 \times r-\mathrm{t}_{\mathrm{w}}\right) / 2\right) / \mathrm{t}_{\mathrm{fe}}=5.05<9->\mathrm{flange} \text { is in class } 1 . \\
\mathrm{c}_{\mathrm{w}} / \mathrm{t}_{\mathrm{we}}=\left(\mathrm{h}-2 \times \mathrm{t}_{\mathrm{f}-}-2 \times \mathrm{r}\right) / \mathrm{t}_{\mathrm{we}}=14.4<72->\mathrm{web} \text { is class } 1 . \\
\mathrm{M}_{\mathrm{c}, \mathrm{rd}}=\mathrm{f}_{\mathrm{y}} \times 2 \times \mathrm{s}_{\mathrm{y}} / \mathrm{Y}_{\mathrm{m}, 0}=355 \times 2 \times 241 \times 10^{3} / 1.05 \times 10^{6}=162.96 \mathrm{kNm}
\end{gathered}
$$

For the beams holding up the roof:

$$
M_{y, e d}=317.63 \mathrm{kNm}
$$

we will utilize the same beam HE240-B as for $\mathrm{Y}_{2,3,4}$ with a $\mathrm{M}_{\mathrm{c}, \mathrm{rd}}=356.35 \mathrm{kNm}$.

### 14.2 Columns

## Corner column with a height of 4 meters.

Trying a cross-section of $S H S 200 \times 200 \times 8 \mathrm{~mm} \mathrm{~N}_{\mathrm{ed}}=1940.4 \mathrm{kN}$ and $\mathrm{M}_{\mathrm{ed}, \mathrm{y}}=\mathrm{M}_{\mathrm{ed}, \mathrm{z}}=97.0 \mathrm{kNm}$.

$$
\begin{aligned}
& W_{p l, y}=W_{p l, z}>M_{e d} \times Y_{m, 0} / X_{L T} \times f_{y} \\
& \chi_{\text {LT }}=1.0 \\
& \mathrm{~W}_{\mathrm{pl}}=432>358.8 \\
& \text { classification of cross-section: } \\
& c_{1} / s \times \varepsilon=(h-3 \times s) / s \times 0.92=23.9<33->\text { class } 1 . \\
& \mathrm{N}_{\mathrm{pl}, \mathrm{rd}}=A \times \mathrm{f}_{\mathrm{y}} / \mathrm{Y}_{\mathrm{m}, 0}=2045.5 \mathrm{kN} \\
& M_{n, r d}=\left(W_{p l} \times f_{y} / Y_{m, 0}\right) \times\left(1-n / 1-0.5 a_{w}\right) \\
& \mathrm{n}=\mathrm{N}_{\mathrm{ed}} / \mathrm{N}_{\mathrm{pl}, \mathrm{rd}}=0.96 \\
& a_{w}=(A-2 \times b \times t) / A=0.47 \text { use } 0.5 \\
& \mathrm{M}_{\mathrm{n}, \mathrm{rd}}=7.8 \mathrm{kNm}<97.0 \text {->not ok } \\
& \text { trying cross-section SHS300×300×10 } \\
& \mathrm{W}_{\mathrm{pl}}=1238 \\
& \text { classification of cross-section: } \\
& \mathrm{c}_{1} / \mathrm{s} \times \varepsilon=(\mathrm{h}-3 \times \mathrm{s}) / \mathrm{s} \times 0.92=29.3<33->\text { class } 1 . \\
& N_{p l, r d}=A \times f_{y} / Y_{m, 0}=3854.3 \mathrm{kN} \\
& M_{n, r d}=\left(W_{p l} \times f_{y} / Y_{m, 0}\right) \times\left(1-n / 1-0.5 a_{w}\right) \\
& \mathrm{n}=\mathrm{N}_{\mathrm{ed}} / \mathrm{N}_{\mathrm{pl}, \mathrm{rd}}=0.5 \\
& a_{w}=(A-2 \times b \times t) / A=0.47 \\
& \mathrm{M}_{\mathrm{n}, \mathrm{rd}}=273.5 \mathrm{kNm}>97.0 \text {-> check is ok. }
\end{aligned}
$$

$$
\begin{gathered}
\left(M_{y, e d} / M_{y, \text { rd }}\right)^{\alpha}+\left(M_{z, e d} / M_{z, \text { rd }}\right)^{\beta}<1.0 \\
\alpha=\beta=1.66 / 1-1.13 \times n^{2}=2.31
\end{gathered}
$$

$\left(M_{y, e d} / M_{y, r d}\right)^{\alpha}+\left(M_{z, e d} / M_{z, r d}\right)^{\beta}=0.3<1.0$ cross-section is good.
check for buckling:
expression that needs to be satisfied:

For the columns forming the perimeter of the building:
$N_{\text {ed }}=1515.7 \mathrm{kN}$, if using a cross-section of RHS250x250x10mm $\mathrm{M}_{\text {ed }}=189.46 \mathrm{kNm}$ bending in
one direction.

$$
\begin{gathered}
W_{\mathrm{pl}, \mathrm{y}}=\mathrm{W}_{\mathrm{pl}, 2}>\mathrm{M}_{\mathrm{ed}} \times Y_{\mathrm{m}, 0} / \chi_{\mathrm{LT}} \times \mathrm{f}_{\mathrm{y}} \\
\chi_{\mathrm{LT}}=1.0 \\
\mathrm{~W}_{\mathrm{pl} 1}=845>560.4
\end{gathered}
$$

classification of cross-section:

$$
c_{1} / s \times \varepsilon=(h-3 \times s) / s \times 0.92=23.9<33->\text { class } 1 .
$$

$$
N_{p l, r d}=A \times f_{y} / Y_{m, 0}=3195 \mathrm{kN}
$$

$$
M_{n, r d}=\left(W_{p l} \times f_{y} / Y_{m, 0}\right) \times\left(1-n / 1-0.5 a_{w}\right)
$$

$$
\mathrm{n}=\mathrm{N}_{\mathrm{ed}} / \mathrm{N}_{\mathrm{pl}, \mathrm{rd}}=0.47
$$

$$
a_{w}=(A-2 \times b \times t) / A=0.47 \text { use } 0.5
$$

$N_{\text {ed }}=1515.7 \mathrm{kN}>0.25 \times \mathrm{N}_{\text {pl, rd }}=798.75->\mathrm{N}_{\text {ed }}$ has an effect on bending resistance.
$\mathrm{M}_{\mathrm{n}, \mathrm{rd}}=201.88 \mathrm{kNm}<189.46$->check ok.
check for buckling:
expression that needs to be satisfied:

$$
\begin{gathered}
N_{e d} /\left(\chi_{L T} \times N_{r k} / Y_{m 1}\right)+k_{y y} \times\left(M_{y, e d}+\Delta M_{y, e d}\right) /\left(\chi_{L \tau} \times M_{y, r k} / Y_{m 1}\right)<1.0 \\
N_{r k}=A \times f_{y}=3354.75 \mathrm{kN} \\
M_{y, r k}=M_{z, r k}=w_{p} \times f_{y}=299.98 \mathrm{kNm} \\
\Delta M_{e d}=0 \text { for class } 1 \text { cross-section }
\end{gathered}
$$

$$
\begin{aligned}
& N_{\text {ed }} /\left(\chi_{L T} \times N_{r k} / Y_{m 1}\right)+k_{y y} \times\left(M_{y, \text { ed }}+\Delta M_{y, \text { ed }}\right) /\left(\chi_{L T} \times M_{y, r k} / Y_{m 1}\right)+k_{y z} \times M_{z, e d} / M_{z, r k}<1.0 \\
& \mathrm{~N}_{\mathrm{rk}}=\mathrm{A} \times \mathrm{f}_{\mathrm{y}}=4047.0 \mathrm{kN} \\
& M_{y, r k}=M_{z, r k}=w_{p} \times f_{y}=439.5 \mathrm{kNm} \\
& \Delta M_{\text {ed }}=0 \text { for class } 1 \text { cross-section } \\
& k_{y y}=k_{y z}=1.0 \text { estimated as a simplification. } \\
& N_{\text {ed }} /\left(\chi_{L T} \times N_{r k} / Y_{m 1}\right)+k_{y y} \times\left(M_{y, \text { ed }}+\Delta M_{y, e d}\right) /\left(\chi_{L T} \times M_{y, r k} / Y_{m 1}\right)+k_{y z} \times M_{z, e d} / M_{z, r k}=0.95<1.0 \\
& \text { no buckling occurs. }
\end{aligned}
$$

$k_{y y}=k_{y z}=1.0$ estimated as a simplification.
$N_{e d} /\left(\chi_{L T} \times N_{r k} / Y_{m 1}\right)+k_{y y} \times\left(M_{y, e d}+\Delta M_{y, e d}\right) /\left(\chi_{L T} \times M_{y, r k} / Y_{m 1}\right)=1.14<1.0$
buckling can occur. Try a bigger cross-section, SHS300x300x10mm.

$$
\begin{gathered}
N_{r k}=A \times f_{y}=4047.0 \mathrm{kN} \\
M_{y, r k}=M_{z, r k}=w_{p} \times f_{y}=439.5 \mathrm{kNm} \\
\Delta M_{e d}=0 \text { for class } 1 \text { cross-section } \\
k_{y y}=k_{y z}=1.0 \text { estimated as a simplification. } \\
N_{\text {ed }} /\left(\chi_{L T T} \times N_{r k} / Y_{m 1}\right)+k_{y y} \times\left(M_{y, e d}+\Delta M_{y, e d}\right) /\left(\chi_{L T} \times M_{y, r k} / Y_{m 1}\right)=0.85<1.0 \\
\text { no buckling occurs. }
\end{gathered}
$$

## For the columns in the center

$$
\mathrm{N}_{\mathrm{ed}}=2181.2 \mathrm{kN} \text {. }
$$

choosing SHS300x300x10mm
$N_{c, r d}=A \times f_{y} / Y_{m, 0}=3854.2 \mathrm{kN}>N_{\text {ed }}=2181.2$->no cross-sectional yielding.

$$
\begin{gathered}
N_{b, r d}=\chi \times A \times f_{y} / Y_{m, 1} \\
\chi=1 / \Theta+\left(\Theta^{2}+\lambda^{2}\right)^{0.5} \\
\lambda=L_{c r} \times 1 / i \times \lambda_{1}=0.27 \\
i=118 \mathrm{~mm}
\end{gathered}
$$

$$
\lambda_{1}=86.4 \text { for s355 steel }
$$

$L_{c r}=0.7 \times L$ for a fixed column with pinned top.

$$
\Theta=0.5 \times\left(1+\alpha \times(\lambda-0.2) \times \lambda^{2}=0.5\right.
$$

$\alpha=0.21$ from table 6.2 of the standard.
$\chi=0.93$
$\mathrm{N}_{\mathrm{b}, \mathrm{rd}}=3584.4 \mathrm{kN}>\mathrm{N}_{\text {ed }}=2181.2 \mathrm{kN}$
cross-section will not buckle

Beams:

Table 15 beams made from steel

| position | Cross-section | $M_{c, r d}$ | $M_{\text {ed }}$ |
| :---: | :---: | :---: | :---: |
| $\mathrm{X}_{1,6} \mathrm{Y}_{1,5}$ | HE180-B | 162.96 | 157.9 |


| $X_{2,3,4,5}$ | HE240-B | 356.35 | 340.56 |
| :---: | :---: | :---: | :---: |
| $\mathrm{Y}_{2,4}$ | HE220-B | 279.9 | 227.3 |
| Roof | HE240-B | 356.35 | 317.63 |

Columns:

Table 16 columns made from steel

| position | Cross-section | $\mathrm{N}_{\mathrm{b}, \mathrm{rd}}$ | $\mathrm{N}_{\text {ed }}$ |
| :---: | :---: | :---: | :---: |
| corner | SHS300×300×10 | 3584.4 | 1940.4 |
| perimeter | SHS300x300×10 | 3584.4 | 1515.7 |
| internal | SHS300x300×10 | 3584.4 | 2181.2 |

## 15 Steel structure in a fire-situation

Calculations done according to NS-EN 1993-1-2:2005+NA:2009-Design of Steel Structures-
Part 1-2: Structural Fire Design. [21]

### 15.1 Beams

for beams holding the roof $\mathrm{M}_{\mathrm{ed}, \mathrm{fi}}=181.86 \mathrm{kNm}$ to be suitable in $R 90$ the expression $\Theta_{a, c r}>\Theta_{a, t}$ must be satisfied.
$\Theta_{a, c r}=39.19 \times \ln \left(1 / 0.9674 \times \mu_{0}^{3.833}-1\right)+482^{\circ} \mathrm{C}$ for a class 1 beam.
$\mu_{0}=E_{f i, d} / R_{f i, d, 0}=181.86 / 356.35=0.51$
$\Theta_{\mathrm{a}, \mathrm{cr}}=581.0^{\circ} \mathrm{C}$
$\Theta_{\mathrm{a}, \mathrm{t}}$ is found from table 13.7.

$$
A_{m} / V=68
$$

Table 13.7 in the standard show that after 30 minutes the temperature of the beam is around $750^{\circ} \mathrm{C}$, this beam therefore needs to be protected. By using the calculator for protection with conlit150/150p from rockwool no we see that with a 20 mm layer of insulation the temperature of the beam will be $453^{\circ} \mathrm{C}$ after 90 minutes of exposure. This is satisfactory.

As the thickness of the wall is 202 mm and the floor-joists is 270 mm thick the other steel beams are already protected from the fire by the walls and floors.

### 15.2 Columns

## corner column:

$$
\begin{gathered}
\Theta_{\mathrm{a}, \mathrm{cr}}=39.19 \times \ln \left(1 / 0.9674 \times \mu_{0}^{3.833}-1\right)+482^{\circ} \mathrm{C} \text { for a class } 1 \text { beam. } \\
\qquad \begin{array}{c}
\mu_{0}=\mathrm{E}_{\mathrm{fi}, \mathrm{~d}} / R_{\mathrm{fi}, \mathrm{~d}, 0}=772.42 / 3584=0.22 \\
\Theta_{\mathrm{a}, \mathrm{cr}}=710.6^{\circ} \mathrm{C}
\end{array}
\end{gathered}
$$

$\Theta_{a, t}$ is found from table 13.7.
column is exposed on two sides.

$$
A_{m} / V=52.6
$$

After 30 minutes of exposure the temperature is around $700^{\circ} \mathrm{C}$. The column needs protection. The calculator from rockwool shows that 20 mm of conlit150/150p will keep the temperature at $383^{\circ} \mathrm{C}$ in R90, which is sufficient.

$$
\Theta_{a, t}=383^{\circ} \mathrm{C}<\Theta_{a, c r}=710.6^{\circ} \mathrm{C}
$$

Perimeter columns:
$\Theta_{a, c r}=39.19 \times \ln \left(1 / 0.9674 \times \mu_{0}{ }^{3.833}-1\right)+482^{\circ} \mathrm{C}$ for a class 1 beam.
$\mu_{0}=E_{f i, d} / R_{f i, d, 0}=772.42 / 3584=0.22$

$$
\Theta_{\mathrm{a}, \mathrm{cr}}=710.6^{\circ} \mathrm{C}
$$

$\Theta_{a, t}$ is found from table 13.7.
The column is exposed on three sides.

$$
A_{m} / V=79.0
$$

After 30 minutes of exposure the temperature is around $750^{\circ} \mathrm{C}$. The column needs protection. The calculator from rockwool shows that 20 mm of conlit150/150p will keep the
temperature at $498^{\circ} \mathrm{C}$ in R90, which is sufficient.

$$
\theta_{\mathrm{a}, \mathrm{t}}=498^{\circ} \mathrm{C}<\theta_{\mathrm{a}, \mathrm{cr}}=710.6^{\circ} \mathrm{C}
$$

Inner columns:
$\theta_{a, c r}=39.19 \times \ln \left(1 / 0.9674 \times \mu_{0}^{3.833}-1\right)+482^{\circ} \mathrm{C}$ for a class 1 beam.

$$
\mu_{0}=E_{\mathrm{f}, \mathrm{~d}} / R_{\mathrm{fi}, \mathrm{~d}, 0}=1396.1 / 3584=0.4
$$

$\Theta_{a, c r}=619.8^{\circ} \mathrm{C}$
$\Theta_{\mathrm{a}, \mathrm{t}}$ is found from table 13.7.
The column is exposed on four sides.
$A_{m} / V=105.3$
After 30 minutes of exposure the temperature is around $770^{\circ} \mathrm{C}$. The column needs protection. The calculator from rockwool shows that 20 mm of conlit150/150p will keep the temperature at $595^{\circ} \mathrm{C}$ in R90, which is sufficient.

$$
\Theta_{\mathrm{a}, \mathrm{t}}=595^{\circ} \mathrm{C}<\Theta_{\mathrm{a}, \mathrm{cr}}=619.8^{\circ} \mathrm{C}
$$

## 16 Comparison regarding economy and $\mathrm{CO}_{2-}{ }^{-}$ emmisions.

After dimensioning the building for glue-laminated timber, steel and concrete the dimensions was used in IZY Calcus to get an estimate for the price and $\mathrm{CO}_{2}$ emissions for the structural components with each of the solutions. The buildings made from concrete and steel both had shear-walls made from concrete with a thickness of 200mm. The results can be found in table 17:

Table 17 comparison for economy and $\mathrm{CO}_{2}$-emmisions

| material | Price in NOK | $\mathrm{CO}_{2}$-emmisions in Kg |
| :--- | :--- | :--- |
| Glu-laminated timber | $7536544+3972269$ for shear- <br> walls | $34537+32137$ for shear-wall |
| steel | $9086453+3878128$ | $371985+152982$ |
| concrete | $9011083+3878128$ | $347693+152982$ |

The values listed is the price and emissions from the materials with a 60-year life cycle. The construction of the building its-self is not included. The difference in price is around 1.5 million kroners, with glue-laminated timber being the cheapest. This is not a huge difference, and some of the difference may be due to inaccuracies in the computer program or over dimensioning of elements with concrete and steel. The cost of construction is not taken into account, and might make a difference in the final cost-comparison of the building. The difference in emissions of $\mathrm{CO}_{2}$ however is substantial. With Steel and concrete being almost 10 times more polluting, even when considering a possible flaw in the programing it is obvious that glue-laminated wood is a much more environmentally friendly option.

## 17 Conclusion

The background for this thesis was to do a literature review of the techniques and design considerations when using glue-laminated timber in construction of high-rise buildings. A special emphasis was put on the fire resistance of timber due to the public perception of it being an inferior building material to concrete and steel regarding fire-resistance. when reviving the literature and tests done on the fire-resistance of glue-lam I found there to be a lot of variation in results and in how different tests was performed. The techniques used for calculation and dimensioning of glue-laminated timber elements are also diverse, However, there are standardized and recommended methods for calculating fire resistance. These standard methods have been extensively tested and proves to be both reliable and accurate. The components additive method proved to be effective and practical for calculating protection time of cladding and the reduced cross-section is the advised and proven method for calculation of strength during a fire-situation.

For glue-lam to be a viable building material to replace concrete and steel in the future it must satisfy certain criteria. In best case scenario it would have better structural properties, economic benefits and lower emissions of $\mathrm{CO}_{2}$ associated with its use in construction. In this thesis a load-bearing structure was designed in R90 and comparisons was made between glue-laminated timber, concrete and steel. Timber proved to perform just as well as or better then concrete in bending, we were able to design beams with a smaller cross-section to bear the loads. Timber also proved to be as good as concrete, and better than steel, for fire-resistance. When considering structural elements in compression, concrete performed better. And steel allowed us to design both beams and columns with a smaller cross-section than with timber, however needing protection against fire. After the dimensioning of the structure was finished, IZY calcus was used to calculate the price of the materials and emissions of $\mathrm{CO}_{2}$ in their production. Material amounts for glue-lam and concrete had to be adjusted by volume since we did not utilize standardized dimensions. The difference in price between glue-laminated elements and those made from concrete and steel was found to be around 1.5 million kroners, with glue-lam being the cheapest alternative. The $\mathrm{CO}_{2}$ emissions was found to be almost 10 times higher for both concrete and steel than for a structure
made of glue-laminated elements. Considering these results, I would say glue-laminated timber should become increasingly popular as a building material in the future.

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[^0]:    $t_{\text {prot, }, 0,1}=30 \times\left(h_{1} / 15\right)^{1.2}=30.0 \mathrm{~min}$

